

IEST7600

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7ci fgY 8YHJ] g

7 fYX]hDc]bhg**

Gi a a UfmcZh\Y'7ci fgY

±0X][Ybci g'_bck `YX[Y'\c`XYfg'UfY'k cf_]b['k]h\'\ck 'hc'Uff]W\'UhY'h\Y]f'_bck `YX[Y'dfUWf]W\g'UbX'VY`]YZg'hc bcb!±0X][Ybci g'UbX'bcb!`cWU``Ui X]YbW'g"'±0'h\]g'Wci fgYžmci 'k]``ZcW g'cb'Yh\]WU``UbX'Yei]hUYY'k Umg'cZ]bhY[fUh]b['±0X][Ybci g'UbX``cWU``_bck `YX[Y'gmghYa g'k]h\'K YghYfb'gW]Ybh]Z]W_bck `YX[Y'gmghYa g'hc]bZcfa 'gi ghU]bUV]`]mmUbX'WcbgYfj Uh]cb'dc`]WmUbX'dfUWf]W\"'Mci 'k]```YUfb'UVci hUddfcdf]UhY'UbX'YZZYWf]j Y k Umg'hc'g\UfY'UbX'Wca V]bY'h\YgY'_bck `YX[Y'gmghYa g'Zcf'Wc``UVcfUh]j Y'Ybj]fcba YbhU```YUXYfg\]d"'±0'h\Y a]XghcZ[`cVU``Wf]gYgž]bWi X]b['W]a UhY'X]gfi dh]cbž``Uf[Y'gWU'Y'YI h]bWf]cbgž'UbX'YI UWYfVUhYX'Vi g\ZfYgž mci 'k]``fYh\]b_'k Umg'gcW]YhmWUb'WcbWYdh U`]gY'Ybj]fcba YbhU``dfcV`Ya g'UbX'WcbgYfj Uh]cb'dfUWf]W\g'''±0 UXX]h]cbž'mci 'k]``]bj Ygh][UhY'\ck 'hc'Vi]`X'fY[]cbU'ž'bUh]cbU`ž'UbX'[`cVU``gW]YbW''dc`]Wmh\Uh]g']bWi g]j Y'cZ g]h UhYX'±0X][Ybci g'UbX``cWU``_bck `YX[Y'gmghYa g'k]h\ci hWca dfca]g]b['h\Y']bhY[f]mmcf``Y[]h]a UWncZ gW]Ybh]ZW±±0X][Ybci gžcf``cWU``_bck `YX[Y'gmghYa g'k]h\ci hWca dfca]g]b['h\Y']bhY[f]mmcf``Y[]h]a UwncZ gW]Ybh]ZW±±0X][Ybci gžcf``cWU`_bck `YX[Y'gmghYa g''

7 ci fgY @YUfb]b[Ci hWca Yg

%" 8 YgWf]VY 'h, Y ']bhYfWcbbYWhYXbYgg cZW 'h fY 'UbX'YWc`c[m]b'+bX][Ybci g'UbX'`cWU`_bck `YX[Y gmghYa g'UbX'h, Y'dcgg]V]`]h]Yg'Zcf'Yh,]WU``]bhY[fUh]cb'k]h, 'K YghYfb'gW]Ybh]Z]W_bck `YX[Y &" 5 dd'ma i 'h]d'Y'Yj]XYbW' VUgYg'hc'h, Y'h, YcfmUbX'dfUW]WY'cZ'UbX'fYghcfUh]cb'UbX'WUfY

5ggYgga Ybh

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8YHJ]`g.

H\Y`cifbU`k]``VY`_Ydhh\fci[\cihh\Y`h\fažk]h\k\YY_`mYbhf]Yg`fbi Va]h\X`k\YY_`m—`ZYYXVUW_'j]U'j\YfVU` cf`kf]h\Yb`WcaaYbhg\"FYei]f\Yg`Wf]h]WU``UbX`dYfgcbU``Yb[U[YaYbhk]h\WcifgY`Wcbh\YbhUbX`YIdYf]Ybh]U``YUfb]b[žUbX`aUm]bWiXY`g\cfhfYZYWf]cbg`cb`U`biaVYf`cZdfY!gYheiYgh]cbg"`@Yb[h\.`&\$\$`kcfXg`dYfkYY_g`%*"

: YYXVUW_'j]U'U'fi Vf]Wz'bi a Yf]WU`a Uf_z'UbX'Wca a Ybhg"

5XX]h]cbU`XYhJ]`g.

