

ARTS2384

Dc`]hJWU`D\]`cgcd\m

HYfa 'C bY''##'&\$%

7ci fgY⁻8YHJ]`g

7 fYX]h'Dc]bhg '* '

Gi a a UfmcZ'h\Y'7ci fgY

Gi VYWn5fYU. BZ[aeabZk

 $\label{thm:condition} $$H\Y'WcifgY'dfcj_XYg'mci'k_h'h'U'gc'XZcibXUhcb']b'dc'hWU'd\]`cgcd\mVmaYUbg'cZWcgY'fYUX]b[g'cZWbhU'hYlhg'Vmh\]b_Yfg'gi WX'Ug'H\caUg'<cVVYgž'>c\b'@cW_Y'UbX'<UbbU\'5fYbXh'Dc'h\W'd\]`cgcd\m$

5ggYgga Ybh

5ggYgga YbhFi Vf]W#9ggUmGrUbXUfXg

	< 8	8B	7 F	DG
	Wc∖YfYbha UbbYf'U WYUf'UbX'dfcZci bX Wca dfY∖Ybg]cb'cZ h\Y']ggi Yg"	Wc∖YfYbha UbbYf'U WYUf Wca dfY\Ybg]cb'cZ h\Y']ggi Yg"	Wc\YfYbha UbbYf`U Wca dfY\Ybg]cb`cZ h\Y`]ggi Yg"	-00 0
5bU`mg]g	h\Y`d\]`cgcd\]\WU` UbU`mg]g`cZhYI hgž cZZYf]b[`]bbcj Uhjj Y UbX`]bg][\hi]`	h\Y`d\]`cgcd\]\W\` UbU`mg]g`cZhYI hgž	0 0	91 \]V]hgʻgca Y fYZYWh]cbʻcbʻh\Y]ggi YgʻWtj YfYX"
	XYHJ]YX UMYbHcb Ic UbX gi WWggZ YI YW Hcb cZU k]XY fUb[Y cZ Wbj YbHcbg dUfHW Uffic hY UWUXYa]WYggUm]b d\]cgcd\nž]bWi X]b[cf[Ub]gUHcbž MbHybHz dfYgYbHUHcbž]a dcffUbh Wcbj Ybh]cbg dUfh]W`Uf'hc'h\Y UWUXYa]WYggUm]b d\]`cgcd\mž	Uddfcdf]UHY hc d\]`cgcd\mUbX'h\Y UWUXYa]WYggUm	5 HHY a dhg hc i gY U Webg]ghY bhigmghY a Zef VUg]W ef[Ub]gUh]cb UbX dfYgY bhUh]cb"
- 0	8YacbglfUhYg Wf]h]WU``mfYZYWf]jY igY'cZfY`YjUbh gcifWYg'hc	8Ya cbglfUliYg fYZYWij Y'i gY'cZ fY'Yj Ubhigci fWYg hc'gi ddcfh dcg]hjcb"		

K f]h]b['Ub'UWUXYa]WYggUma YUbg'_YYd]b[']b'a]bX'gYj YfU`'HUg_g.

UŁ UWW fUHY mWcbj Ymjb['th\Y'a YUb]b['cZh\Y'df]a UfmthYl tifk \Uti]g'th\Y'thYl ti U`'Yj]XYbWY Zcf'mci f]bHYfdfYtUHcb3Ł/

VŁfYZYWIJD['cb'h\Y'dcgg]V`Y'k YU_bYggYg'UbX']a d`]WUlfJcbg'cZh\Y'Ui h\cf'g'dcg]lfJcbg'fk \Ulrighf]_Yg'mci 'Ug WcbhYbhJci g']b'h\Y'fYUX]b['UbX#cf'k \UlriZc``ck g'Zfca ']h3Ł/

