

# **IEST5003**

5XXfYgg]b[ '9bj ]fcba YbHJ``=ggi Yg

HYfa 'H\fYY''##'&\$%-

# 7ci fgY 8YHJ] g

## 7 fYX]hDc]bhg\*\*

## Gi a a UfmcZh\Y'7ci fgY

H\]g`Wci fgY`]`i glfUlh'g`h\Y`bUhi fY`cZz`UbX`bYYX`Zcfz`a i `h]!`cf`lfUbg!X]g\]d`]bUfmUddfcU\W\Yg`Zcf`UXXfYgg]b[Ybj ]fcba YbfU``dfcV`Ya g`cZbUh]cbU``UbX#cf`[`cVU``]a dcffUb\W`"`Ghi XYbhg'`]bXYdYbXYbhifYgYUf\W.z`Z]Y`X ghi Xmz`UbX`h\Y`\wca d`Yh]cb`cZUb`]bX]j ]Xi U``fYgYUf\W.`dfc^Y\mik ]```XfUk `cb`\W ffYbhcf`fY\Wbh\_Ym Ybj ]fcba YbfU``]ggi Yg`UbX`k ]```VY`gi ddcfhYX`Vm`Y\Wi fYgz`gYa ]bUfgz`UbX`cb!`]bY`hi ]hJcb`UbX`fYgci f\Wg"`H\Y \_Ymh\Ya Y`cZh\Y`\wci fgY`]g`h\Y`bYYX`hc`UXcdh`]bhY[fUhj] Y`UbX`a i `h]!X]g\Jd`]bUfmUddfcU\W\Yg`hc Ybj ]fcba YbfU``a UbU[Ya Ybh'`Gca Y`cZh\Y`hcd]\\g`mci k ]```\wcj Yf`UfY. `Ybj ]fcba YbfU``[cj YfbUb\W`z`]bhYfbUh]cbU``Ybj ]fcba YbfU``fY[]a Yg#\\cbj YbhJcbg/ZfUa ]b[`UbX`XYZ]b]b[`Ybj ]fcba YbfU``]ggi Yg/di V`]\W dUfhJ\JdUh]cb``UbX`gfU\_Y\c`XYf`Yb[U[Ya Ybh']b`XY\Jg]cb`a U\_]b[\]b[\]bhY[fUhYX`UbX`Zcfk UfX``cc\_]b[`UbU`mg]g/d`Ubb]b[`Zcf`gi ghU]bUV`Y`XYj Y`cda Ybh'`g\J\Yb\Wzf]g\_`UbX`\_bck `YX[Y/\car d`Yl `gmghYa g`UbX`UXUdh]j Ya UbU[Ya Ybh'\gi ghU]bUV`Y`bUhi fU``fYgci f\W`a UbU[Ya Ybh'Ybj ]fcba YbhU``]a dU\Wg`cZdfcXi \Mjcb`UbX \Wcbgi a dh]cb"

## 7ci fgY @YUfb]b[ 'Ci hWca Yg

- %" 8Ya cbglfUlY`Ub`UXj UbWX`i bXYfglUbX]b[ `cZh\Y`a i `h]!X]gW]d`]bUfmVcXmcZ\_bck `YX[ Y`bYYXYX`Zcf Ybj ]fcba YblU``a UbU[ Ya Ybh'UbX`Udd`mX]gW]d`]bUfmUbX`lfUbg!X]gW]d`]bUfmdf]bW]d`Yg`UbX`dfUWf]VW'g hc`bYk `cf`Wca d`YI `W\U``Yb[ Yq"
- &" 8 Yj Y`cd`UbU`mtj\WJ``g\_]``gž`UXj Ub\\YX`\Vf]hj\WJ``t\]b\_]b[ `UbX`dfcV`Ya `gc`j ]b[ `g\_]``gž`UbX`i bXYfgtUbX]b[ cZYbei ]fm\VUqYX``YUfb]b[ `]b`t\Y`fYU`a `cZYbj ]fcba YbtU``a UbU[ Ya Ybt'
- ' " 9I \]V]hWUdUV]`]lmrZcf`]bXYdYbXYbhUbX`Wc``UVcfUhjj Y`Ybei ]fmž'UbX`Zcf`hYUa k cf\_"
- ("8YacbghfuhYYZZYWfjYjYfVu`UbX#cfkf]hhYbWcaaib]Wuhlcbj]UUUfUb[YcZhYWkb]eiYg"
- ) " 8 Yj Y`cd`Uk UfYbYgg`cZ`cWJ`ž'bUf]cbU``UbX`]bfYfbUf]cbU``]ggi Yg`fY`Yj UbfiZcf`Ybj ]fcba YbfU` a UbU[ Ya Ybf'

