

ARTS2510

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; fWd_ WW[SfW9 Wd_ S` 3]g]XYU`]Zmci `\Uj Y`gi WWggZ ``mUVWca d`]g\YX'h\Y`\bfcXi Wcfm; Yfa Ub'5 'UbX'6 Wci fgYg cfz]Zmci `\Uj Y`h\Y`Yei]j U`YbhcZ'U`mYUf`cZ; Yfa Ub``Ub[i U[Y``YUfb]b["'\biWcbgc`]XUhYg`UbX YI hYbXg`mci f`dfYj]ci g`mUWei]fYX`cfU``UbX`k f]hhYb'; Yfa Ub``Wca a i b]WUhJcb'g_]``gžUbX`YI hYbXg`mci f j cWUVi `UfmUbX'[fUa a Uf`Zci bXUhJcb"'H\i gž'h\Y`Wci fgY`YbUV`Yg`mci 'hc 'Wca a i b]WUhY`]b`U`a cfY gdcbhUbYci g`UbX`Y`UVcfUhY`k Um]b`; Yfa Ub"`Nci 'k cf_'k]h\`U`fUb[Y`cZUi h\Ybh]W`YUfb]b['a UhYf]U`fZ]WJcbU``UbX`bcb!Z]WJcbU`žcb`WcbhYa dcfUfmUbX`\]ghcf]WJ``hcd]WgŁk\]W\`dfcj]XYg`mci 'k]h\`YI hYbg]j Y_bck`YX[Y`UbX`U`VYhhYf`i bXYfghUbX]b['cZh\Y`gcW]YhJYg`UbX`W`hi fY`cZ; Yfa Ub!gdYU_]b['Wci bhf]Yg"

7ci fgY @YUfb]b['Ci hWca Yg

- %" I bXYfghUbX`UbX`fYgdcbX`]b`; Yfa Ub`hc`h\Y`a U]b`dc]bhg`cZcfU``UbX`k f]hhYb`hYI hg`XYU`]b[`k]h\hcd]\Mg`cZVfcUXYf`gc\MJU``\Wcb\Wfbg`Yb\Wci bhYfYX`]b`h\Y`; Yfa Ub!gdYU_]b[`\Wca a i b]h]Yg"
- &" DfcXi Wig]a d`Yž'Wc\YfYbhihYl hg`fbfU``UbX`k f]hhYbŁ`]b`; Yfa Ub`cb`'Wca a cb`hcd]Wg`cf`UfYUg`cZ dYfqcbU``]bhYfYqh'
- ' " 8 YgWf]VY YI dYf]YbWfg UbX Yj Ybhg UbX dfcj]XY fYUgcbg cf YI d`UbUh]cbg Zcf cd]b]cbg UbX d`Ubg]b Yfa IIb"
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-) "8YjY`cd`ghfUhY[]Yg`hc`Wcaaib]WUhY`YZZYWhjjY`mik]h\`ch\Yf`aYaVYfg`cZh\Y`[fcid"

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H\Y'hYUW\]b['gffUhY[]Yg'cZci f'; Yfa Ub'WUggYg'UfY'VUgYX'cb'h\Y'Wca a i b]Whij Y'UbX'hUg_!VUgYX UddfcUW\žk\]W\'U]a 'Uh[]j]b['gh XYbhg'cddcfh b]hj\g'hc 'dfUwj\W'h\Y]f'Wca a i b]Whijcb'g_]``g']b'WcbhYl hg h\UhiUfY'dYfgcbU``mfY'Yj UbhUbX'WcbbYWfYX'hc'Yj YfmXUm']Z'"'H\i gžgh XYbhg``YUfb'U'j YfmUi h\Ybh]Wi gY'cZh\Y'; Yfa Ub'`Ub[i U[Y'Wca V]bYX'k]h\ W'h fU``UbX\\]ghcfJWU`_bck 'YX[Y"'H\Y'`YUfb]b['a UhYf]U``fdf]bhUbX X][]hU`cUbX``YUfb]b['UWjj]hj\Yg'ff'"['"cb']bY'hUg_gžga U```HUg_g#dfc'YWg']bg]XY'UbX'ci hg]XY'h\Y'WUggfcca ž ZWfjcbU``UbX'bcb!ZWfjcbU'`hYl hgcdfcj]XY'ghi XYbhg'k]h\'j Uf]YX'cddcfh b]hj\Yg'hc'dfUwfjW''h\Y]f'fYW'dhj Y'UbX dfcXi Wfj Y'g_]``gž'Ug'k Y``Ug'h\Y]f'j cWUVi `UfmUbX'VUg]W; Yfa Ub'[fUa a Uf"'K Y'YbWci fU[Y'ghi XYbhg'hc Yl dUbX'h\Y]f'fYdYffc]fY'cZgi]hUVY`Ub[i U[Y'`YUfb]b['gffUhY[]YgžUbX'hc']bXYdYbXYbhmdfUwfjW''cfffy]gY h\Y]f'; Yfa Ub'g_]``g'cb'U'fY[i `Uf'VUg]gž']bg]XY'UbX`VYmcbX'h\Y'WUggfcca "'H\Y'`Ub[i U[Y'cZ]bghfi Wfjcb']g dfYXca]bUbhm; Yfa Ub'fUdUfhZca 'gca Y'Yl d'UbUhjcb'cZ[fUa a UhjWD'ZYUh fYgb'gc'h\Uhghi XYbhg'XYj Y'cd h\Y]f'`]ghYb]b['g_]``g''-&'Vch\``YWfi fY'UbX'h fcffga U``'[fci d'k cf_z']bX]j [Xi U``Ugg][ba YbhgE'hc'dfcj]XY'Yl hYbg]j Y'UbX a cfY'\c']ghfWcddcfh b]hjYg'hc '`]ghYb'b'hc'zfgdYU_'UbX'k f]hY']b'; Yfa Ub''