WE'g]hi Uh]b['mci f']bhYfdfYhUh]cb']b'fY`Uh]cb'hc'Yl]gh]b['Wca a YbhUf]Yg'fXcYg'mci f'hU_Y'cb'h\Y'hYl h'X]ZYf'Zfca k\Uh'ch\Yfg'\Uj Y'a UXY'cZ]h'UbX'WUb'mci 'dfcj]XY'fYUgcbg'Zcf'mci f'ck b'k Um'cZfYUX]b['h\Y'hYl h'8Ł"

K]h\ci hfU\ti='Ub'U\W\fuhr'YI dcg]h]cb'cZh\Y'df]a UfmhYI h—'mci 'a U_Y']h\UfXYf'Zcf'mci f'fYUXYf'hc'gYY\tiZcf]bghUb\W'\ti'\Uhmci f'\\fu]h]\\U'\Tya Uf_g'ghf]_Y'\ca Y'fUbX'Xc'bch'\figh`UbX'U'"_]``Yf'V`ck "'cb'U'\ti][a YbhcZmci f]a U[]bUhcbt"

K]h\ci hfV\z='h\Y'YI dfYgg]cb'cZmci f'ck b'fYZYWf)cbg'cb'h\Y'df]a UfmhYI h='mci 'a U_Y']h\UfXYf'Zcf'mci f fYUXYf'hc'gYY'h\Uh'gca Yh\]b[']g'VY]b['qU]X'h\Uh'\Ug'bch'VYYb'qU]X'VYZcfY"

K]h\ci hftWe—Yb[U[Ya Ybhk]h\ gYWbXUfm`]h\fUh fY`—mci 'a U_Y`]h\UfXYf`Zcfmci f`fYUXYf`hc`gYY`\ck 'mci f]bh\fdfYhUhcb`Wbhf]Vi h\g`hc`Wbh\a dcfUfmUWUXYa]Wi bXYfghUbX]b['cZh\Y`]ggi Yg`UhghU_Yž'bY]h\Yf fYd`]WUh]b['k\Uhch\Yfg`\Uj Y`U`fYUXmgU]X`bcf`ZJ``]b['Zci ``cZh\Y]f`Uf[i a Ybhg"

B6"? YYd]b[`fUłzffVŁ'UbX'ffWt]b'a]bX`]g'YI ffYa Y`mX]ZJW `hUbX'bYj Yf'VYWca Yg'glfU][\hZcfk UfX"'Hc'lfmž \ck Yj Yfz']g'hc'gYhci h]b'h\Y'f][\hX]fYWqcb"

5g'U'fi `Y'cZh\i a VžfYZYff]b['hc'Wca a YbhUhcfg'k \Yb'h\YmWf]h]W]gY'cf'Y`UVcfUhY'cb'h\Y'df]a UfmihYI hi]g VYhhYf'h\Ub'fYZYff]b['hc'h\Ya 'k \Yb'h\Ymg]a d`mdUfUd\fUgY']hcf'fYdYUhk]XY`m_bck b'ZUWg'WcbWYfb]b[']hg Wca dcg]h]cb'cf']bZi YbW'''=hi]g'Yj Yb'VYhhYf'k \Yb'mci 'WUb'di h'Zcfk UfX'Ub'Uf[i a YbhcZmci f'ck b']b fYgdcbgY'hc'U'Wca a YbhUhcf'g'Wf]h]W]ga 'cf'Y`UVcfUh]cb'cZh\Y'df]a UfmihYI h'

5ggYgga Ybh'HUg_g'

5ggYgga Ybh'tUg_	K Y][\h	8iY'8UHY	Gh XYbh@YUfb]b[Ci hWca Yg 5ggYggYX
F YgYUfWX 'YggUm'%) \$\$'k cfXg'	')	&&#\$' #&\$% `\$(.\$\$`DA</td><td>%Ž Ž(Ž)</td></tr><tr><td>F YgYUfW '9ggUm&\$\$\$'k cfXg'</td><td>) \$1</td><td>\$' #\$) #&\$% `\$(.\$\$`DA</td><td>%ž&ž ž(ž)</td></tr><tr><td>A ccX`Y`Dcghg`</td><td>%) ।</td><td>\$'#\$)#&\$%-`\$(.\$\$`DA</td><td>%ž&ž ž(</td></tr></tbody></table>	

