

ARTS2485

9|d`cf]b[': fYbW\'@]b[i]gh]Wg

HYfa 'H\fYY''##'&\$&\$

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GHJZ7cbHJWh8YHJ]`g

7cbj Ybcfg

B Ua Y	9a U]`	5j U]`UV]`]lm	@cWUh]cb	D\cbY
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@c\\U||cb. G\\cc``C\\Z|\\\žA\cfj\Yb'6fck\b'6i]\X]b[\z'@\j\Y``&z'&),

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D\cbY.'Ž*%'&'-',)'%*,%

: UI . 'Ž * %'&'-' ,) ', +\$)

9a U]`. '<u>\U`4 i bgk "YXi "Ui</u>

7ci fgY⁻8YHJ]`g

7 fYX]h'Dc]bhg'*

Gi a a UfmcZh\Y 7ci fgY

 $\label{thm:continuous} $$H\]g'WcifgY'HUi[\hi]b'9b[\]g\cZYfg'U'gmghYaUh]WWcadUf]gcb'cZ: fYbW.'UbX'9b[\]g\'Ug'ZUf'Ug'gcibXgž$

5ggYgga Ybh

5ggYgga Ybh'HUg_g'

5ggYgga Ybh'hJg_	K Y][\h	8i Y'8UHY	Gh XYbh@YUfb]b[Ci hWca Ygʻ5ggYggYX
HYghi) \$1	8 i f]b[``YWni fYgžf]k:k YY_''. &, #\$-#&\$&\$/f]]k:k YY_'). %&#%\$#&\$&\$</td><td>%ž&</td></tr><tr><td>Dfc ΥWi</td><td>) \$1</td><td>CfU`dfYgYbfUf]cb`XiY`cb kYY,Vm) da žGi bXUm \$,#%#&\$&\$/f\Y`k f]ffYb fYdcfh]g`XiY`Xi f]b[`f\Y`YI Ua dYf]cX.`cb`&+#%#&\$&\$`Vm) da"</td><td>' <u>ž</u>(</td></tr></tbody></table>	

5ggYgga Ybh'8YHJ]`g

5ggYgga Ybh'% 'HYgh

 $\textbf{GhUfhXUhY}. \ \texttt{`Bch'5dd`]WUV`Y}$

@Yb[h\."\\U"") \$ a]b""YU\\

8YHJ]`g.

 $\label{thm:continuous} Hk\ c\ "]b!\ WUgg'\ H'\ ghg'\ c\ ZWU"')\ \$'\ a\]bi\ h'\ g'\ YUWX'\ We'j\ Yf]b[\ 'h'\ Y'\ We'bh'\ bh'\ c\ Zh'\ Y'\ We'i\ fgY''j\]U'\ dfc\ V'\ Ya\ 'gY\ g'\ Ub\ X'g\ cfh\ YggUmei\ Ygh]cbg'''\ H'\ Y'\ ghg'\ Uf\ 'dfY\ W'\ XY\ X'\ Vm'\ Zcfa\ Uh'j\ Y'\ k\ YY_`mcb`]bY'\ Ub\ X''\ f'\ h'\ f'\ h'\ f'\ H'\ Yf\ Yf\ Ygg''g''$

: YYXVUW_'j]U']b!WUgg'X]gW gg]cbž'Yffcf'WcffYWf]cbž'UbX'k f]hhYb'Wca a Ybhg"

Hi fb]h]b gYhh]b[. "

5 https://bxubww.Fyei]fyaybhg

 $\hbox{Ghi XYbhg'UfY'ghfcb[`mYbWci fU[YX'hc'UhhYbX'U```WUggYg'UbX'fYj]Yk ``YWhi fY'fYWcfX]b[g''] }$

