

# **IEST5012**

9bj ]fcba YbhJ``A UbU[ Ya Ybh'Dfc YWh'DUdYf

HYfa 'H\fYY''##'&\$&\$

## 7ci fgY'Cj Yfj ]Yk

## GHJZ7cbHJWh8YHJ]`g

### 7cbj Ybcfg

B Ua Y	9a U]`	5j U]`UV]`] <b>m</b>	@cWUh]cb	D∖cbY
HYa U'A ]`ghY]b	hYa U"a ]`ghY]b4 i bgk "YXi "Ui	6miUddc]bha Ybh	A cfj Yb <sup>.</sup> 6fck b	
		Xif]b['Wcbgi`HUH]cb	' *( 'fbf'cb`]bY	
		\ci fg	j]U'HYUa g'Xi Y	
		fK YXbYgXUmgž'‱	hc:X]ghUbWY	
		U"a "`!`%&`d"a "Ł	`YUfb]b[ 'cf	
			7 cj ]XŁ	

## GWXcc`7cbHJWhi±bZcfa Uh]cb

GWkcc``cZ<iaUb]h]Yg'UbX'@Ub[iU[Yg

@c\\U||cb. G\\cc``C\\Z|\\\žA\cfj\Yb'6fck\b'6i]\X]b[\z'@\j\Y``&z'&),

CdYb]b[ '<ci fg. 'A cbXUm!': f]XUmž'- Ua '!') da

D\cbY.'Ž\*%'&'-',)'%\*,%

: UI . Ž\*%'&'-',) ', +\$)

9a U]`. \<u>U`4 i bgk "YXi "Ui</u>

## 7ci fgY 8YHJ] g

### 7 fYX]hDc]bhg '%'

### Gi a a UfmcZh\Y 7ci fgY

H\Y`[cU``cZh\]g`Wci fgY`]g`hc`YbUV`Y`gh XYbhg`hc`k f]hY`U`gi dYfj ]gYX`Ybj ]fcba YbhU``a UbU[Ya YbhfYgYUfW\dUdYf"'H\]g`fYgYUfW\`Wci `Xž`Vi hXcYg`bch\Uj Y`hc`VYž`VUgYX`cb`a UhYf]U``[Uh\YfYX`Xi f]b[``h\Y 9bj ]fcba YbhU``A UbU[Ya YbhF YgYUfW\`\DhYfbg\]d`f\DGH) \$\$(\E''`H\Y`Wci fgY`XcYg`bcha U]bhU]b`fY[i `Uf`m gW\YXi `YX`WUggYg'''< ck Yj Yfžghi XYbhg`UfY`fYei ]fYX`hc`dUff]W]dUhY`]b`cfU``dfYgYbhUh]cbg`cb`h\Y`dfc^YWh dUdYfg`hck UfX`h\Y`YbX`cZh\Y`hYfa "'H\fci [\ci hh\Y`hYfa `cZh\Y`dfc^YWbzghi XYbhg`k ]```VY`k cf\_]b[`k]h\`cbY cf`a cfY`a i h`U``mU[fYYX`i dcb`UWUXYa ]Wgi dYfj ]gcfg`k \c`k]```fYj ]Yk `dfc[fYgg`hck UfX`h\Y`]bU``dfc^YWh dUdYf`XcW`a Ybh''H\]g`Wci fgY`]g`Uj U]`UV`Y`VmX]ghUbWY`ghi Xm'

### 7 ci fgY @YUfb]b[ Ci hWca Yg

%" 5dd`mfYgYUfW\`a UbU[Ya Ybhg\_]``g`hc`Ub`cf][]bU``fYgYUfW\`dfcYWf' &" 5bU`mgY`UbX`]bHYfdfYhfYgYUfW\`XUHU" ' " 7 ca a i b]\\UhY`fYgYUfW\`Z|bX]b[q`]b`k f]\thYb`UbX`cfU``Zcfa Uhg"

#### HYUW ]b[ GhfUhY[ ]Ya

H\]g`Wci fgY`U]a g`fc`YbUV`Y`ghi XYbhg'`]b!XYdh\`UbX`cf][]bU``fYgYUfW\`f\fci [\`f\Y`k f]h]b[`cZU`fYgYUfW\\dUdYf`i bXYf`h\Y`gi dYfj ]g]cb`cZcbY`cf`a cfY`a i hi U``mU[fYYX`i dcb`UWUXYa ]Wgi dYfj ]gcfg`k \c`k]``gi ddcfhih\Y`XYj Y`cda YbhcZh\Y`Z]bU``dfc`YWhdUdYf`XcW a Ybh'`H\Y`X]fYWhYX`gi dYfj ]g]cb`ghfUhY[m]b`f\Y Wci fgY`U]a g`fc`XYj Y`cd`fYgYUfW\`g\_]``g`UbX`a Yf\cXgž'hYUa k cf\_'UbX``]U]gcb`k]h\`U`dUffbYf`cf[Ub]gUh]cbfk\YfY`fY`Yj UbHžUbX`fYgYUfW\`dfYgYbhUh]cb`g\_]``g"`H\]g`Wci fgY`]g`Uj U]`UV`Y`VmX]ghUbW\`ghi Xm]b`k\]Wqi XYbhg`UfY`qi dYfj ]qYX`X]fYWhmVmUb`UWUXYa ]Wqi dYfj ]qcf"