5ggYgga Ybh'8YhJ]`g

5qqYqqa Ybh% F YqYUfW YqqUm% \$\$ k cfXq

GhUfhXUhY. Bch5dd`]WUV`Y

@Yb[h\. '%) \$\$ k cfXg

8YHJ]`g. `Gh XYbhg`k f]hY`U`fYgYUfW\`YggUm!`%) \$\$`k cfXg": YYXVUW_`k]```HU_Y`h\Y`Zcfa `cZU`fi Vf]WUbX |bX]i [Xi U``Wca a Ybhg"

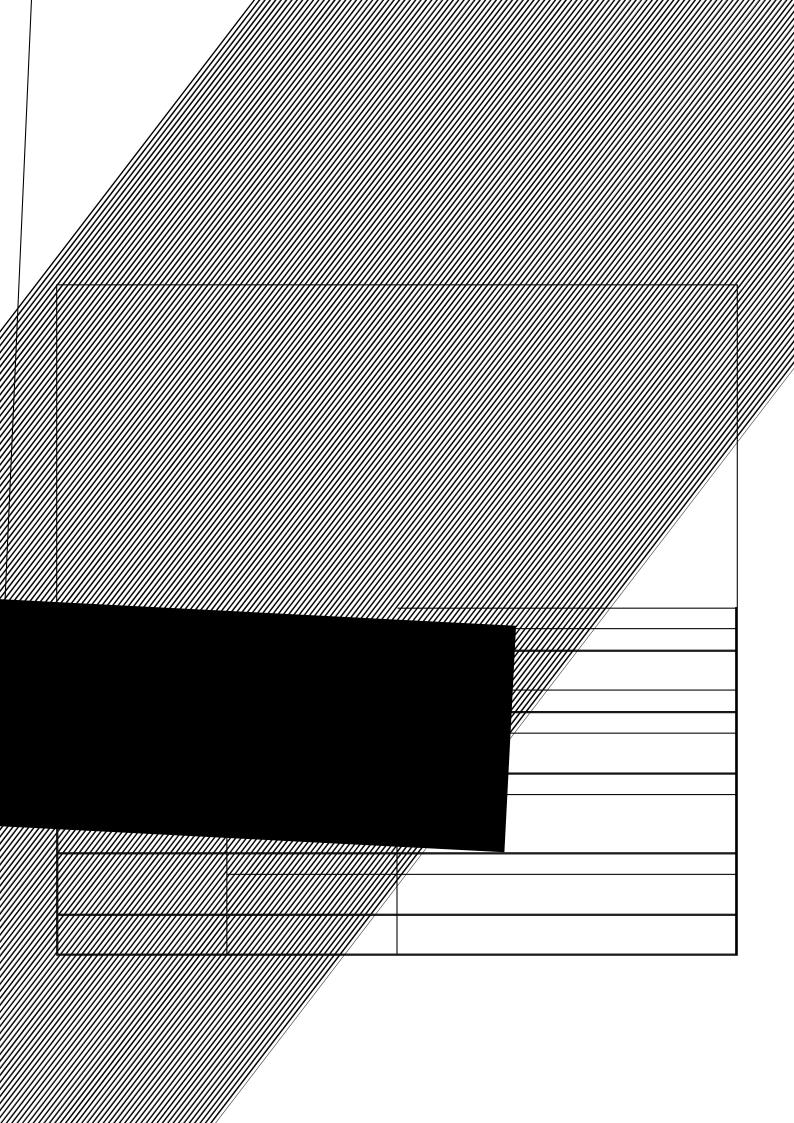
5XX]h]cbU`XYhJ]`g.

9ggUmhcd]Wq'k]``VY'dcghYX'cb'AccX`Y'Uhh\Y'ghUfhcZhYfa"

5ggYgga Ybh& FYgYUfW 9ggUm&\$\$\$ k cfXg

GHJfhXUhY. Bch5dd`]WJV`Y

8YHJ]`g.



