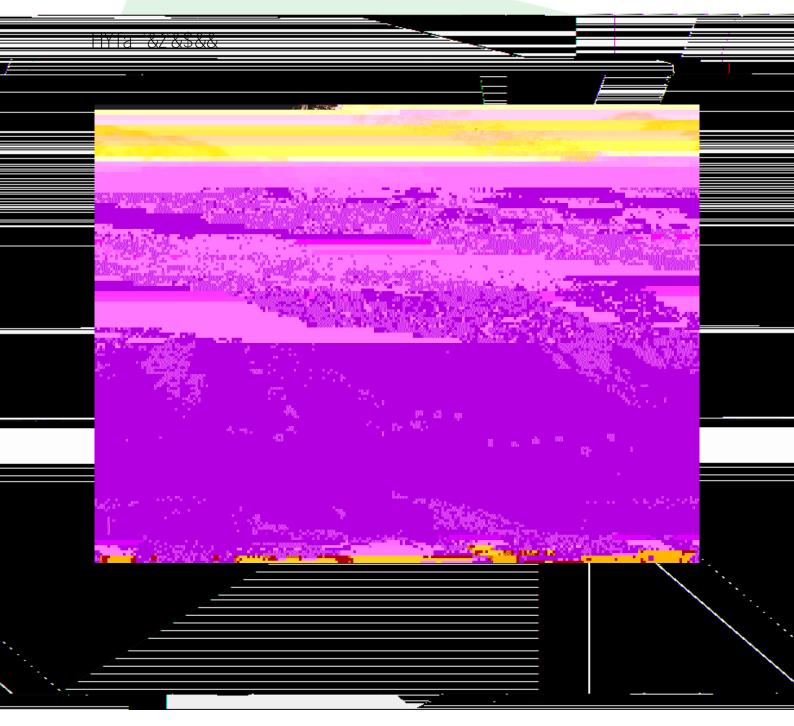


EDST5321

A chj Uhjeb jb 9 Xi WUhjebU`GYHnjb[g



7ci fgY^{*}Cj Yfj]Yk

GHJZ7cbHJWh8YHJ]`g

7cbj Ybcfg

| BUa Y | 9a U]` | 5j U]`UV]`]lm | @cWUh]cb | D\cbY |
|-----------|-----------------------------|---------------|--------------------|-------|
| 9``Yb'@YY | \YYa]b"`YY4 i bgk "YXi "Ui | | A cfj Yb 6fck b | |

GWXcc``7cbHJWh'±bZcfa Uh]cb

GWcc~cZ9Xi Whcb

5 fhgž8 Yg][b'UbX'5 fWX]hYWhifY

; fci bX': `ccfž'A cfj Yb '6fck b '6i]`X]b['fl &\$Ł

H. $^{'}$ Ž * % $^{'}$ f&Ł $^{'}$ - $^{'}$,) $^{'}$ % ++

9. YXi WUhcb4 i bgk "YXi "Ui

K. `\hdg.#kkk"Ufhg"i bgk"YXi "Ui #YXi WUhjcb

5W_bck `YX[Ya YbhcZ7ci bhfm

I BGK '5frgž8Yg][b'UbX'5fW,]h'Wi fY'? Ybg]b[hcb'UbX'DUXX]b[hcb'Wa di gYg'UfY'Vi]'hcb'5Vcf][]bU`@UbXg"'K Y'dUmci f'fYgdYWrg'hc'h\Y'6]X'][U''UbX'; UX][U''dYcd'Yg'k\c'UfY'h\Y'7i ghcX]Ubg'cZh\YgY'`UbXg" K Y'UW_bck 'YX[Y'h\Y'5Vcf][]bU`'UbX'HcffYg'GHfU]h=g`UbXYf'dYcd'Ygž'h\Y':]fgh5i ghfU`]Ubgžk\cgY'`UbXgžk]bXg'UbX'k UhYfg'k Y'U``'bck 'g\UfYž'UbX'dUmfYgdYWhc'h\Y]f'i b]ei Y'j U'i Ygž'UbX'h\Y]f'Wcbh]bi]b['UbX'YbXi f]b['W'h fYg'k\]W\XYYdYb'UbX'Ybf]W\h\Y'`]ZY'cZci f'bUh]cb'UbX'Wca a i b]h]Yg"''

