

ARTS2455

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HYfa 'H\fYY''##'&\$&\$

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7cbj Ybcfg

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7ci fgY 8YW] g

7 fYX]hDc]bhg**

Gi a a UfmcZh\Y'7ci fgY

H\]g'Wci fgY YI d'cfYg'h\Y XfUa UhJWW.Ub[Yg'hc'[YbXYf'UbX'gYI i U']lmibcfa g'YI dYf]YbWX.VmdYcd'Y '`]j]b[]b'7\]bU'cf'cdYfUhJb[']b'h\Y'G]bcd\cbY'k cfX"'H\Y'Wci fgY YI Ua]bYg'h\Y'hfUbgZcfa UhJcb']b'h\YgY'fYU'a g Zfca ']a dYf]U''hJa Yg'h\fci [\'hc'h\Y'W ffYbhYfU"'±ig\ck g'h\Y'cb[c]b['hYbg]cb'VYk YYb'dcdi 'Uf']XYUg'UVci h fffUX]hJcbfiUbX'fa cXYfb]mfiUg'[YbXYf'UbX'gYI i U']lmibcfa g'UbX'dfUWJWg'\Uj Y'W\Ub[YX'cj Yf'hJa Y"'±h YI Ua]bYg']bhYfj YbhJcbg'Vm7\]bUfg'j Uf]ci g'[cj Yfba Ybhg'UbX'`Y[U'''gmghYa g'UbX'WJa dU][bg'VmUWJj]]ghg UbX'fYZcfa Yfg'hc'W\Ub[Y'h\Y'ghUhi g'ei c'Ug'k Y'''Ug'h\Y'i gY'cZgYI 'UbX'[YbXYf'VmWfYUhJj Y'Uff]ghgž'k f]hYfg UbX'UXj YfhJgYfg"'Nci 'k]'''YUfb'Uvci hd\Ybca YbU'gi W\ 'Ug. 'dfc[fYgg'hck UfXg'gYI 'Yei U']lmž'hYbg]cbg VYfk YYb']bX]j]Xi U''XYg]fYg'UbX'ZYa]b]b]hJYg']b''cWJ''UbX'[`cvU''WcbhYI hgž'X]j Yfg]hm]b'[YbXYf'UbX gYI i U']lmbcfa g'Ua cb['7\]bUfg'bcb!<Ub'Yh\b)MJhJYg'UbX'X]ZYfYbhigcWJU''WUggYgž'W ffYbhW\U''Yb[Yg']b [YbXYf'UbX'gYI i U']lmbcfa g']b'fY'UhJcb'hc'd\Ybca Ybcb'']_YZJa]'mZcfa UhJcbžYa d'cma Ybhz'dc']hJWJ'

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8YHJ]YX`]bghfi Whjcbg`Zcf`YUW\`UggYgga YbhHJg_'k]``VY`i d`cUXYX`hc`A ccX`Y"`FYZYf`hc`UggYgga YbhVf]YZ'`

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DYfgcbU`*\DHYfdfYfUfJcb'	&\$I	(da 'Hi YgXUm']b'K YY_'+	%ž&Ž Ž(ž)
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GhUfhXUhY. K YY_&

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Gh XYbhg k]```dfYgYbhh\Y]f'i bXYfgHUbX]b['UVci hU'gY`ZgY`YVMYX`WJgY'fY`UhYX`hc 'h\Y`k YY_fg``X]gW gg]cb hcd]W'`H\Ymk]```VY`Ug_YX`hc 'dfca dhX]gW gg]cb 'Zcf'h\Y]f'dYYfg"'H\Y`ZYYXVUW_k]```VY`dfcj]XYX'j]U'U'F i Vf]W Zcf'DfYgYbhUh]cbg`W ffYbhm]b'i gY`]b'5g]Ub'Gh X]Yg'Wci fgYg"

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Gi Va]gg]cb`bchYg.Mci `WJb`YX]hmci f`dfYgYbhUh]cb`UbX`h\Y`hfUbgWf]dh]b`DDH`UbX`gUj Y`]hUg`U`D8: `Z]`Y`Zcf Z|bU``gi Va]gg]cb"

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GHJfhXUhY. Bch5dd`]WUV`Y

8YHJ]`g.