# HYUWX]b[ 'GhfUhY[]Yg'

H\]g`Wci fgY`]g`HJ\_Yb`hck UfX`h\Y`YbX`cZU'ghi XYbhg`dUh\k Umih\fci [\`h\Y`A UghYf`cZ9bj]fcba YbhU`A UbU[Ya Ybh''-\b\Y`A 9A ž]bXYdYbXYbhfYgYUfW\`UbX`ghi XYbh\WfbhYfYX``YUfb]b[`'UddfcUW\Yg`UfY dUfUa ci bh''7 ca d`Ya Ybh]b[`]b!WUgg`X]gW gg]cbg`UbX`gYa ]bUfgžih\]g`Wci fgY`i gYg`h\Y`A ccX`Y`d`UhZcfa 'hc XY`]j Yf`cb!`]bY`fYgci fWYg`UbX`Ug`U'g]hY`Zcf`h\Y`YI W\Ub[Y`cZghi XYbhfYgYUfW\"'K YY\_`mV`c[gž`Ub YI dYf]Ybh]U``Z]Y`X`ghi Xmž`U`W ffYbhWUgY`ghi XmcZUb`Ybj ]fcba YbhU``Wcbhfcj Yfgmž`UbX`Ub`UXj Ub\WX`fYgYUfW\ dUdYf`a U\_Y`i d`U'gYhcZ]bhYf!`]b\_YX`Ugg][ ba Ybhg''`H\Y`Wci fgY`i gYg`U'gmghYa ]Wt]bhYfX]gW]d`]bUfmUddfcUW\ h\Uh\Wb'UXYei UhY`mUVWci bhZcf`h\Y`Wa d`YI ]mmcZYbj ]fcba YbhU``]ggi Yg`UbX`gi ddcfhih\Y`XYj Y`cda YbhcZ YZYWf]j Y`dfcdcgU`g`Zcf`UWf]cb"

5ggYgga Ybh

; fUXYg

**8 YHJ]`g.** 'K YY\_`mg\cfhk f]hhYb`gi a a Uf]Yg`Zcf`X]ghUbWY`UbX`cb!WUa di g`ghi XYbhgž'k ]h\`g\cfhicb`]bY ZYYXVUW\_[] jj Ybž'Zcf`%\$`k YY\_g`r' \$\$`k cfXg`dYf`k YY\_

5XX]h]cbU`XYhU]`g.

 $Hcd]Wg'Zcf'mcif'V`c[g'k]```VY'YgHUV`]g\YX'YUWX'kYY_ž'UbX'k]``fY`UHY'hc'mcif']bXYdYbXYbhfYgYUfWX''$ 

Hi fb]hb gYhb[. H\]g ]g bchU Hi fb]hb Ugg][ ba Ybh

5ggYgga Ybh&; fci d 7 UgY Gh Xm

GhUfh XUhY.

@Yb[h\.G\cfhdfYgYbhUh]cb

8YHJ]`g. "\$ a ]bg WUgg dfYgYbHJhcb cf Zcf X]gHJbW cbY k YY\_ "YUX]b[ "Ub cb`]bY Zcfi a "

5XX]h]cbU`XYhU]`g.

 $\label{eq:continuous} D`YUgY`gYY`mcif`A ccX`Y`g]hY`Zcf`XYhU]`YX`[i]XUbWY"`H\Y`[fcid`k cf_k]``VY`VUgYX`cb`mcif`cf][]bU`fYgYUfW\"$ 

