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- %" 7 cbg/fi Whu Wea d`YI a cXY``cZ\i a Ub``Ub[i U[Y`]b`hYfa g`cZ\ck `]h]g`cf[Ub]gYXž\ck `]h]g`UWei]fYXž UbX`\ck `_bck `YX[Y`cZ`Ub[i U[Y`]g`di hhc`i gYž`]b`h\Y`dfcXi Whcb`UbX`Wea dfY\Ybg]cb`cZk cfXgž gYbhYbW'gž'UbX`d]YWYg`cZX]gWei fgYž'Vma cbc`]b[i U`g`UbX`V]`]b[i U``gdYU_Yfg"`
- '"9jU`iUHY`h\Y`aU^cf`UddfcUVXYg`]b`dgmVXc`]b[i]gh]Vgž]b`HYfag`cZh\Y]f`dckYf`hc`UVWcibhZcf`h\YdgmVXc`c[]VU``dfcVWggYg`ibXYf`m]b[`h\Y`dfcXiVM]cbždfcVWgg]b[`UbX`fYdfYgYbHUh]cb`cZ\iaUb``Ub[iU[Y"
- ("5ddfU]gY'U'j Uf]YhmcZYa d]f]WU``hcc`g'i gYX`VmdgmWkc`]b[i]ghg'hc'ghi Xm``Ub[i U[Y'UWei]g]h]cb'UbX `Ub[i U[Y'dYfZcfa UbWY"'

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H\Y'HYUW\]b['gHfUhY[]Yg']bWi XY'`YWfi fYgz'fi fcf]U`gz'WUgg'dfYgYbHJfcbgz'UbX'[fci d'X]gWi gg]cbg"'H\Y k YY_`m`YWfi fYg'UfY'X]j]XYX']bhc'fk c'dUffg"'-\(\frac{1}{2}\)fh\Y'\Z]fghdUffz'VUg]WWcbW'dfg'UbX'f\YcfYf]WU``]ggi Yg'UfY dfYgYbhYX''-\(\frac{1}{2}\)fh\Y'gYWcbX'dUffzj Uf]ci g']ggi Yg'UbX'ei Ygf]cbg'UfY'dfYgYbhYX'UbX'X]gWi ggYX']b'Ub]bhYfUWf]j Y'a UbbYf'UbX'mci 'UfY'YbWci fU[YX'hc'Wcbf]Vi hY'hc'f\YX]gWi gg]cb"'H\Y'fi hcf]U`g'dfcj]XY'f\Y cddcffi b]miZcf'Ub']b!XYdh\YI Ua]bUf]cb'cZf\YcfYf]WU`'UbX'Ya d]f]WU`']ggi Yg']b'dgmW\xc`]b[i]gf]Wg'k]h\ dUff]W'\'UffYZYfYbW''hc''\Ub[i U[Y'XYjY`cda Ybf'

ARTS2693 Term 2, 2021 published at 26-04-2021 // © University of New South Wales, 2021

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Gi Va]gg]cb bch/g. 'D`YUgY 'gYY 'A ccX`Y 'Zcf'h\Y ']bglfi Wh]cbgž'fYgci fW/gž'UbX 'a Uf_]b['Wf]hYf]U 'Zcf'h\]g UggYgga Ybh'

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; `Y]ha Ubž@'F"/ `DUdUZfU[ci ž'5"`f&\$% Ł"`FY`Uh]cbg`VYhk YYb``Ub[i U[Y`UbX`h\ci [\h':\=b`8"`FY]gVYf[`f\PX"\z': S` VTaa] aX5aY` [f\hWBekUZa^aYk"`BYk `Mcf_. `C | ZcfX`l b]| Yfq]hm'DfYqqz'dd"`) \$(!) &' "

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• i bXYfgHJbX'mci f'f][\hg'UbX'fYgdcbg]V]`]h]Yg'Ug'U'gh XYbh'Uhil BGK

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: cf'YggYbhJU`gh XYbh]bZcfa UhJcb fY`UhJb[hc.

- fYei YghgʻZcfʻYl hYbg]cb/
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- YI Ua]bUh]cb dfcW/Xi fYg/
- gdYWJU``Wcbg]XYfUHjcb']b'H\Y'Yj YbhcZ]``bYgg'cf'a]gUXj Ybh fY/
- gh XYbhYei]hmUbX'X]gUV]`]hm/
- UbX'ch\Yf'YggYbhJU`'UWUXYa]W]bZcfa UhJcbž'gYY