## 5ggYgga Ybh

H\]gʻdfc YWifYei ]fYgʻ]b]hJuhj YʻubXʻgYʻZX]fYWYXʻYUfb]b[ ʻcbʻh\YʻdufficZh\Yʻghi XYbh]bʻWcbgi `huhjcbʻk ]h\
h\Y]fʻWkcgYbʻUbXʻU[ fYYXʻi dcbʻUWUXYa ]WghUZgi dYfj ]gcfʻZcfʻh\Yʻdfc YWiʻ5ggYgga YbhYl dYWiUhjcbgʻUfY
k cf\_YXʻci hUhih\YʻghUfficZh\YʻhYfa ʻcbY!cb!cbY`VYhk YYbʻh\Yʻghi XYbhUbXʻh\Y]fʻgi dYfj ]gcfʻ'K YʻfYWca a YbX
h\Yʻghi XYbhWcbhUWiʻ9bj ]fcba YbhUbXʻGcWjYhm; fci dʻUWUXYa ]Whc`VYʻdchYbhJUʻ`gi dYfj ]gcfgʻk \c`]gʻUʻ[ ccX
ZhZcfʻh\YʻgdYWZW\_]bX`UbXʻZcW gʻcZfYgYUfW\`h\Yʻghi XYbhk Ubhgʻhcʻi bXYfhU\_Y''

#### 5ggYgga Ybh'HUg\_g'

5ggYgga Ybh'hJg_	K Y][ \h	8i Y'8UHY	Gh XYbh@YUfb]b[ Ci hWca Ygʻ5ggYggYX
Dfc YWn6f]YZ	%\$I	Bch5dd`]WUV`Y	%ž&
C fU``DfYgYblUljcb`	' \$1	Bch5dd`]WUV`Y	% <u>ž&amp;</u> Ž
: ]bU`fYdcfh	* \$1	Bch5dd`]WUV`Y	% <u>ž&amp;</u> Ž

### 5ggYgga Ybh'8YhJ]`g

5ggYgga Ybh% Dfc YWh6f]YZ

GhUfhXUhY. Bch5dd`]WUV`Y

8YHJ]`g.

5') \$\$!k cfX'Vf]YZk \]W\`]bWi XYg`U`VUg]Wci h]bY`cZh\Y`Ufh]WY`rc`VY`XYj Y`cdYXžrh\Y`dchYbh]U``&i fbU`fgŁ`Zcf]hhc`VY`gi Va ]hhYXžrh\Y`h]a Y`]bY`Zcf`XUhU`UbU`mg]g`UbX`k f]h]b[ žXYhU]`g`cZk cf\_`gh]``hc`VY`W&bXi WhYX" \
\(\pi\X)] ]Xi U``k f]hhYb`ZYYXVUW\_`dfcj ]XYX"

#### 5XX]h]cbU`XYhU]`g.

 $\label{thm:condition} Dfc \Upsilon WhiXYhU] \ ghc `VY'k cf_YX'ci hcbY!cb!cbY'VYhk YYb'h\Y'ghi XYbhUbX'h\Y]f'U[fYYX!i dcb'UWUXYa] WghUZZ gi dYfj ]gcf''$ 

5qqYqqa Ybh'& 'CfU' DfYqYbhUhlcb

GhUfhXUhY. Bch5dd`]WUV`Y

8YW]`q.

±X]j ]Xi U``%) !a ]bi hY`cfU``dfYgYbhUh]cb`cZfYgYUfW\`dfcYWh'`±b!WUgg`ZYYXVUW\_`dfcj ]XYX"

#### 5XX]h]cbU`XYhJ]`g.

8 YHJ]`g`hc`VY`k cf\_YX`ci hcbY!cb!cbY`VYhk YYb`h\Y`gh XYbh'UbX`h\Y]f`U[fYYX!i dcb`UWUXYa]WgHUZ gi dYfj ]gcf"

## 5 https://bxubwww.Fyei]fYaYbhg

 $\hbox{Ghi XYbhg'UfY'ghfcb[`m'YbWc'i fU[YX'hc'UhhYbX'U```WUggYg'UbX'fYj]Yk'``YWhfY'fY'WcfX]b[g''' } \\$ 