Hi fb]hjb gYhjb[. H\]g ]g bchU Hi fb]hjb Ugg][ ba Ybh

5ggYgga Ybh' .: ]Y`X 5gg][ ba Ybh

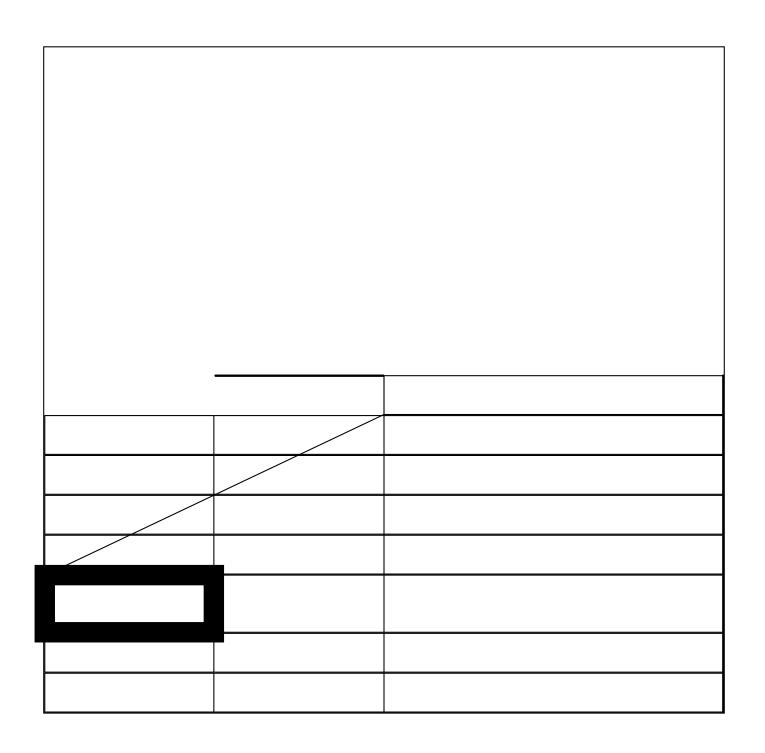
GHJfhXUhY.

@Yb[h\."\$\$\$ k cfXg" A Umj UfmXYdYbX]b[ cb Zcfa Uh

8YHJ]`g. `Gh XYbhg`k]```VY`fYei]fYX`hc`gi Va]hU`' ž\$\$\$`k cfX`fYdcfhVUgYX`cb`U`ZJY`X`Ugg][bYa Ybh

5XX]hcbU`XYHJ]q.

5 a UʻcfifYZYW]ji YiYggUmfl \$\$\$ k cfXgŁžVUgYXiUfci bXi]bXYdXYbhfYgYUfWkiii



# FYgci fWyg

#### DfYgWf]VYX F Ygci fWYg

±JZcfa Uh]cb'UVci hfYgci fWyg'k]``VY'j]U'h\Y'Wci fgY'A ccX`Y'g]hY"'FYUX]b[g'k]``VY'`]ghYX'UbX'a UXYUjU]`UV`Y'h\fci [\'h\Y'@9; 5BHC'gmghYa"

#### FYWca a YbXYX FYgci fW/g

±JZcfa Uhjcb 'UVci hfYgci fWyg'k ]``'VY'j ]U'h\Y'Wci fgY'A ccX`Y'g]hY"'F YUX]b[g'k]``'VY'`]ghYX'UbX'a UXY Uj Uj`UV'Y'h\fci [\'h\Y'@9; 5BHC 'gmghYa "''Nci 'k]``'U`gc'VY'YI dYWhYX'hc'WcbXi WhjbXYdYbXYbhfYgYUfW\ h\Uh`YUXg'mci 'hc'ch\Yf'gdYW]U`]gYX'gci fWyg"

### 7 ci fgY 9j U'i Uh]cb UbX 8 Yj Y'cda Ybh

A m91 dYf]YbWFk ]``VYTi gYXTUhth\YTYbXTcZgYgg]cbTbTYj U`i UhYTh\YTWci fgY": cW gT[ fci dgTk ]```dfcj ]XYUXX]h]cbU``ZYYXVUW\_Tbck UfXgTh\YTa ]XXTYTcZh\YTWci fgY"

6UgYX`cb`dUghghi XYbhYl dYf]YbW'`UbX`fYgi `h]b[`'Wci fgY`XYj Y`cda Ybhzh\Y`ZcW g`k]```VY`cb`UddfcUW\Ygh\UhZghYf`]bXYdYbXYbhfYgYUfW\`UbX`k f]h]b[`'h\Uh]g`cZU`gW\c`Uf`m\][\`ghUbXUfX/UbX`ci hdi hg`h\Uh'UfY`cZ