 $\label{eq:continuous} \begin{array}{ll} \text{$\stackrel{\cdot\cdot}{\to}$ U[Y'WciftYgmicZh\Y'CZh\Y'Dfc'J]WY!7\lubWY``cf'$$$ bX][Ybcig']$$ Ybcig'ghfUhY[m] $$ $$ U[Y'WciftYgmicZh\Y'CZh\Y'Dfc'J]WY!7$$ $$ U[Y'WciftYgmicZh\Y'CZh\Y'Dfc'J]WY!7$$ $$ U[Y'WciftYgmicZh\Y'CZh\Y'Dfc'J]WY!7$$ $$ U[Y'WciftYgmicZh\Y'CZh\Y'Dfc'J]WY!7$$ $$ U[Y'WciftYgmicZh\Y'CZh\Y'Dfc'J]WY!7$$ $$ U[Y'WciftYgmicZh\X'Ch'Zh\Y'Dfc'J]WY!7$$ $$ U[Y'WciftYgmicZh\X'Ch'Zh\Y'Dfc'J]WY!7$$ $$ U[Y'WciftYgmicZh\X'Ch'Zh\X$

7ci fgY 8YHJ]`g lb]hg`cZ7fYX]h*

K cf_`cUX

5ggYgga Ybh

| 5ggYgga Ybh'tUg_ | K Y][\h | 8iY'8UHY | 7 ci fgY @YUfb]b[Ci hWca Yg 5ggYggYX |
|---------------------------|----------|---|--|
| %":5bbcfUfYX:V]V`]c[fUd\m |) \$1 | DUffi% '&%\$* #&\$&&') .\$\$DA / DUffi& '% #\$+#&\$&&') .\$\$DA | %ž`& |
| &""A chj Uhjcb fydcfh |) \$1 | %&#\$, #&\$&&`\$).\$\$`DA</td><td>%ž`&ž`'</td></tr></tbody></table> | |

5ggYgga Ybh'% '5bbcHJhYX'V]V`]c[fUd\m

8i Y'XUhY. DUfh'% '&%#\$*#&\$&&').\$\$DA /DUfh'&.'% #\$+#&\$&&').\$\$DA

HUg_% 5bbchJhYXV]V`]c[fUd\m

@Yb[h\.'&) \$\$'k cfXg

E i U`]hUh]j Y`UbX`ei Ubh]hUh]j Y`ZYYXVUW_`dfcj]XYX`cb`]bY`h\fci [\`Wci fgY`k YVg]hY`k]h\]b`%\$`XUmg`cZ gi Va]gg]cb"

5XX]h]cbU`XYhJ]`g

DfYgYbh'Ub'UbbchUhYX'V]V`]c[fUd\mcZgcifWfg'dfcj]XYX']bWiX]b['gcaY'cZmcif'Wkcg]b["'H\Y'difdcgY'cZh\Y'UbbchUhYX'V]V`]c[fUd\m]g'hc'UWeiU]bh'mci'k]h\YhYY'YaYbhUfmUgdYWfg'cZachjjUhjcb'UbX'h\Y'`]hYfUhifYUggcWjUhYX'k]h\'achjjUhjcb']b'YXiWUhjcbU``gYhfjb[g"

 $\label{thm:condition} $$HY'Ubbc'UhYX'V]V^{c}[fUd\m^{2}Wca\d^{Y}h'X']b''k\ c'gYdUfUhY''dUffgz''gc''h\Uh'ZYYXVUW_''Zfca''h\Y''Z[fghdUffhWUb\Y'd''mci'''Wca\d^{Y}h'Y'h\Y'gYWcbX'dUffh''$

GYY'AccX'Y'Zcf'Z ff\Yf'XYhU]`q'cb'\ck 'bc'Wcad'YhY'h\Y'UbbchUhYX'V]V`]c[fUd\m'