FYgci fWyg

DfYgWf]VYX F Ygci fWYg

FYWca a YbXYX FYgci fW/g

5 ``]ghcZfYWca a YbXYX gYWcbXUfmfYUX]b[g'k]``VY 'Uj U]`UV Y 'cb'A ccX`Y 'UbX'j]U'@Y[Ubhc"

7 ci fgY 9j U'i Uhjcb UbX 8 Yj Y'cda Ybh

Gh XYbhg`\Uj Y`h\Y`cddcfh b]hmhc`dfcj]XY`ZYYXVUW_`cb`h\Y`Wci fgY`Vch\`Zcfa U``m!`j]U`h\Y`YbX!cZhYfa A m9! dYf]YbW'`qi fj Ym!`UbX`]bZcfa U``m!`j]U`Y!a U]``cf`ZUW!!c!ZUW!"

H\]g`mYUf`=\Uj`Y`fYXi WYX`h\Y`bi a VYf`cZYggUmg`Zfca `h\fYY`hc`lk c"``H\Y`gYWcbX`YggUm`]g`bck `U Wca dUfUh]j Y`YggUmcb`@cW_Y`UbX`5fYbXh'``=g`h\]g`dfYZYfUV`Y`hc`k f]h]b[`'U`gYdUfUhY`YggUmcb`YUW\`cZh\YgY h\]b_Yfg3

=\UjY'U`gc`W\Ub[YX'h\Y`k Um=k]```fYgdcbX'hc'A ccX`Y`dcghg"``=bghYUX'cZfYd`m]b[`hc'YUW\`cbYž'=k]```k f]hY'U
`cb[Yf`fYgdcbgY'hc'h\Y`dcghg`cZh\Y`k YY_žfYZYff]b[`hc']bX]j]Xi U``Wcbhf]Vi h]cbg'h\YfY]b"``

Gi Va]gg]cb cZ5ggYgga YbhHUg_g

Gi Va]gg]cb cZ5ggYgga YbhHUg_g

Hi fb]h]b Gi Va]gg]cb

_Zmci YbWci bhYf'U'dfcV`Ya 'k \Yb'UhYa dhJb['hc'gi Va]hmci f'Ugg][ba Ybhh\fci [\ 'Hi fb]hJbž'd`YUgY
hY`Yd\cbY'9| hYfbU``Gi ddcfhcb'-',) '' ' ' %cf'Ya U]`'h\Ya 'cb'Y! hYfbU`hY`hgi ddcfh4 i bgk "YXi "Ui '"'Gi ddcfh
\ci fg'UfY', .\$\$Ua '-'%\$.\$\$da 'cb'k YY_XUmg'UbX'-.\$\$Ua '-') .\$\$da 'cb'k YY_YbXg'fl *) 'XUmg'U'mYUft'' =Zmci
UfY'i bUV`Y'hc'gi Va]hmci f'Ugg][ba YbhXi Y'hc'U'ZUi 'hk]h\'Hi fb]hJb'mci 'a Um'Udd'mZcf'Ub'Y! hYbg]cbžVi hmci
a i ghfYhU]b'mci f'hJW_Yhbi a VYf'Zfca '9! hYfbU``Gi ddcfhfU'cb['k]h\'Ubmch\Yf'fY`Yj UbhXcW a Ybhgt'hc
]bWi XY'Ug'Yj]XYbW'hc'gi ddcfhmci f'Y! hYbg]cb'Udd`]WUhJcb'' =Zmci 'Ya U]`'9! hYfbU``Gi ddcfhmci 'k]``

5 WUXYa | W < cbYghmUbX D`U[| Uf]ga

D`U[]Uf]ga i]gii g]b[ih\Yik cfXgicfi]XYUgicZch\YfgiUbXidfYgYbh]b[ih\Ya iUgimci fick b"i±iWUbihU_Yia Ubm Zcfa qžZfca iXYi]VYfUhYiW\YUh|b[ihciUVW]XYbhU`mWcdm]b[iZfca iUiqci fWYik]h\ci hiUW_bck iYX[Ya Ybh'i

IBGK '[fci dg'd'U[]Uf]ga ']bhc'h\Y'Zc``ck]b['WUhY[cf]Yg.

