

# **ARTS2462**

±bhYfa YX]UhY '7 \]bYgY 'Zcf'6UW\_[ fci bX'GdYU\_Yfg'6

HYfa 'H\fYY''##'&\$&\$

## 7ci fgY'Cj Yfj ]Yk

### GHJZ:7cbHJWh:8YHJ]`g

#### 7cbj Ybcfg

B Ua Y	9a U]`	5j U]`UV]`]hm	@cWUhjcb	D∖cbY
K U\'; i Ub'@]a	k [`]a 4 i bgk "YXi "Ui	Vm'Uddc]bha Ybh	A cfj Yb 6fck b	\$&`-',)
	_		&()	%* , %

#### @YWhi fYfg

BUa Y	9a U]`	5j U]`UV]`] <b>m</b>	@cWUh]cb	D\cbY
7\Yb[!K Y] <sup>*</sup> K Ub[	W.Yb[!kY]"k Ub[4 i bgk "YXi "Ui	Vm'Uddc]bha Ybh	A cfj Yb 6fck b	\$&`-',)
			&(\$	&, %)

#### Hi hcfg

B Ua Y	9a U]`	5j U]`UV]`]hm	@cWUhjcb	D\cbY
7\Yb[!K Y] <sup>.</sup> K Ub[	WXYb[!kY]"kUb[4 i bgk"YXi"Ui	VmUddc]bha Ybh	A cfj Yb 6fck b	\$&`-',)
			&(\$	&, %)

### GWXcc`7cbHJWhi±bZcfa Uh]cb

GWkcc`cZ<iaUb]hJYg'UbX'@Ub[iU[Yg

@c\Wbhcb. G\\cc``C\Z]\\\žA\cfj\Yb'6fck\b'6i]\X]b[\z'@\j\Y``&z'&),

 $\texttt{CdYb]b[} \ \, (\texttt{cifg.} \ \, \texttt{AcbXUm!} \ \, (\texttt{f]XUm\'z} \ \, (\texttt{Ua} \ \, (\texttt{I})) \ \, \texttt{da}$ 

D\cbY.'Ž\*%'&'-',)'%\*,%

: UI . Ž\*%'&'-',)', +\$)

9a U]`. '<u>\U`4 i bgk "YXi "Ui</u>

## 7ci fgY 8YW] g

#### 7 fYX]hDc]bhg \*

#### Gi a a UfmcZh\Y 7ci fgY

#### 7 ci fgY @YUfb]b[ Ci hMca Yg

%" I bXYfghUbX'U'k ]XY fUb[Y'cZhYl hg Zfca 'j Uf]ci g'gci fWyg'UbX'cb'U'j Uf]YhmcZhcd]Wg

- &" 7 ca dcgY'g\cfhYggUmg']b'7\]bYgY'cb'U'[]j Yb'hcd]W
- ' " 5 Wei ]fY 'Wca a i b]WUh]cb 'g\_]``gž'UbX`]XYbh]Zm'Wca a i b]WUh]cb 'ghm`Yg`]b '7 \]bYgY

#### HYUWX]b[ GlfUhY[]Yg

H\]g``Ub[i U[Y`Wci fgY`fYei ]fYg`mci `hc`UhhYbX`WUggYg`hchU`]b[`Zci f`\ci fg`dYf`k YY\_..cbY`&!\ci f``YWhi fY`UbX cbY`&!\ci f``h hcf]U`"H\Y``YWhi fY`Wcj Yfg`bYk 'j cWUVi `Ufmž`hYl hž'[fUa a Uh]WU``ghfi Whi fYž'UbX`gcW]U`ž'W``hi fU` UbX`\]ghcf]WU``Uk UfYbYgg`]b`h\Y`7\]bYgY`WcbhYl h'`H\Y`h hcf]U``hUf[Yhg`k cf\_Vcc\_Yl YfW]gYg`UbX`dfcj ]XY cddcfhi b]h]Yg`Zcf`ghi XYbhg`hc`gdYU\_`7\]bYgY`UbX`UXXfYgg`UbmfYUX]b[``UbX`k f]h]b[``]ggi Yg"`Mci ``UfY`U`gc fYei ]fYX`hc`gdYbX`U'a ]b]a i a `cZ' `\ci fg`dYf`k YY\_`hc`ghi Xmci hg]XY`h\Y`WUgg`]b`cfXYf`hc`UW\]Yj Y`U gUh]qZJWhcfm`YUfb]b[`ci hWca Y"`

