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Gi a a UfmcZh\Y'7ci fgY

H\]gʻgʻi VYWitU_YgʻUbʻ]bh/fbUhjcbUʻdYfgdYWij YʻcbʻYVcʻc[]WUʻʻUbXʻgcWJUʻ]bYei]hmUbXʻchXff[ʻcVUʻ WkUʻYb[YgžZcWig]b[ʻcbʻcb[c]b[ʻ]a dUWgʻcZVcʻcb]gUhjcbž'hXʻfcʻYʻcZYbj]fcbaYbhUʻWcbjYbhjcbgʻUbXʻhfUXY fi YgžUbXʻhXYʻ]a dUWicZ[ʻcVUʻ`[cjYfbUbWfghfUhY[]Ygʻgi WkUgʻhXʻ"gi ghU]bUVʻYʻXYjYʻcdaYbh[cUʻgʻ"i'H\]g Wci fgYʻk]``VYʻcZdUfhjWi`Uf`]bh/fYgh]Zmci 'UfY`WcbWfbYXʻk]h\`]ggi YgʻcZ[`cVU``]bYei U`]mžYbj]fcbaYbhUʻ ^ghJWfžUbXʻhXYfcʻYgʻcZhXYʻghUhYʻUbXʻWj]`jgcWYhmʻ =bʻh\]gʻWci fgYžmci 'k]``YI d`cfYʻhXYYbj]fcbaYbhUʻ %ghJWfžUbXʻhXYfcʻYgʻcZhXYʻghUhYʻUbXʻWj]`jgcWYhmʻ =bʻh\]gʻWci fgYžmci 'k]``YI d`cfYʻhXYYbj]fcbaYbhUʻ WkU`Yb[YgʻhUhZJWFhXYʻ; `cVU`Gci h\"`UbXʻYb[U[Yʻ]bʻUʻdfcXiWijYVWjhjei YʻcZbYc`]VYfU`a cXYʻgʻcZ YVcbca]W[fck h`UbX`XYjY`cdaYbhi\Uhi bXYf]YʻhXgY`WkU`Yb[Ygʻ'H\Y'Wci fgY`dfcj]XYgʻmci 'k]h`Ub i bXYfgHUbX]b[`cZhXY`\]ghcf]WUʻždc`]nJWUʻžUbX`]bh/fbUhjcbU``WcbhYI hgʻk]h\]bʻk`]Wk`]ggi YgʻcZYbj]fcbaYbh UbXʻ"XYjYcdaYbh'`UfY`ZfUaYXž[cjYfbYXžUbX`f]bʻgcaY`WUgYgE'UXXfYggYX''Mci 'k]``Wcbg]XYfʻh`YʻgcWJU` UbX`Ybj]fcbaYbhU`]a dUWgʻUbX`]a d`]WUhjcbgʻcZ[`cVU`j`JU`i YʻWkU]bgʻUbX`dfcXi WijcbʻbYhk cf_gžUgʻkY``Ug YZcfhgʻhc`i bXYfhU_Y`a`cfY'h`]WU``UbX`gi ghU]bUVY`UddfcUWXYgʻ'Nci 'k]``Yb[U[Y`]b`WJgY`gh X]YgʻUbX`YUfb UVci hUdd`]YXždfUWijWUžUbX`fYZYI]jY`UddfcUWXYgʻZcf`UXXfYgg]b[`[`cVU``m]bh/f]b_YX`]ggi YgʻZJWjb[`h`Y "; `cVU``Gci h\z"cf``aUcf]hmk cfX'''

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- %" 5dd`mW]h]WU``h\]b_]b[`hc`WcfY`WcbW/dhg`fY`Yj Ubhhc`Ya Yf[]b[`[`cVU``Ybj]fcba YbhU``]ggi Yg`UbX W.U``Yb[Yg
- &" 9I d`U]b`YI hYfbU``dc`]hJWU``YWcbca]W]bZi YbWYg`cb`h\Y`; `cVU``Gci h\#a U'cf]hmik cfXž'UbX`\ck `h\YgY]bZi YbWY`'gi ghU]bUVY`XYj Y`cda Ybh'hmdY`W\U``Yb[`Yg`UbX`]bYei]hJYg
- ' " 9I d`cfY`UbX`UggYgg`h\Y`i gY`cZ[`cVU`žYWcbca]Wž`Y[U`žUbX`]bgh]hi h]cbU``ZfUa Yk cf_g`Zcf UXXfYgg]b[`Ybj]fcba YbhU``]ggi Yg`]b`h\Y`WcbhYI hcZU`fUb[Y`cZch\Yf`ghfi Whi fU``]bYei U`]h]Yg`UbX WLU``Yb[Yg
- ("8]gW gg'UbX'Wf]hJei Y'hXY'ZYWfj YbYgg'cZ]bgh]h hJcbU``cf'fY[i`UhcfmUddfcUWXYgža Uf_YHVUgYX UddfcUVXYgžh/W.bc`c[mhfUbgZYfž'WUdUW]hmVi]`X]b[žUbX'chXYf'UddfcUWXYg'Zcf'XYU`]b['k]h 'gi ghU]bUV`Y'XYj Y`cda Ybh'W.U``Yb[Yg
-) " I gY _bck `YX[Y cZ gi ghJ]bUV`Y XYj Y cda Ybh WX U``Yb[Yg UbX h Y dfUWf)WU``UbX`Udd`]YX`UhhYa dhg hc `fYgc`j Y h Ya `hc `UbU`mgY`U`fUb[Y cZ`cWU`ž`bUh]cbU`ž'UbX`fY[]cbU``WUgY`ghi X]Yg