Gi Va |gg|cb cZ5ggYgga YbhHUg\_g

Gi Va ]gg]cb cZ5ggYgga YbhHUg\_g

Hi fb]h]b Gi Va ]gg]cb

#mci YbWci bhYf'U'dfcV'Ya 'k \Yb'UthYa dr]b['rc'gi Va ]hmci f'Ugg][ ba Ybht\fci [\'Hi fb]r]bž'd'YUgY
hY'Yd\cbY'9I hYfbU'Gi ddcfhcb'-', ) '''' %cf'Ya U]''h\Ya 'cb'YI hYfbU'hY'hgi ddcfh4 i bgk "YXi "Ui '"'Gi ddcfh
\ci fg'UfY', .\$\$Ua '-'%\$.\$\$da 'cb'k YY\_XUmg'UbX'-.\$\$Ua '-').\$\$da 'cb'k YY\_YbXg'fl \*) 'XUmg'U'mYUft'''#mci
UfY'i bUV'Y'hc'gi Va ]hmci f'Ugg][ ba YbhXi Y'hc'U'ZJi 'hk ]h\'Hi fb]h]b'mci 'a Um'Udd'mZcf'Ub'YI hYbg]cbž'Vi hmci
a i ghfYhJ]b'mci f'h]W\_Yhbi a VYf'Zfca '9I hYfbU''Gi ddcfhfU'cb['k]h\'Ubmch\Yf'fY'Yj UbhXcW'a Ybhgt'hc
]bWi XY'Ug'Yj ]XYbWY'hc'gi ddcfhmci f'YI hYbg]cb'Udd']WUh]cb'''#mci 'Ya U]''9I hYfbU''Gi ddcfhmci 'k]''
Ui hca Uh]WJ''mfYWY']j Y'U'h]W\_Yhbi a VYfž'Vi h]Zmci 'hY'Yd\cbY'mci 'k]'''bYYX'hc'gdYW]ZWJ''mUg\_'Zcf'cbY''
Hi fb]h]b'U'gc'dfcj ]XYg'i dXUhYg'cb'h\Y]f'gmghYa 'gfUh' g'cb'Hk]hYf"

; YbYfU``mž'UggYgga YbhiHug\_g'a i ghVY'gi Va ]hhYX'Y`YVWfcb]\W)``mij ]U'Y]h\Yf'Hi fb]h]b'cf'U'A ccX`Y Ugg][ ba Ybh'' =b']bgHJb\W'g'k \YfY'h\]g']g'bchdcgg]V`Yž']hk ]``'VY'gHJhYX'cb'mci f'\\ci fgY'g'A ccX`Y'g]hY'k ]h\ U`hYfbUh]j Y'gi Va ]gg]cb'XYhJ]`g''

: cf']b $\mathbb{Z}$ cfa Uh]cb'cb'\ck 'hc'gi Va ]h'Ugg][ ba Ybhg'cb`]bY'j ]U'A ccX`Y. `\hhdg.##gh XYbh'i bgk "YXi "Ui  $\mathbb{A}$ ck! qi Va ]h'Ugq][ ba Ybha ccX`Y

## 5 WUXYa ]W<cbYghmUbX D`U[]Uf]ga

D`U[]Uf]ga `]g`i g]b[ 'h\Y`k cfXg`cf`]XYUg`cZch\Yfg`UbX`dfYgYbh]b[ 'h\Ya `Ug`mci f`ck b"'=hWUb`hU\_Y`a Ubm Zcfa gžZfca `XY`]VYfUhY`W\YUh]b[ 'hc`UWW]XYbhU``mWcdm]b[ 'Zfca `U`gci fW'k ]h\ci hUW\_bck `YX[ Ya Ybh'

 $I BGK `[fci dg'd`U[]Uf]ga `]bhc'h\Y'Zc``ck]b[`WUhY[cf]Yg.$ 

 $7 \text{ cdm}b[...i g]b[...h\Y.gUa Y.cf.j Yfmig]a] \Uf'k cfXg'hc'h\Y.cf][]bU''hYl h'cf']XYU'k]h\ci h'U\V_bck `YX[]b[...h\Y.cf][]bU''hYl h'cf']XYU'k]h'cf']$ 

#### 5 WUXYa ]W = b Zcfa Uh cb.

: cf`YggYbhJU``gh XYbh`]bZcfa UhJcb`fY`UhJb[ 'hc.

- fYei Yghg Zcf Yl hYbg]cb/
- `UhY`gi Va ]gg]cbg`[i ]XY`]bYg/
- fYj ]Yk 'cZa Uf\_g/
- I BGK '< YU`h\ 'UbX'GUZYhm'dc`]W[Yg/
- YI Ua ]bUhcb dfcWXi fYg/
- gdYWJU``Wcbg]XYfUhJcb`]b`h\Y`Yj YbhcZ]``bYgg`cf`a ]gUXj Ybh fY/
- gh XYbhYei ]mUbX X]gUV]`]m/
- UbX'ch\Yf'YggYbhJU`'UWUXYa ]W]bZcfa UhJcbž'gYY

\hdg.#k k k "Uffg"i bgk "YXi "Ui #W ffYbhgh XYbhg#UWJXYa ]W]bZcfa Uf]cb#dfchcWc`g![i]XY`]bYg#

a U[Y'7fYX]h

D\chc VmHcV]Ug Hi ``]i g cb l bgd Ug\

7F = 7CG

7F = 7CG Dfcj ]XYf 7cXY. \$\$\$-,;