 $H\Y'\cite{thmoments} H\Y'\cite{thmoments} H\X'\Cite{thmoments} H\X'\C$

 $$$ > ci fbU`g`Zcf`gi VgYei Ybh`k YY_g`k]```VY`VUgYX`cb`mci f`ck b``YUfb]b[`fYZYWf]cbg`fWf]hYf]U`UbX`[i]XUbW dfcj]XYX`]b`WUgg`k YY_'%±ž'i b`Ygg`ch\Yf`gdYW]Z]WhUg_g`UfY`gYh'$

Gi Va]gg]cb bchYg. Gi Va]hh\fci [\accxy^]b_cb: f]XUmZcfYUVX cZk YY_g'%!*"

Hi fb]h]b gYh]b[. H\]g]g bchU Hi fb]h]b Ugg][ba Ybh

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@Yb[h\.'\%\\$\!\(\\$\k\cfXg\fbch]b\\\\X]b[\fY\Z\fYb\\\\'\]ght

8YHJ]`g.

: YYXVUW_'k]``VY'[]j Yb']b'h\Y'Zcfa 'cZU'fi Vf]Wf]bWi X]b['h\Y'\i fX`Y'HUg_gŁž'bi a Yf]WU``a Uf_ž'UbX Wca a Ybhg"

5XX]h]cbU`XYhU]`g.

<i fX`Y`Ugg][ba Ybhg`k]``VY`gYhZcf`k YY_g`&!('UbX`dfcj]XYX`cb`a ccX`Y"</pre>

9ggUmiWf]hYf]U^UbX^[i]XUbWY^k]```VY^dfcj]XYX^]b^WUgg^]b^k YY__%fbi Va]gg]cb^XUhY^Zcf^YggUmi]g^>i `m% Ł"

Gi Va]gg]cb bchYg. Gi Va]hh\fci [\accx\Y\]b_

Hi fb]hb gYhb[. H\]g]g bchU Hi fb]hb Ugg][ba Ybh

5ggYgga Ybh' . FYZYWjcb

GhUfhXUhY. Bch5dd`]WUV`Y

@Yb[h\.'&\$\$\$'kcfXg'fbch']bWiX]b['fYZYfYbWY'`]ghŁ

8YW]`q.

H\Y`Z|bU``UggYgga YbhfUVci hi&\$\$\$'k cfXgŁik]```VY`U`fYZYWfjcb`cb`k\Uh\Ug`VYYb``YUfbhžfYZfUa YX`UbX i bXYfghccX`Xi f]b[`h\Y`Wci fgY"'H\Y`UggYgga Ybhk]```]bWi XY`U`k f]hfYb`hUg_`fUggYggYX`Vmi b]j Yfg]hm UWUXYa]WgŁ'UbX`h\Y`ch\Yf`Wca dcbYbhg`cZh\Y`UggYgga Ybhk]```VY`VUgYX`cb`XYa cbghfUh]cb`cZ i bXYfghUbX]b[`]b`h\Y`Z|Y`X"'H\Y``cWI`_bck`YX[Y`Ui h\cf]h]Yg`k\c`\cghh\Y`Z|Y`X'hf]d`k]``Wc!XYg][b'h\]g UgdYWficZh\Y``YUfb]b[`hUg_`UbX`VY`Wc!UggYggcfg`cZWca dYhYbWf#YUfb]b[`ci hWca Yg"