H\Y'Wci fgY'U]a g'hc'Yb\UbW'UbX'UggYgg'gh XYbhg''Zci f``Ub[i U[Y'g\_]``g'h\fci [\ci hh\Y'Wci fgY'k\YfY ghfi Wh fU`'UbX']bhYfUWhj Y'a Yh\cXg'UfY'Yei U``mUdd`]YX"'±0'YUW\``Yggcbžmci 'k]```ghUfhk]h\'j cWUVi `UfmUbX ghfi Wh fU``dfUWhJW''k\]W\'k\]``h\Yb'VY'Zc``ck YX'VmhUg\_!VUgYX'UWhj ]hJYg"'7 cbg]XYf]b['h\Uhmci 'UfY VUW\_[ fci bX``YUfbYfgž'U'gi VghUbhJU``Ua ci bhcZWUgg'k]``VY'WcbXi WhYX']b'7\]bYgY"'H\Y'`Ub[i U[Y cZ]bghfi WhJcb']b'h\Y'WUgg']g'df]a Uf]`mh\Y'hUf[Yh`Ub[i U[Y'UbX'9b[`]g\'k]``VY'i gYX'cb`mk\Yb'bYWfggUfm hc'WUf]Zm]ggi Yg"'H\Y'UggYgga Ybhg'k]``fYei ]fY'mci 'hc'XYa cbghfUhY'U'gc`]X'Wca dfY\Ybg]cb'UbX'cdhJa U` i gY'cZWcbhYbrg'Wcj YfYX']b'h\Y'hYI Wcc\_'fUh\Yf'h\Ub'hc'fYdYUhfi X]a YbhUfm\_bck `YX[Y'UWei ]fYX'VmfchY"

## 5ggYgga Ybh

### 5ggYgga Ybh'HUg\_g'

sggYgga Ybh'tUg_ K Y][\h		8iY'8UhY	Gh XYbh@YUfb]b[ Ci hWca Yg 5ggYggYX	
HYgh&	&\$I	K YY_`)	%ž&ž(	
; fci d'DfYgYblUljcb'	&) ı	K YY_*%\$	' <u>ž</u> (	
HYgh%	))।	: ]bU``9  Ua `DYf]cX	%ž&ž(	

#### 5ggYgga Ybh8YlU]`g

5ggYgga Ybh% HYgh&

GhUfhXUhY. Bch5dd`]WUV`Y

8 YW] g.

HYgh]b['j cWJVi `Ufmž'[fUa a Ufž'a UghYfmicZk f]h]b['WXUfUWhYfg'UbX'k f]h]b['g\_]``g'f@Yggcb''&\$\!/+\$`a ]bi hYg"

: YYXVUW\_TUbXTWca a Ybhg`]b`hi hcf]U`g"

5XX]h]cbU`XYhU]`g.

D`YUgY`fYZYf`hc`AccX`Y`UbX`]b!WUgg`UbbcibWYaYbhg`Zcf`U```id!hc!XUhY`UggYggaYbh`]bZcfaUh]cb`ZcfHYfa'' &\$&\$"

5ggYgga Ybh&; fci d DfYgYbhJh]cb

GhUfhXUhY. Bch5dd`]WUV`Y

8YW]`q.

Cfu`ZYYXVUW\_']b'WUgg

5XX]h]cbU`XYhU]`g.

D`YUgY`fYZYf`hc`AccX`Y`UbX`]b!WUgg`UbbcibWaYbhg`Zcf`U```id!hc!XUhY`UggYggaYbh`]bZcfaUh]cb`ZcfHYfa'' &\$&\$"

5ggYgga Ybh' . HYgh%

GhUfhXUhY. Bch5dd`]WUV`Y

#### 8YHJ]`g.

 $\label{thm:continuous} HYgh]b[~"j~cWUVi~`Ufmž'[~fUa~a~Ufž'a~UghYfm'cZk~f]h]b[~`W.UfUWYfg'`UbX'k~f]h]b[~"g_]``g'`f@Yggcb'`%%!~@Yggcb'`%+Ł/%&$`a~]bi~hYg''$ 

: YYXVUW\_'UbX'Wca a Ybhg']b'hi hcf]U'g

.

#### 5XX]h]cbU`XYHJ]`g.

D`YUgY`fYZYf`hc`AccX`Y`UbX`]b!WUgg`UbbcibWaYbhg`Zcf`U```id!hc!XUhY`UggYggaYbh]bZcfaUh]cb`ZcfHYfa`' `&\$&\$"

## Gi Va ]gg]cb cZ5ggYgga YbhHUg\_g

## Hi fb]h]b Gi Va ]gg]cb

Image: Ybwb: bh/f'u'dfcv'ya k \yb'uhh/a dhjb[ 'hc'gi va ]hmci f'ugg][ ba Ybhh\fci [ \ 'Hi fb]h]bz'd'YugY

Hy'Yd\cby'9| h/fbu''Gi ddcfhcb'-', ) " ' ' %cf'Ya u] h\ya 'cb'Yl h/fbu'h/hgi ddcfh4 i bgk "YXi "Ui "'Gi ddcfh\ci fg'ufy', .\$\$ua '-'%\$.\$\$da 'cb'k YY\_Xumg'ubX'-.\$\$ua '-').\$\$da 'cb'k YY\_YbXg'fl \*) 'Xumg'u'mYuft'' I'mci