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: YYXVUW_j]U'a Uf_YX'hYghdUdYfg'UbX']b!WUgg'X]gW gg]cb'cZ'Wca a cb'a]grU_Yg"'

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: YYXVUW_cb^YUWX^dUfhj]U^a Uf_]b[fi Vf]Wk]h\^]bX]j]Xi U^Wca a Ybhg"

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: YYXVUW_j]U'Ui hca Uh]WWcffYWh]cb'Ug'k Y``'Ug']bX]j]Xi U``Wca a Ybhg'UbX'gUa d'Y'Ubgk Yfg"

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5 hm/b XUb WY F Yei]fYa Ybhg

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\ci fg'UfY', .\$\$Ua '-'%\$.\$\$da 'cb'k YY_XUmg'UbX'-.\$\$Ua '-').\$\$da 'cb'k YY_YbXg'fl *) 'XUmg'U'mYUft"'=Z'mci
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a i ghfYhJ]b'mci f'h]W_Yhbi a VYf'Zfca '9| hy'fbu''Gi ddcfhfU'cb['k]h\ 'Ubmch\Yf'fy'Yj UbhXcW a Ybhgthc
]bWi XY'Ug'Yj]XYbW'hc'gi ddcfhmci f'Yl hy'bg]cb'Udd']WUh]cb"'=Zmci 'Ya U]''9| hy'fbu''Gi ddcfhmci 'k]'`
Ui hca Uh]WJ'`mfYW']j Y'U'h]W_Yhbi a VYfZ'Vi h]Zmci 'hy'Yd\cby'mci 'k]``bYYX'hc'gdYW]Z]WJ'`mUg_'Zcf'cby''
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; YbYfU`mž'UggYgga YbhiHug_g'a i ghVY'gi Va]hhYX'Y`YVWfcb]\WJ``mij]U'Y]h\Yf'Hi fb]h]b'cf'U'A ccX`Y Ugg][ba Ybh''=b']bgHJb\W'g'k \YfY'h\]g']g'bchdcgg]V`Yž']hk]```VY'gHJhYX'cb'mci f'\\circ i fgY'g'A ccX`Y'g]hY'k]h\U`hYfbUh]j Y'gi Va]gg]cb'XYHJ]`g"

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5 WUXYa]W<cbYghmUbX D`U[]Uf]ga

D`U[]Uf]ga i]gii g]b[ih\Yik cfXgicfi]XYUgicZch\YfgiUbXidfYgYbh]b[ih\Ya iUgimci fick b"i=hWJbihU_Yia Ubm Zcfa gžZfca iXYi]VYfUhYiWXYUh]b[ihciUWW]XYbhU`mWcdm]b[iZfca iUigci fWYik]h\ci hiUW_bck iYX[Ya Ybh'

IBGK [fcidg'd'U[]Uf]ga]bhc'h\Y'Zc``ck]b['WUhY[cf]Yg.

- i bXYfgfUbX mci f'f][\hg'UbX'fYgdcbg]V]`]hJYg'Ug'U'gh XYbhUhl BGK
- VY`Uk UfY`cZd`U[]Uf]ga ž`Wcdmf][\hz'l BGK `Gh XYbh7cXY`cZ7cbXi WhUbX`5VWWdhUV`Y`l gY`cZ I BGK `=\forall H`F Ygci f\W\g`Dc`]\m\m
- VY 'Uk UfY 'cZh\Y 'ghUbXUfXg 'cZVY\Uj]ci f'Yl dYWYX 'cZYj YfmcbY ']b 'h\Y 'l BGK 'Wca a i b]hm
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Gca Y'cZh\YgY'UfYUg'k]``VY'ZJa]`]Uf'hc'mci ž'ch\Yfg'k]``VY'bYk"'; U]b]b['U'gc`]X'i bXYfgHJbX]b['cZU``h\YfY`UhYX'UgdYWng'cZ9@+69'k]``\Y`d'mci 'a U_Y'h\Y'a cghicZmci f'ghi X]Yg'UhI BGK "'\\hd.##qi VYWfi |XYg"`]VfUfm'i bqk "YXi "Ui #\`]qY#JVci hY`]qY

5 WUXYa]W = b Zcfa Uh cb

: cf'YggYbhJU`'gh XYbh']bZcfa UhJcb'fY`UhJb['hc.

- fYei Yghg 'Zcf'Yl hYbg]cb/
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- I BGK '< YU'h\ 'UbX'GUZYhm'dc`]\\\Yg/
- YI Ua]bUhcb dfcWXi fYg/
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