HYUWX]b[GHfUHY[]Yg

H\Y`WcifgY`]g`HUi[\h]b`U`gYa]bUf`ghm`Y`k]h\`gcaY``YWhifY`WcbhYbhUbX`fY[i`Uf`VfYU_!cihg`Zcf X]gWigg]cbg#UWhjj]h]Yg"

5ggYgga Ybh

8YHJ]YX'Ugg][ba Ybh]bZcfa Uh]cb'k]``VY'dfcj]XYX']b'Ub'Ugg][ba Ybhg\YYh]b'a ccX`Y"'8i Y'hc'7CJ =8!% gca Y'W\Ub[Yg'hc'h\Y'dfYgYbHJh]cb'a UmVY'fYei]fYX"

: cf'U```Ugg][ba Ybłg'< Ufj UfX'cf'5D5']b!hYl hfYZYfYbW]b[']g'dfYZYffYXžk]h\'U'Z ```fYZYfYbWf`]ghUhh\Y'YbX'cZ mci f'Ugg][ba Ybłg'fcb`mfYZYfYbWf'h\Y'k cf_g'h\Uhmci 'i gY'UbX'W]hY'':5`k Umg']bWi XY'U'W]tUh]cb'k \Yb'i g]b[gca YcbY'Y`gYfg'k cf_'k \Yh\Yf']h]g'U'dUdYfž'Vcc_ž'fYdcfhcf'k YVg]hY'': U]`]b['hc`\Uj Y'W]tUh]cbg']g Wcbg]XYfYX'd`U[]Uf]ga "': cf'h\Y'dfYgYbfUh]cbž'd`YUgY'\Uj Y'ga U```]b!hYl hfYZYfYbWfg'k \Yb'mci 'i gY'ch\Yfg k cf_'X]fYWfmž'UbX'U'g]b['Y'g']XY'WcbfU]b]b['mci f'X]fYWfmi gYX'fYZYfYbWfg'Uhh\Y'YbX''

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ŧbX]j]XiU`g\cfhYggUm"

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A U′cf`fYgYUfW\`fYdcfhUbX`WUgY`ghi Xmcb`gdYW]Z]Whcd]WfgŁWcj YfYX"`⊕X]j]Xi U``k f]hhYb`ZYYXVUW_`dfcj]XYX" 5ddfcl '' \$\$\$`k cfXg"`H\]g`]g`h\Y`Z]bU``UggYgga YbhZcf`UhhYbXUbWY`di fdcgYg"

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: i fh\Yf`]bZcfa Uh]cb`]g`dfcj]XYX`]b`h\Y`Ugg][ba Ybhg\YYh`]b`a ccX`Y"

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5 HrYbXUbWY F Yei]fYa Ybhg

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K YY_`%`%) : YVfi Ufm!`%- : YVfi Ufm	GYa]bUf	H\Y`Wci fgY`fi bg`]b`]bhYbg]j Y`a cXY`Zfca``%\$Ua !) da cb`A cbXUmg`UbX`Hi YgXUmg`]b`k YY_g`%I`ž`k]h`U`% \ci f`VfYU_`Zcf``i bW\`Zfca``%'da`YUV\`XUmUbX`g\ci VfYU_g`Yj Yfm\ci f"`H\Y`Wci fgY`]g`gW\YXi`YX`Zcf WUggYg`cb`]bY`]b`6`UW_VcUfX`7 c``UVcfUhY`fh\fci [\ a ccX`YE`5B8`ZJVW!hc!ZJVW`g]a i `hUbYci g`m'`;]j Yb h\Y`fYWYbh7CJ =8`ci hVfYU_žih\Y`ZJVW!hc!ZJVW WUggYg`UfY`i b`]_Y`m'`=b`h\Y`Yj Ybhih\]g`V\Ub[Ygžih\` fcca g`k ci `X`VY.		
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K YY_`&`&&`: YVfi Ufm!`&* : YVfi Ufm		H\Y`WcifgY`fibg`]b`]bHYbg]j Y`acXY`Zfca`%\$Ua!) da cb`AcbXUmg`UbX`HiYgXUmg`]b`kYY_g`%I'žk]H\`U`% \cif`VfYU_`Zcf``ibW\`Zfca`%da`YUW\`XUmUbX`g\cfh VfYU_g`YjYfm`\cif"`H\Y`WcifgY`]g`gW\YXi`YX`Zcf WUggYg`cb`]bY`]b`6`UW_VcUfX`7c``UVcfUHY`ff\fci[\ accX`YE`5B8`ZJWY!hc!ZJWY`g]ai`HUbYcig`m'`;]jYb H\Y`fYWYbh7CJ=8`ciHVfYU_ž'H\Y`ZJWY!hc!ZJWY WUggYg`UfY`ib`]_Y`m'``=b`H\Y`YjYbhH\]g`W\Ub[Ygž'H\Y fccag`kci`X`VY.		
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K YY_''%A UfVX'!') A UfVX	GYa]bUf	H\Y`WcifgY`fibg`]b`]bHYbg]jYacXY`Zfca`%\$Ua!)da cb`AcbXUmg`UbX`HiYgXUmg`]b`kYY_g`%'žk]h\`U`% \cif`VfYU_`Zcf``ibW\`Zfca`%da`YUW\`XUmUbX`g\cfh VfYU_g`YjYfm\cif"`H\Y`WcifgY`]g`gW\YXi`YX`Zcf WUggYg`cb`]bY`]b`6`UW_VcUfX`7c``UVcfUHY`fh\fci[\		