Ghi XYbhgʻk]```gi Va]hiU'dYfgcbU`]nYX'UggYgga Ybhhcʻg\ck WJgY'h\Y]fʻi bXYfghJbX]b['UVci h[YbXYfʻ]bʻ7 \]bU" H\]g'UggYgga YbhiWJb'VY`]bʻh\Y`Zcfa 'cZg\cfhiYggUmžj]XYcžXcW a YbhJfmž'dcghYfž'dcXWJghžYh\bc[fUd\]W]bhYfj]Yk žk YVg]hY'cf`Ubmch\Yf`Zcfa Uhg"'Ghi XYbhgʻg\U```X]gW ggʻh\Y]f'dfcdcgU`gʻk]h\'h\Y``YWhi fYf'UbX cVhJ]b'dYfa]gg]cb'VYZcfY'gi Va]hh]b['h\Y`UggYgga Ybh'

C fu`ZYYXVUW"

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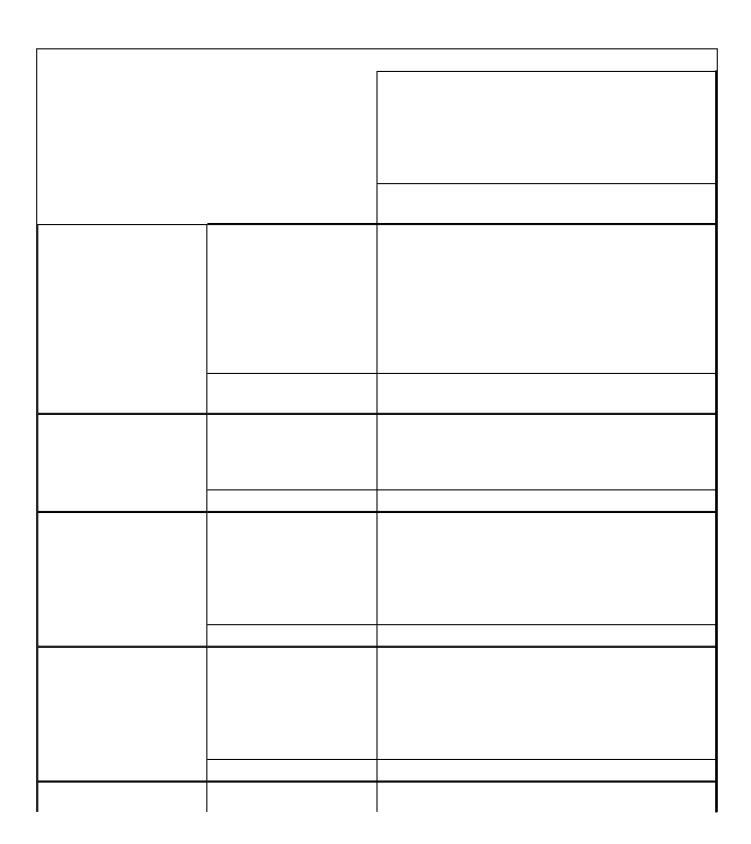
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Ghi XYbhgik]```\Uj Yihk cicdhjcbgiZcfih\YihUg_"'Cdhjcbi%]giU'WU"'&ž(\$\$!kcfXifYgYUfW. YggUm'iGhi XYbhgik]``VYUg_YXihcigY`YWhiUifYgYUfW. iei YghjcbiZca iU'bca]bUhYX``]ghi'H\Y]fihUg_i]gihci[Uh\YfifYgYUfW. iei YghjcbiZca iU'bca]bUhYX``]ghi'H\Y]fihUg_i]gihci[Uh\YfifYgYUfW. iei Yhhk]h\Yj]XYbWfiUbX``c[]\Wi`U'WYUfi iei YbhiUfci bXih\YifYgYUfW. iei YghjcbiZvi hffYggih\]giUf[iei Ybhik]h\Yj]XYbWfiUbX``wca e iei]\WhYi]biU'WYUfikf]hhYbiZJg\]cb"'H\YiYj]XYbWfik]``VY'dfYgYbhYX`]biZcfe U''UWUXYe]\WebiUhJcb'''CdhJcbi&i]giU'Wf]hJWU``fYZYWhJcbiCZh\YiWci fgY"'H\]giHUg_i]giYei]j U'Ybhhcih\YfYgYUfW. YggUm]bihYfe gicZkcfXiYb[ih\"iGhi XYbhgik]``kf]hYiY][\hi'\$\$!kcfX'Wf]hJWU``fYZYWhJcbgiVmh\YiYbXcZh\YihYfe ibcXYeeoffUhYih\Y]fii bXYfgHUbX]b[iUVci hh\YikYy_`mhcd]\WUbXifYUX]b[g"'H\Yikf]hjb[iHUg_i]gh\YiZfUUy\XifYUX]b[g"'H\Yikf]hbXUbWfidi fdcgYg"