## 7ci fgY GWX YXi `Y

## J]Yk 'WUgg'hja YHUV'Y

## H]a YtUV`Y

8 UHY	HmdY	7 cbhYbh
C'K YY', 'GYdhYa VYf'!'- GYdhYa VYf		5 k YY_`mgW.YXi `Y`]gʻbchdfcj ]XYX`\YfY"'8i f]b[ 'cf VYZcfY'h\Y`Z]fghk YY_'cZHYfa ž'h\Y'gWcdY'cZh\Y dfc^YWibYYXgʻhc`VY`XYhYfa ]bYX`VYhk YYbʻmci 'UbX mci f`U[ fYYX`i dcb`UWUXYa ]WghUZZgi dYfj ]gcf"'5`` ch\Yf`gW.YXi `]b[ 'UbX`fYei ]fYa YbhgʻZck 'Zfca 'h\]g YUf`mYghUV`]g\a YbhcZh\Y'dfc^YWf

## Fygci fWyg

## DfYgWf]VYX F Ygci fWYg

 $\label{thm:continuity} Hc \ VY \ XY \ h \ fa \ ]b \ YX \ ]b \ Wc \ bgi \ \ h \ h \ mci \ f \ gi \ dY \ fj \ ]gcff \ gk$ 

## FYWca a YbXYX FYgci fWYg

 $\label{thm:continuity} \mbox{Hc\,}^{\mbox{"}}\mbox{VY\,}^{\mbox{"}}\mbox{XY\,}^{\mbox{"}}\mbox{Mc\,}^{\mbox{"}}\mbox{bgi\,}^{\mbox{"}}\mbox{Mc\,}^{\mbox{"}}\mbo$ 

## 7 ci fgY '9j U'i Uh]cb 'UbX '8 Yj Y`cda Ybh

DfYj ]ci gʻghi XYbhgʻ\Uj Yʻj Uʻi YXʻh\YʻfYgYUfVXʻdfc^YWhUgʻUbʻcddcfhi b]hmhcʻfYWY]j Yʻa Ybhcf]b[ʻ]bʻfYgYUfVX

# Gi Va ]gg]cb cZ5ggYgga YbhHUg\_g

## Hi fb]h]b Gi Va ]gg]cb

#mci 'YbWci bhYf'U'dfcV'Ya 'k \Yb'UthYa dhJb[ 'tc'gi Va ]hmci f'Ugg][ ba Ybht\fci [ \'Hi fb]hJbž'd'YUgY
hY'Yd\cbY'9| hYfbU'Gi ddcfhcb'-', ) '''' %cf'Ya U]''h\Ya 'cb'Yl hYfbU'hY'hgi ddcfh4 i bgk "YXi "Ui '"'Gi ddcfh
\ci fg'UfY', .\$\$Ua '-'%\$.\$\$da 'cb'k YY\_XUmg'UbX'-.\$\$Ua '-').\$\$da 'cb'k YY\_YbXg'fl \*) 'XUmg'U'mYUft\"'#c'i'#c'i'
UfY'i bUV'Y'hc'gi Va ]hmci f'Ugg][ ba YbhXi Y'hc'U'ZUi 'hk ]h\ 'Hi fb]hJb'mci 'a Um'Udd'm\Zcf'Ub'Yl hYbg]cb\ZVi hmci
a i ghfYhU]b'mci f'hJ\W\_Yhbi a VYf'\Zfca '9| hYfbU''Gi ddcfhfU'cb[ 'k ]h\ 'Ubmch\Yf'fY'Yj UbhXcW a Ybhgthc
]bWi XY'Ug'Yj ]XYbW''hc'gi ddcfhmci f'Yl hYbg]cb'Udd']\WUh]cb'''#c''' Zmci 'Ya U]''9| hYfbU''Gi ddcfhmci 'k ]'`

## 5 WUXYa ]W<cbYghmUbX D`U[]Uf]ga

D`U[]Uf]ga i]gii g]b[ih\Yik cfXgicfi]XYUgicZch\YfgiUbXidfYgYbh]b[ih\Ya iUgimci fick b"i=iWUbihU\_Yia Ubm Zcfa gžZfca iXYi]VYfUhYiWXYUh]b[ihciUWW]XYbhU`mWcdm]b[iZfca iUigci fWYik]h\ci hiUW\_bck iYX[Ya Ybh'i

- i bXYfgHUbX'mci f'f][\hg'UbX'fYgdcbg]V]`]h]Yg'Ug'U'gh XYbhUhI BGK
   VY'Uk UfY'cZd`U[]Uf]ga ž'Wcdmf][\hz'I BGK 'Gh XYbh7cXY'cZ7cbXi WhUbX'5VWWdhUV`Y'I gY'cZ IBGK =7 HF Ygci fWrg Dc`]Wh