7 cdm]b[.'i g]b['h\Y'gUa Y'cf'j Yfmg]a]`Uf'k cfXg'hc'h\Y'cf][]bU`hYl h'cf']XYU'k]h\ci h'UW_bck `YX[]b['h\Y gci fW'cf'i g]b['ei chUh]cb'a Uf_g"'H\]g'U`gc'Udd`]Yg'hc']a U[Ygž'Ufh'UbX'XYg][b'dfcYWhgž'Ug'k Y``'Ug dfYgYbhUh]cbg'k \YfY'gca YcbY'dfYgYbhg'Ubch\Yf'g']XYUg'cf'k cfXg'k]h\ci h'WfYX]h'

⇒ Uddfcdf]UhY 'dUfUd\fUg]b[...7\Ub[]b['U'ZYk 'k cfXg'UbX'd\fUgYg'k \]'Y 'a cghmfYhJ]b]b['h\Y'cf][]bU` ghfi Wh fY 'UbX#cf'dfc[fYgg]cb'cZ]XYUg'cZh\Y'cf][]bU'žUbX']bZcfa Uh]cb'k]h\ci hUW_bck `YX[Ya Ybh'H\]g'U`gc Udd`]Yg']b'dfYgYbhUh]cbg'k \YfY'gca YcbY'dUfUd\fUgYg'Ubch\Yf'g']XYUg'cf'k cfXg'k]h\ci hWfYX]hUbX'hc d]YW]b['hc[Yh\Yf'ei chYg'UbX'dUfUd\fUgYg']bhc'U'bYk 'k \c`Yžk]h\ci hUddfcdf]UhY'fYZYfYbW]b["

7 c``i g]cb. 'k cf_]b['k]th 'cth Yfg'Vi hidUgg]b['cZZth Y 'k cf_'Ug'U'dYfgcb'g']bX]j]Xi U``k cf_"'7 c``i g]cb'U`gc]bWi XYg'dfcj]X]b['mci f'k cf_'thc'Ubcth Yf'ghi XYbh'VYZcfY'th Y'Xi Y'XUHYZcf'Zcf'th Y'di fdcgY'cZth Ya

- i bXYfgfUbX mci f'f][\hg'UbX'fYgdcbg]V]`]hJYg'Ug'U'gh XYbhUhl BGK
- VY`Uk UfY`cZd`U[]Uf]ga ž`Wcdmf][\hz'l BGK `Gh XYbh7cXY`cZ7cbXi WhUbX`5VWWdhUV`Y`l gY`cZ I BGK `=\forall H`F Ygci f\W\g`Dc`]\m\m
- VY 'Uk UfY 'cZh\Y 'ghUbXUfXg 'cZVY\Uj]ci f'Yl dYWYX 'cZYj YfmcbY ']b 'h\Y 'l BGK 'Wca a i b]hm
- `cWUHY 'gYfj]WYg'UbX ']bZcfa UH]cb'UVci hI BGK 'UbX'I BGK '@]VfUfm

Gca Y'cZh\YgY'UfYUg'k]``VY'ZJa]`]Uf'hc'mci ž'ch\Yfg'k]``VY'bYk"'; U]b]b['U'gc`]X'i bXYfgHJbX]b['cZU``h\YfY`UhYX'UgdYWng'cZ9@+69'k]``\Y`d'mci 'a U_Y'h\Y'a cghicZmci f'ghi X]Yg'UhI BGK "'\\hd.##qi VYWfi |XYg"`]VfUfm'i bqk "YXi "Ui #\`]qY#JVci hY`]qY

5 WUXYa]W±bZcfa Uhjcb

: cf'YggYbhJU`gh XYbh]bZcfa UhJcb'fY`UhJb['hc.