5ggYgga Ybh& A chij Uhcb fYdcfh

8i Y'XUhY.'% #\$, #&\$&&'\$).\$\$'DA

HUg_*&. A chij Uhich fydcfh

@Yb[h. &) \$\$ k cfXg

 $\label{eq:conditional} Eiu'] \mbox{h is in h in $h$$

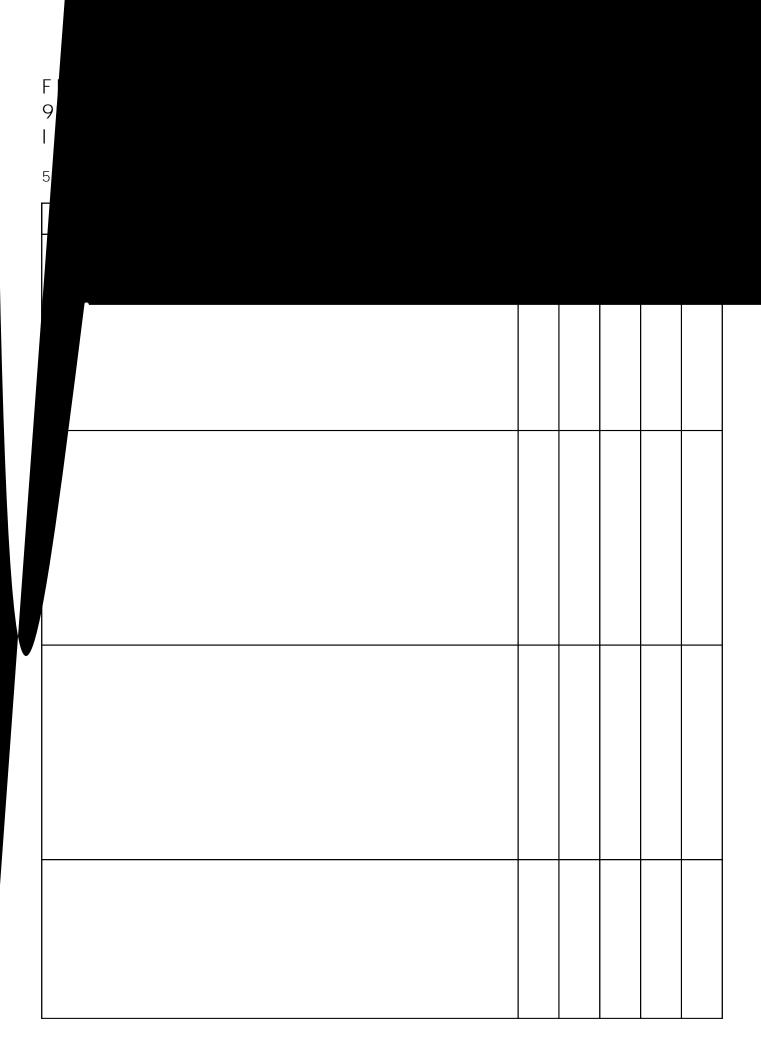
5XX]h]cbU`XYhU]`g

F Ydcfhirc 'U'gWkcc'ž'gYWrcfž'X]ghf]Wrž'[cjYfbaYbhiXYdUfhaYbhiz'cf'ch\Yf'cf[Ub]gUh]cb'VUgYX'cb'mcif'UbU'mg]gcZ]ng'dc']W]Ygž'ghfUhY[]Ygž'dfUWr]WYgž'cf'W ff]W'ia"'Mcif'gcifW']bZcfaUh]cb'Wci'X'VY'VUgYX'cb'U'gWkcc''gX]gW[d']bY'dc']Whiz']bhYfi]Ykg'k]h\'U'gYb]cf'ghUZZaYaVYf'Uh'U'gWkcc''cf'U'W ff]W'ia"cZZWYfzgWkcc'

 $\label{thm:limit} We a a i b] WUIJcbg\'zcf'ch\Yf'gWkcc``cZJWJU``cf'dc`] WmXcW a YbIg''`H\Y'fYdcfhig\ci``X'VY'k f] ImYb'Ug'I\kci [\'mciUfY'U'Wcbgi``HJbh'Zcf'h\Y'gWkcc`''$

GUa d`Y`gWYbUf]cg`UbX`XUHU`k]```VY`dfcj]XYX`]b`H\Y`WUgY`H\Uhmci f`k cf_d`UWY`cf`dfYj]ci g`k cf_d`UWYg'UfYbchgi]HUV`Y"

GYY'A ccX`Y'Zcf'Z ft\Yf'XYhU]`g'cb'\ck 'bc'Wca d`YhY't\Y'gW\cc``a chjj Uhjcb'fYdcfh'



| GdYWJZJW7 f]hYf]U | ¨flŁ— | | 2fŽŁ |
|--|-------|--|----------|
| DfYgYbhJhjcbicZifYgdcbgYiUWWcfX]b[ihciUddfcdf]UhYiUWUXYa]WUbXi]b[i]ghjWWcbjYbhjcbg | | | |
| • 5ddfcdf]UhY`fY[]ghYf`Zcf`UWUXYa]W#dfcZYgg]cbU``9b[`]g\ | | | |
| • FYZYfYbWYg'WJNYX'Uddfcdf]UNY`m | | | |
| | | | |
| ; YbYfU`Wca a Ybhg#fYWca a YbXUh]cbgʻZcfʻbYl hh]a Y.ʻ | | | |
| | | | |