7ci fgY'GWXYXi `Y

J]Yk 'WUgg'hja YhUV'Y

H]a YtUV`Y

8 UHY	HmdY	7 cbhYbh
C'K YY', 'GYdhYa VYf'!'- GYdhYa VYf		: Ua j`]Uf]nY`mci fgY`Zk]h\`h\Y`7ci fgY`CjYfj]Yk`f17CŁ

		GYa]bUf YI YfW]gYg	
K YY_').'%&'CWfcVYf'!'%* CWfcVYf	Hcd]W	H\Y`Zcfa Uhjcb`UbX`a YUb]b[`cZk cfXg`fWcbhjbi UhjcbŁ"	
		BUa YgʻcZcWW dUhjcbgʻUbXʻ[YbXYfʻ]bWi g]j Y `Ub[i U[Y"	
		GYa]bUf ⁻ 91YfW]gYg"	
	5ggYgga Ybh	H9GH'!'&)ı 'flWU'')\$'a]b"ž'cb`]bYž'Xif]b['h\Y''YWifYŁ	
K YY_'*.'%-'CWvcVYf'!'&' CWvcVYf	@YWi fY	BC '@97 HI F 9 'C B 'K 99? '*	
	Hi hcf]U`	BC 'HI HCF =5@'CB'K 99? '*	
K YY_'+.'&*'CWfcVYf'!'' \$ CWfcVYf	Hcd]W	H\Y`[fUa a Uf`cZ: fYbW\.`a cfd\c`c[miUbX`gmbHUI	
		9 d`cf]b['h\Y': fYbW\'`Ub[i U[Y. '7 \Udh\fg'+'/ ',	
		HfUX]hjcbU`'/ 'Zcfa U`'XYZjb]hjcbg'cZWUhY[cf]Yg'cZk cfXg	
		GYa]bUf'YIYfW]gYg	
K YY_', .`&BcjYa VYf'!`* BcjYa VYf	Hcd]W	H\Y`[fUa a Uf`cZ: fYbWX`f17cbh]bi Uh]cbŁ	
		: fca 'k cfXg'hc'gYbhYbWYg	
		GYa]bUf'YI YfW]gYg	
	5ggYgga Ybh	; fci d'cfU`dfYgYblUljcbg'!'&)ı 'f%) 'lc'&\$'a]bi lYgž gi Va]lHYX'cb`]bY'cb'Jc]WYH\fYUX'j]U'A ccX'YŁ"	
		K Uh/W. 'UbX'dcgh'Wca a Ybhg'cb'hk c'ch\Yf'[fci dgfi cb`]bY'dfYgYbhUh]cbg'VYZcfY'k YY_'-'h hcf]U`"	
K YY_''- 'Bcj Ya VYf'!	@YVVn fY	H\Y`[fUa a Uf`cZ: fYbWX`fWcbf]bi Uf]cbŁ	
% Bcj Ya VYf		7 ca dUf]gcb'VYlk YYb': fYbW\'UbX'9b[`]g\	
		: YYXVUW_'UbX'X]gW gg]cb'cZcfU`'dfYgYbfUf]cbg fXi f]b['fi fcf]U`gŁ"	
		GYa]bUf'YI YfW]gYg	
K YY_'%\$.'%*'Bcj Ya VYf'! &\$'Bcj Ya VYf	Hcd]W	H\Y`[fUa a Uf`cZ: fYbWX`fWcbh]bi Uh]cbŁ"	
lay Doj Ta vii		7 cbWi g]cb cZh\Y Wa dUfUhj Y UddfcUW\ hc : fYbW\	
		DfYdUfUhjcb~cZh\Y~ZjbU~Ugg][baYbhfKiY~Xif]b[
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FYgci fW/g

DfYgWf]VYX F Ygci fWyg

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- 5XX]h]cbu``a UhYf]u`g`dfcj]XYX'j]U'A ccX`Y"

FYWca a YbXYX FYgci fW/g

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Gi Va]gg]cb cZ5ggYgga YbhHUg_g

Hi fb]h]b Gi Va]gg]cb

Image: Ybwei bhyfu'dfcv'ya k \yb'uhhya dhjb['hc'gi va]hmci f'Ugg][ba Ybhh\fci [\ 'Hi fb]h]bž'd'YUgY