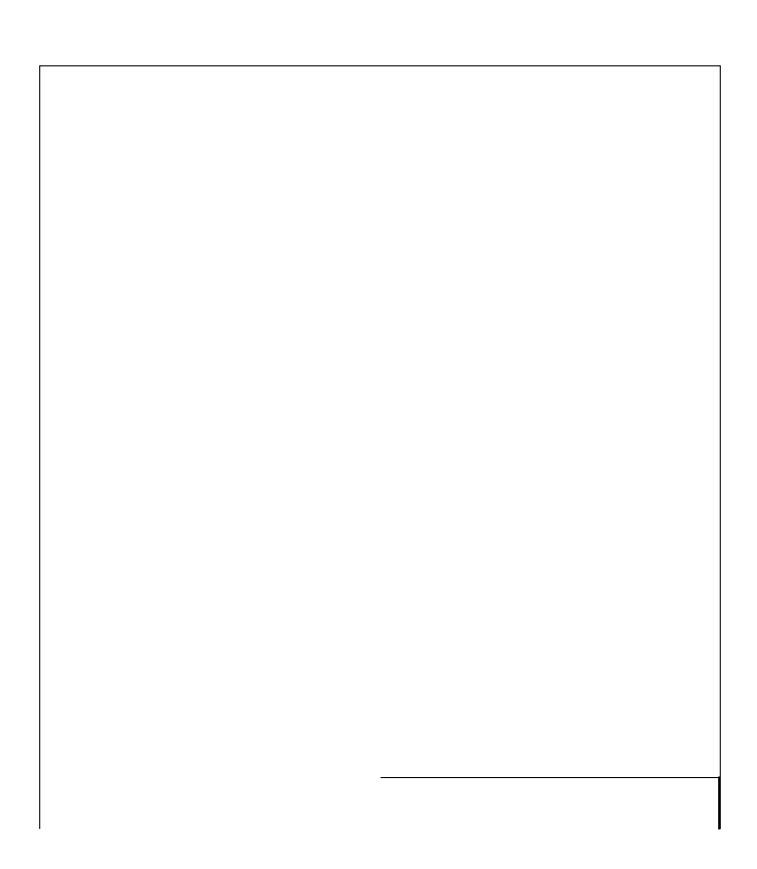
: YYXVUW_'j]U'U'fi Vf]Wžbi a Yf]WU`a Uf_žUbX'Wca a Ybhg"

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 $H\Y'Z]bU``k f]hYb'fYZYWf]cb'fa Uf_YX'VmWci fgY'Wcbj YbcfgŁ'k]``VY'ci h]bYX'Xi f]b['WUgg']b'k YY_'%UbX']g Xi Y'YbX'cZhYfa 'fl f]XUm5i [i gh'*h\z'k YY_'%$Ł''$

Gi Va]gg]cb bch/g. Gi Va]hZ|bU`k f]hh/b fYZYWh]cb h\fci [\``]b_'cb a ccX`Y"

 $\label{eq:higher_problem} \mbox{Hi fb]h]b "gYhh]b[. "H\]g"]g"bch"U"Hi fb]h]b"Ugg][\mbox{ba Ybh}$



Xi Y	"Ugh'XUm'c ZhYfa	fl f]XUm5i	[igh*t"
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DfYgWf]VYX F Ygci fWYg

5 W fUhYX 'gYhcZa UbXUhcfmfYgci fWg'k]``VY 'Uj U]`UV`Y h\fci [\@Y[Ubhc'UbX'cb'h\Y'Wci fgY'a ccX`Y'g]hY Zcf'h\Y'ghUfhcZhYfa "

H\YfY`]g`U`j UghUffUmcZ`]hYfUhi fY`UbX`k YV]bUfgž'dcXWUghg`YhWzh\Uhi]bZcfa `h\]g`Wci fgY"`\\ight]g`ghfcb[`m fYWca a YbXYX`h\Uhimci `ghUfh`cc_]b[`UhifY`Yj UbhifYgci fWrg`VYZcfY`h\Y`Wci fgY`ghUfhg"`Gca Y`fYgci fWrg fUj U]`UV`Y`h\fci [\`@Y[Ubhc`UbX`Ug`YVcc_q`]b`I BGK ``]VfUfmz`hc`ghUfhk]h\`]bWi XY.

"8 Uf_'9a i "'Vm'6fi WY'DUgWcY'

~@cj]b[~7cibhfm~7\UdhYf~%fdd~%%~cb~;i~U[U/~6]UaUb[U~fdfYdUfUh]cb~Zcf~Z]Y~X~hf]dk2~&\$&\$

"Gcb[`]bYg'! 'H\Y'Dck Yf'UbX'h\Y'Dfca]gY"'VmA Uf[c'BYU`'UbX'@mbbY'? Y``m&\$&\$'

"GUWfYX 9 Wc`c[m"Vm:]f_Yh6Yf_Yg &\$\%

FYWca a YbXYX FYgci fW/g

5 ``]ghcZk]XYf'fYWca a YbXYX'fYgci fWYg'fYVcc_g']b'I BGK ``]VfUfmUbX``]b_YX'bc'@Y[UbbcŁ']bWi XYg.