 $FYWca\ a\ YbXYX. \qquad \hbox{$^*\#$} S\ fl\ @`DG\ 7F\ 8B\ 8k \qquad \qquad K\ Y][\ \ h]b[\ . \qquad)\ l

B6. H\Y'I]W_g`]b`I\Y'j Uf]ci g`Vcl Yg`UfY`XYg][bYX`Ic`dfcj]XY`ZYYXVUW_`Ic`ghi XYbhg/I\YmUfY`bchi[]j Yb Yei U``k Y][\hi]b`XYhYfa]b]b['I\X'fYVca a YbXYX`[fUXY"8YdYbX]b['Icb'I\X'bUhi fY`cZi\Y`UggYgga Ybh'HUg_ž `YWfi fYfg`a Um'U`gc`VcbIYl fi U`]gY`UbX#cf`Ua YbX`I\YgY`gdYWJZ]WWf]IYf]U": H\Y`fYVca a YbXYX`[fUXY`]g \hybHJhj Y`cb`mz`gi VYWfic`gHJbXUfX]gUI]cb`dfcWfggYg`UbX`Uddfcj U``VmI\Y`GW\cc``cZ9Xi WUI]cb`@YUfb]b[UbX`HYUW\]b['7 ca a]hYY"

Gi Va]gg]cb cZ5ggYgga YbhHUg_g

Hi fb]h]b Gi Va]gg]cb

Image: Ybwei bhyfu'dfcv'ya k \yb'uhhya dhjb['hc'gi va]hmci f'Ugg][ba Ybhh\fci [\ 'Hi fb]h]bž'd'YUgY

Hy'Yd\cby'9| hy'fbu''Gi ddcfhcb'-',) '' ' ' %cf'Ya U]''h\Ya 'cb'Y! hy'fbu'hy'hgi ddcfh4 i bgk "YXi "Ui "''Gi ddcfh
\ci fg'UfY', .\$\$Ua '-'%\$.\$\$da 'cb'k YY_XUmg'UbX'-.\$\$Ua '-').\$\$da 'cb'k YY_YbXg'fl *) 'XUmg'U'mYUft"'=Z'mci
UfY'i bUV'Y'hc'gi va]hmci f'Ugg][ba YbhXi Y'hc'U'ZJi 'hk]h\ 'Hi fb]h]b'mci 'a UmUdd'mZcf'Ub'Y! hy'bg]cbž'Vi hmci
a i ghfYhJ]b'mci f'h]W_Yhbi a VYf'Zfca '9! hy'fbU''Gi ddcfhfU'cb['k]h\ 'Ubmch\Yf'fy'Yj UbhXcW a Ybhgt'hc
]bWi XY'Ug'Yj]XYbW' 'hc'gi ddcfhmci f'Y! hy'bg]cb'Udd']WUh]cb"'=Zmci 'Ya U]''9! hy'fbU''Gi ddcfhmci 'k]'`
Ui hca Uh]WJ'`mfYW']j Y'U'h]W_Yhbi a VYfZ'Vi h]Zmci 'hY'Yd\cbY'mci 'k]``bYYX'hc'gdYW]Z]WJ'`mUg_'Zcf'cbY''
Hi fb]h]b'U'gc'dfcj]XYg'i dXUhy'g'cb'h\Y]f'gmghYa 'ghUh' g'cb'Hk]hyf''

; YbYfU`mž'UggYgga YbhiHug_g'a i ghVY'gi Va]hhYX'Y`YVWfcb]\WJ``mij]U'Y]h\Yf'Hi fb]h]b'cf'U'A ccX`Y Ugg][ba Ybh''=b']bgHJb\W'g'k \YfY'h\]g']g'bchdcgg]V`Yž']hk]```VY'gHJhYX'cb'mci f'\\circ i fgY'g'A ccX`Y'g]hY'k]h\U`hYfbUh]j Y'gi Va]gg]cb'XYHJ]`g"

cfi]bZcfa Uhjcbicbi\ckihcigi Va]hUgg][ba Ybhgicbi]bYij]UiA ccXiY.i\hdg.#gh XYbhi bgk "YXi "Ui #\ck! gi Va]hUgg][ba Ybha ccXiY

5 WUXYa]W<cbYghmUbX D`U[]Uf]ga

D`U[]Uf]ga i]gii g]b[ih\Yik cfXgicfi]XYUgicZch\YfgiUbXidfYgYbh]b[ih\Ya iUgimci fick b"i=hWbihU_Yia Ubm Zcfa qžZfca iXYi]VYfUhYiWXYUh]b[ihciUWW]XYbhU`mWcdm]b[iZfca iUiqci fWYk]h\ci hUW bck iYX[Ya Ybh'

IBGK [fcidgdu[]Uf]ga]bhch\YZc``ck]b[WUhY[cf]Yg.