K f]hhyb ZYYXVUW "

 $\label{thm:continuous} \begin{tabular}{ll} Hi fb]h]b"gYh]b[."H\]g"Ugg][ba Ybh]g"gi Va]hhYX"h\fci [\Thi fb]h]b"UbX"gh XYbhg"WUb"gYY"Hi fb]h]b"g]a]"Uf]hm fYdcfhg" \end{tabular}$



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FYZYf'hc'k YY_`mfYZYfYbWYg'UbX'@Y[Ubhc'fYUX]b['`]ghi]b'AccX`Y'

FYWca a YbXYX FYgci fWYg

9Xk UfXgž@"&\$\$, ž9W VWd Ba f f[Ueł S`V 6 W_ a UdSUk, I a_ W e E g XdSYW[5 Z [SžGHJb ZcfXž7 5 žGHJb ZcfX I b]į Yfq]hm DfYqq"

9j Ubgž'< "'% - +ž'l a_ W S` V eWj gS'{fk [` 5Z[` S, Va_ [` S` f V[eUagdeWe a X X W_ S WeWj gS'{fk S` V Y W V W de[` UW#+&+ž' 7 Ua Vf]X[Y. 'Dc`]miDfYgg"

A Ubbž@"G'&\$%%39W VWdS`V EWjgS1fk [? aVWd 5Z[WeW: [efack37Ua Vf]X[Y:7Ua Vf]X[Y'I b]j Yfg]lm DfYgg"

Gcb['; Yb['UbX'<]fXž'8"'&\$%(ž'? W S` V ? SeUg f [f[We [5a`fW_ bac6ck 5Z[Sž'@Y]XYbž'BYh\Yf'UbXg. '6f]`"

K Ub[DUb &\$%) zzahWS V? Sch[SYW] 9 aTS1 Y 5 Z Sz 5 V b Xcbz C I cb / BYk Mcf_ : F ci hYX Y "

NUb['L]UckY]'UbX'N\Uc'L]Uc'@''fYXgŁ'&\$% ž: S`VTaa] a` fZW8S_['k S`V ? Scb[SYW[' 5 Z[' Sž'9Xk UfX 9'[Uf"

7ci fgY'9j U'i Uhcb'UbX'8Yj Y'cda Ybh

H\]gʻWci fgYʻk]``VYʻYj U`i UhYXʻj]Uʻh\Yʻa m9l dYf]YbWYʻgi fj YmgʻUhih\YʻYbXʻcZh\YʻhYfa "ʻ⊋mci ʻ\Uj Y gi [[Ygh]cbgʻcbʻk Umgʻhcʻ]a dfcj Yʻh\YʻWci fgYʻXi f]b['h\YʻhYfa ž'd`YUgYʻZYY``ZfYYʻhcʻWca YʻUbXʻhU`_ihcʻi g"ʻK Y k Y`Wca Y`mci fʻZYYXVUW"