Hy'Yd\cby'9| hy'fbu''Gi ddcfhcb'-',) '' ' ' %cf'Ya U]''h\Ya 'cb'Y! hy'fbu'hy'hgi ddcfh4 i bgk "YXi "Ui "''Gi ddcfh
\ci fg'UfY', .\$\$Ua '-'%\$.\$\$da 'cb'k YY_XUmg'UbX'-.\$\$Ua '-').\$\$da 'cb'k YY_YbXg'fl *) 'XUmg'U'mYUft"'=Z'mci
UfY'i bUV'Y'hc'gi va]hmci f'Ugg][ba YbhXi Y'hc'U'ZJi 'hk]h\ 'Hi fb]h]b'mci 'a UmUdd'mZcf'Ub'Y! hy'bg]cbž'Vi hmci
a i ghfYhJ]b'mci f'h]W_Yhbi a VYf'Zfca '9! hy'fbU''Gi ddcfhfU'cb['k]h\ 'Ubmch\Yf'fy'Yj UbhXcW a Ybhgt'hc
]bWi XY'Ug'Yj]XYbW' 'hc'gi ddcfhmci f'Y! hy'bg]cb'Udd']WUh]cb"'=Zmci 'Ya U]''9! hy'fbU''Gi ddcfhmci 'k]'`
Ui hca Uh]WJ'`mfYW']j Y'U'h]W_Yhbi a VYfZ'Vi h]Zmci 'hY'Yd\cbY'mci 'k]``bYYX'hc'gdYW]Z]WJ'`mUg_'Zcf'cbY''
Hi fb]h]b'U'gc'dfcj]XYg'i dXUhy'g'cb'h\Y]f'gmghYa 'ghUh' g'cb'Hk]hyf''

; YbYfU`mž'UggYgga YbhiHug_g'a i ghVY'gi Va]hhYX'Y`YVWfcb]\WJ``mij]U'Y]h\Yf'Hi fb]h]b'cf'U'A ccX`Y Ugg][ba Ybh''=b']bgHJb\W'g'k \YfY'h\]g']g'bchdcgg]V`Yž']hk]```VY'gHJhYX'cb'mci f'\\circ i fgY'g'A ccX`Y'g]hY'k]h\U`hYfbUh]j Y'gi Va]gg]cb'XYHJ]`g"

cfi]bZcfa Uhjcbicbi\ckihcigi Va]hUgg][ba Ybhgicbi]bYij]UiA ccXiY.i\hdg.#gh XYbhi bgk "YXi "Ui #\ck! gi Va]hUgg][ba Ybha ccXiY

5 WUXYa]W<cbYghmUbX D`U[]Uf]ga

D`U[]Uf]ga i]gii g]b[ih\Yik cfXgicfi]XYUgicZch\YfgiUbXidfYgYbh]b[ih\Ya iUgimci fick b"i=hWJbihU_Yia Ubm Zcfa gžZfca iXYi]VYfUhYiWXYUh]b[ihciUWW]XYbhU`mWcdm]b[iZfca iUigci fWYik]h\ci hiUW_bck iYX[Ya Ybh'

IBGK [fcidg'd'U[]Uf]ga]bhc'h\Y'Zc``ck]b['WUhY[cf]Yg.

- i bXYfgfUbX mci f'f][\hg'UbX'fYgdcbg]V]`]hJYg'Ug'U'gh XYbhUhl BGK
- VY`Uk UfY`cZd`U[]Uf]ga ž`Wcdmf][\hz'l BGK `Gh XYbh7cXY`cZ7cbXi WhUbX`5VWWdhUV`Y`l gY`cZ I BGK `=\forall H`F Ygci f\W\g`Dc`]\m\m
- VY 'Uk UfY 'cZh\Y 'ghUbXUfXg 'cZVY\Uj]ci f'Yl dYWYX 'cZYj YfmcbY ']b 'h\Y 'l BGK 'Wca a i b]hm
- `cWUHY 'gYfj]WYg'UbX ']bZcfa UH]cb'UVci hI BGK 'UbX'I BGK '@]VfUfm

Gca Y'cZh\YgY'UfYUg'k]``VY'ZJa]`]Uf'hc'mci žch\Yfg'k]``VY'bYk"'; U]b]b['U'gc`]X'i bXYfgHJbX]b['cZU``h\YfY`UhYX'UgdYWhg'cZ9@&9'k]``\Y`d'mci 'a U_Y'h\Y'a cghicZmci f'ghi X]Yg'Uh'l BGK "'\\hd.##gi VYWfi]XYg"`]VfUfm'i bgk "YXi "Ui #\`]qY#JVci hY`]qY