7 cdm]b[. `I g]b['h\Y'gUa Y'cf'j Yfmg]a]`Uf'k cfXg'hc'h\Y'cf][]bU`'hYl hcf']XYU'k]h\ci hUW_bck `YX[]b['h\Y gci fW'cf'i g]b['ei chUh]cb'a Uf_g"'H\]g']bWi XYg'Wcdm]b['a UhYf]U`gž']XYUg'cf'WcbW'dhg'Zfca 'U'Vcc_ž'Ufh]WYž fYdcfhcf'ch\Yf'k f]hhYb XcW a Ybhz'dfYgYbhUh]cbž'Wca dcg]h]cbž'Uffk cf_ž'XYg][bž'XfUk]b[ž'WfW]hfmž'Wca di hYf dfc[fUa 'cf'gcZk UfYž'k YVg]hYž']bhYfbYhz'ch\Yf'Y`YWfcb]WfYgci fW'z'cf'Ubch\Yf'dYfgcbfg'Ugg][ba Ybhk]h\ci h Uddfcdf]UhY'UW_bck `YX[Ya Ybh''

Duddfcdf]UhY dufud\fug]b[...7\ub[]b[...12\k...k.cfXg.UbX.d\fugYg.k.\]Y a cghmfYhJ]b]b[...h\Y.cf][]bU`]bZcfa Uh]cbžghfi Wh fY UbX#cfdfc[fYgg]cb.cZ]XYUg.cZh\Y.cf][]bU`k]h\ci hUW_bck `YX[Ya Ybh'.H\]g.U`gc Udd`]Yg.]b`dfYgYbhUh]cbg`k \YfY gca YcbY dufUd\fugYg.Ubch\Yf'g.]XYUg.cf`k cfXg`k]h\ci h`WfYX]h`UbX`hc d]YW]b[...hc[Yh\Yf'ei chYg.UbX.dUfUd\fugYg.]bhc.U`bYk `k\c`Yžk]h\ci h`Uddfcdf]UhY`fYZYfYbW]b[...hc]

7c``i g]cb. K cf_]b[k]h ch\Yfg'Vi hdUgg]b[cZh\Yk cf_'Ug'U'dYfgcb'g']bX]j]Xi U``k cf_"'7c``i g]cb'U`gc]bWi XYg'dfcj]X]b['mci f'k cf_'hc'Ubch\Yf'ghi XYbhZcf'h\Y'di fdcgY'cZh\Ya 'd`U[]Uf]g]b[ždUm]b['Ubch\Yf'dYfgcb'hc'dYfZcfa 'Ub'UWUXYa]Whuq_ž'ghYU`]b['cf'UWei]f]b['Ubch\Yf'dYfgcb'g'UWUXYa]Wk cf_'UbX'Wcdm]b[

5 WUXYa]W + DZcfa Uh]cb

8 i Y 'hc 'Yj c'j]b['UXj]\W 'VmBGK '< YU't\ ž'ghi XYbhg'a i gh'\W.Y\<u>V</u>'Zcf'i dXUh\YX']bZcfa Uh]cb 'fY[UfX]b['cb`]bY 'YUfb]b['Zcf'U``'5fhgž'8Yg][b 'UbX'5f\W.]h\Y\ni fY '\wci fgYg't\]g't\Yfa 'f]]U'A ccX`Y'cf'\wci fgY']bZcfa Uh]cb dfcj]\XYX"Ł

: cf`YggYbhJU``gh XYbh`]bZcfa UhJcb`fY`UhJb['hc.

- fYei YghgʻZcfʻYl hYbg]cb/
- `UhY gi Va]gg]cbg [i]XY`]bYg/
- fYj]Yk cZa Uf_g/
- I BGK '< YU`h\ 'UbX'GUZYhm'dc`]W]Yg/
- YI Ua]bUh]cb dfcWYXi fYg/

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