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\ci fg'UfY', .\$\$Ua '-'%\$.\$\$da 'cb'k YY_XUmg'UbX'-.\$\$Ua '-').\$\$da 'cb'k YY_YbXg'fl *) 'XUmg'U'mYUft'''=Z'mci
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a i ghfYhJ]b'mci f'h]W_Yhbi a VYf'Zfca '9! hy'fbU''Gi ddcfhfU'cb['k]h\ 'Ubmch\Yf'fy'Yj UbhXcW a Ybhgt'hc
]bWi XY'Ug'Yj]XYbW' hc'gi ddcfhmci f'Y! hy'bg]cb'Udd']WUh]cb"'=Zmci 'Ya U]''9! hy'fbU''Gi ddcfhmci 'k]'`
Ui hca Uh]WJ'`mfYW']j Y'U'h]W_Yhbi a VYfz'Vi h]Zmci 'hY'Yd\cbY'mci 'k]``bYYX'hc'gdYW]Z]WJ'`mUg_'Zcf'cbY''
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; YbYfU`mž'UggYgga YbhiHug_g'a i ghVY'gi Va]hhYX'Y`YVWfcb]\WJ``mij]U'Y]h\Yf'Hi fb]h]b'cf'U'A ccX`Y Ugg][ba Ybh''=b']bgHJb\W'g'k \YfY'h\]g']g'bchdcgg]V`Yž']hk]```VY'gHJhYX'cb'mci f'\\circ i fgY'g'A ccX`Y'g]hY'k]h\U`hYfbUh]j Y'gi Va]gg]cb'XYHJ]`g"

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5 WUXYa]W<cbYghmUbX D`U[]Uf]ga

D`U[]Uf]ga i]gii g]b[ih\Yik cfXgicfi]XYUgicZch\YfgiUbXidfYgYbh]b[ih\Ya iUgimci fick b"i=hWJbihU_Yia Ubm Zcfa gžZfca iXYi]VYfUhYiWXYUh]b[ihciUWW]XYbhU`mWcdm]b[iZfca iUigci fWYik]h\ci hiUW_bck iYX[Ya Ybh'

IBGK [fcidg'd'U[]Uf]ga]bhc'h\Y'Zc``ck]b['WUhY[cf]Yg.

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- VY`Uk UfY`cZd`U[]Uf]ga ž`Wcdmf][\hz'l BGK `Gh XYbh7cXY`cZ7cbXi WhUbX`5VWWdhUV`Y`l gY`cZ I BGK `=\forall H`F Ygci f\W\g`Dc`]\m\m
- VY 'Uk UfY 'cZh\Y 'ghUbXUfXg 'cZVY\Uj]ci f'Yl dYWYX 'cZYj YfmcbY ']b 'h\Y 'l BGK 'Wca a i b]hm
- `cWUHY 'gYfj]WYg'UbX ']bZcfa UH]cb'UVci hI BGK 'UbX'I BGK '@]VfUfm

Gca Y'cZh\YgY'UfYUg'k]``VY'ZJa]`]Uf'hc'mci ž'ch\Yfg'k]``VY'bYk"'; U]b]b['U'gc`]X'i bXYfgHJbX]b['cZU``h\YfY`UhYX'UgdYWng'cZ9@+69'k]``\Y`d'mci 'a U_Y'h\Y'a cghicZmci f'ghi X]Yg'UhI BGK "'\\hd.##qi VYWfi |XYg"`]VfUfm'i bqk "YXi "Ui #\`]qY#JVci hY`]qY

5WUXYa]W±bZcfaUhjcb

: cf'YggYbhJU`ghi XYbh]bZcfa UhJcb'fY`UhJb['hc.

• fYei Yghg Zcf Yl hYbg]cb/