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H\YfY`UfY`bc`fYei]fYX`hYI hg`Zcf`ghiXYbhg"`FYUX]b[g`k]``VY`gYhZcf`YUWX`acXi`Y`h\fci[\`@Y[Ubhc`]b AccX`Y"`Mci`k]``VY`UV`Y`hc`UWWYgg`h\YgY`fYUX]b[g`h\fci[\`h\Y`IBGK```]VfUfmik]h\`mcif``c[]b"

FYWca a YbXYX FYgci fWYg

Gca Yʻi gYZ ``hYI hgža cghicZk \]WX WUb VY Zci bX`]bʻI BGK ``]VfUfmž']bWi XY.

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DYYhžF "žFcVV]bgžD"ž/ K UhłgžA "fPXg"Ł"f&\$%\$Ł"9 aTS^ba (f[US^WUa aYk"Fci hYX[Yž@cbXcb"

 $\label{eq:linear} DYYhzF"zZ"K UhhgZA""f&$$(L">[TWdSf[a`Wda'aY[We, Wh[da`_WfFVWhWab_WfFeu][S^_ahW_Wfe"]FcihYX[Yz'@cbXcb"]$

? ch\Uf]ž5"žGU``Y\ž5"ž9gWcVUfž5"ž8YaUf]Už: "ž/ `5WcgHJž5"`f9Xg"Ł"`f&\$% Ł"`B`gdhWdeW 3 baefŽ VWhWab_W fV[Uf[a`Sdk"`Hi`]_U`6cc_g`UbX`5i h\cfgi dZfcbH`9!jYfg]cb`<u>\YfY</u>

8f5`]gUž; "ž8Ya Uf]Už: "ž/ ?U``]gž; "f19Xg"Ł"f&\$%(Ł"6WYdai fZ, ShaUSTg/Sdk XadS`W/WdS"FcihYX[Yž @cbXcb"

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D`U[]Uf]ga `]g`i g]b[`h\Y`k cfXg`cf`]XYUg`cZch\Yfg`UbX`dfYgYbh]b[`h\Ya `Ug`mci f`ck b"`=h`WUb`hU_Y`a Ubm Zcfa gžZfca `XY`]VYfUhY`W\YUh]b[`hc`UVW]XYbhU``mWcdm]b[`Zfca `U`gci fWY`k]h\ci hUW_bck `YX[Ya Ybh'

- i bXYfgHJbX*mci f*f][\hg*UbX*fYgdcbg]V]`]h]Yg*Ug*U*ghi XYbh*Uhil BGK
- VY 'Uk UfY 'cZd'U[]Uf]ga ž Wcdmf][\hzi I BGK 'Ghi XYbhi7 cXY 'cZ7 cbXi WhubX '5 WW dhuV Y I gY 'cZ I BGK '=7 H F Ygci fW g'Dc']Wh
- VY Uk UfY cZh Y gHUbXUfXg cZVY Uj]ci f YI dYWHYX cZYj YfmcbY]b h Y I BGK Wea a i b]m
- `cWUHY'gYfj]WYg'UbX']bZcfa UHjcb'UVci hI BGK 'UbX'I BGK '@]VfUfm

Gca Y'cZh\YgY'UfYUg'k]``VY'ZJa]`]Uf'hc'mci žch\Yfg'k]``VY'bYk"'; U]b]b['U'gc`]X'i bXYfgHJbX]b['cZU``'h\Y fY`UhYX'UgdYWfg'cZ9@=G9'k]``\Y`d'mci 'a U_Y'h\Y'a cghcZmci f`gh X]Yg'Uh'l BGK "' \htd.#gi VYWf[i]XYg"`]VfUfm'i bgk "YXi "Ui #Y`]gY#UVci hY`]gY

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- fYei Yghg Zcf Yl hYbg]cb/
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