Ufy'i buv'y 'hc'gi va ]hmci f'ugg][ ba YbhXi Y'hc'u'Zui 'hk ]h\ 'Hi fb]h]b'mci 'a Um'udd'mZcf'ub'Yl h/bg]cbz'vi hmci

a i ghfYhu]b'mci f'h]w\_Yhbi a vYf'Zfca '9| h/fbu''Gi ddcfhfU'cb[ 'k ]h\ 'Ubmch\Yf'fy'Yj UbhXcW a Ybhgthc

]bWi XY'ug'Yj ]XYbW'hc'gi ddcfhmci f'Yl h/bg]cb'udd']\wuh]cb"'Imci 'Ya U]''9| h/fbu''Gi ddcfhmci 'k ]'`

Ui hca Uh]\wu'`mfYw']j Y'u'h]w\_Yhbi a vYfzvi h]Zmci 'hY'Yd\cbY'mci 'k ]``bYYX'hc'gdYw]Z]\wu'`mug\_'Zcf'cbY''

Hi fb]h]b'u'gc'dfcj ]XYg'i dXUhyg'cb'h\Y]f'gmghYa 'ghUh' g'cb'Hk]hYf''

; YbYfU`mž'UggYgga YbhiHug\_g'a i ghVY'gi Va ]hhYX'Y`YVWfcb]\WJ``mij ]U'Y]h\Yf'Hi fb]h]b'cf'U'A ccX`Y Ugg][ ba Ybh''=b']bgHJb\W'g'k \YfY'h\]g']g'bchdcgg]V`Yž']hk ]```VY'gHJhYX'cb'mci f'\\circ i fgY'g'A ccX`Y'g]hY'k ]h\U`hYfbUh]j Y'gi Va ]gg]cb'XYHJ]`g"

cfi]bZcfa Uhjcbicbi\ckihcigi Va ]hUgg][ ba Ybhgicbi]bYij ]UiA ccXiY.i\hdg.#gh XYbhi bgk "YXi "Ui #\ck! gi Va ]hUgg][ ba Ybha ccXiY

## 5 WUXYa ]W<cbYghmUbX D`U[]Uf]ga

D`U[]Uf]ga i]gii g]b[ih\Yik cfXgicfi]XYUgicZch\YfgiUbXidfYgYbh]b[ih\Ya iUgimci fick b"i=hWJbihU\_Yia Ubm Zcfa gžZfca iXYi]VYfUhYiWXYUh]b[ihciUWW]XYbhU`mWcdm]b[iZfca iUigci fWYik]h\ci hiUW\_bck iYX[Ya Ybh'

IBGK [fcidg'd'U[]Uf]ga ]bhc'h\Y'Zc``ck]b['WUhY[cf]Yg.

- i bXYfgfUbX mci f'f][\hg'UbX'fYgdcbg]V]`]hJYg'Ug'U'gh XYbhUhl BGK
- VY`Uk UfY`cZd`U[]Uf]ga ž`Wcdmf][\hz'l BGK `Gh XYbh7cXY`cZ7cbXi WhUbX`5VWWdhUV`Y`l gY`cZ I BGK `=\forall H`F Ygci f\W\g`Dc`]\m\m
- VY 'Uk UfY 'cZh\Y 'ghUbXUfXg 'cZVY\Uj ]ci f'Yl dYWYX 'cZYj YfmcbY ']b 'h\Y 'l BGK 'Wca a i b]hm
- `cWUHY 'gYfj ]WYg'UbX ']bZcfa UH]cb'UVci hI BGK 'UbX'I BGK '@]VfUfm

Gca Y'cZh\YgY'UfYUg'k]``VY'ZJa]`]Uf'hc'mci ž'ch\Yfg'k]``VY'bYk"'; U]b]b['U'gc`]X'i bXYfgHJbX]b['cZU``h\YfY`UhYX'UgdYWng'cZ9@+69'k]``\Y`d'mci 'a U\_Y'h\Y'a cghicZmci f'ghi X]Yg'UhI BGK "'\\hd.##qi VYWfi |XYg"`]VfUfm'i bqk "YXi "Ui #\`]qY#JVci hY`]qY

# 5WUXYa]**50¥MUXXYa**jc**]W±bZcfaUh]cb**

: cf`YggYbhJU``ghi XYbh`]bZcfa UhJcb`fY`UhJb[ 'hc.

- fYei Yghg Zcf Yl hYbg]cb/
- `UhY`gi Va ]gg]cbg`[i ]XY`]bYg/
- fYj ]Yk 'cZa Uf\_g/
- I BGK '< YU'h\ 'UbX'GUZYhm'dc']W]Yg/
- YI Ua ]bUh]cb dfcW/Xi fYg/
- gdYW]U``Wcbg]XYfUh]cb']b'h\Y'Yj Ybh'U`')