"Gcb[gd]fU`g'!'g\Uf]b['k ca Ybfg'k]gXca 'cZ7ci blfmlh\fci [\'gcb[`]bYg"'Vmlh\Y'; UmfK i'; fci d'cZK ca Ybž &\$% ž'5``Yb'/ I bk]b

"H\Y'8fYUa]b['UbX'ch\Yf'YggUmg"'VmK "9"<"'GhUbbYf'

"6fU]X]b['Gk YYh[fUgg'! '₺X][Ybci g'K]gXca žGV]Ybh]Z]W? bck `YX[Y'UbX'h\Y'HYUW\]b[g'cZD`Ubhg"'VmF cV]b K U```?]a a YfYf'&\$% '! 'fYUX'd&(%'&)' "

Hkc'df]bhVcc_g'UjU]'UV'Y']b'IBGK'']VfUfm'''GUbX'HU'_'''VmHmgcb'Mb_UdcftU

7 ci fgY 9j U'i Uhcb UbX 8Yj Y'cda Ybh

 $H\ [g']g'h\ Y']bUi\ [ifU``mYUf'\ Zcf'h\]g'WcifgY''5g'k\ Y```Ug'h\ Y'am9IdYf]YbW''\ ZYYXVUW_ž'U'gifj\ Ymk\]``VYdfcj]XYX'hc'gh XYbhg'hc'Wcad'YhY'\ Zcf'\ ZYYXVUW_cb'h\ Y'\ ZY`X'hf]dg''$

Gi Va]gg]cb cZ5ggYgga YbhHUg_g

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\ci fg'UfY', .\$\$Ua '-'%\$.\$\$da 'cb'k YY_XUmg'UbX'-.\$\$Ua '-').\$\$da 'cb'k YY_YbXg'fl *) 'XUmg'U'mYUft\"'#c'i'#c'i'
UfY'i bUV'Y'hc'gi Va]hmci f'Ugg][ba YbhXi Y'hc'U'ZUi 'hk]h\ 'Hi fb]hJb'mci 'a Um'Udd'm\Zcf'Ub'Yl hYbg]cb\ZVi hmci
a i ghfYhU]b'mci f'hJ\W_Yhbi a VYf'\Zfca '9| hYfbU''Gi ddcfhfU'cb['k]h\ 'Ubmch\Yf'fY'Yj UbhXcW a Ybhgthc
]bWi XY'Ug'Yj]XYbW''hc'gi ddcfhmci f'Yl hYbg]cb'Udd']\WUh]cb'''#c''' Zmci 'Ya U]''9| hYfbU''Gi ddcfhmci 'k]'`

5 WUXYa]W<cbYghmUbX D`U[]Uf]ga

D`U[]Uf]ga i]gii g]b[ih\Yik cfXgicfi]XYUgicZch\YfgiUbXidfYgYbh]b[ih\Ya iUgimci fick b"i=iWUbihU_Yia Ubm Zcfa gžZfca iXYi]VYfUhYiWXYUh]b[ihciUWW]XYbhU`mWcdm]b[iZfca iUigci fWYik]h\ci hiUW_bck iYX[Ya Ybh'i

- i bXYfglUbX`mci f`f][\hg`UbX`fYgdcbg]V]`]h]Yg`Ug`U`gh XYbh'Uhi BGK
- VY'Uk UfY'cZd`U[]Uf]ga ž'Wcdmf][\hzil BGK 'Gh XYbh7cXY'cZ7cbXi WhUbX'5WWdhUV`Y'I gY'cZ I BGK '= H'F Ygci fWfg'Dc`]Wh
- VY 'Uk UfY 'cZh\Y 'ghUbXUfXg 'cZVY\Uj]ci f'Yl dYWhYX 'cZYj YfmcbY ']b 'h\Y 'l BGK 'Wcaaib]hm
- `cWUHY 'gYfj]WYg'UbX `]bZcfa UH]cb'UVci hI BGK 'UbX'I BGK '@]VfUfm