

ARTS1780

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5 WUXYa]W + DZcfa Uh]cb

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7ci fgY 8YHJ] g

7 fYX]hDc]bhg**

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8 YHU]`g. 'K YY_`mei Ygh]cbgʻcbʻh\YʻfYUX]b[gʻk]```\Y`dʻghi XYbhgʻXcW a Ybhh\Y]fʻfYUX]b[ʻUbXʻh\]b_]b[ʻcbʻh\Y a UhYf]U`"`Ghi XYbhgʻk]``bYYXʻhcʻgi Va]hY][\hgYhgʻcZfYgdcbgYgžYUW\cZa Ul]a i a '&) \$`k cfXgžcj Yfʻh\Y hYfa 'Wcbg]gh]b[ʻcZUʻfYgdcbgYʻhcʻcbYʻcZh\Yʻhk cʻfYUX]b[gʻcZUʻ[]j Ybʻk YY_`UbX`U`X]gW gg]cbʻei Ygh]cbʻcZ

[]j Y`gh XYbhg`h\Y`cddcfh b]hmhc`XYa cbghfUhY`h\Y]f`i bXYfghUbX]b[`cZh\Y`h\Ya Ygž`]ggi Yg`UbX`XYVUhYg Wcj YfYX`]b`h\Y`Wci fgY": YYXVUW_j]U'a Uf_]b[`fi Vf]Wg`UbX`Vf]YZWca a Ybhg

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5XX]h]cbU`XYhU]`g.

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 $\label{eq:higher} \textbf{Hi fb]hjb'gYhjb[.'H\]g'Ugg][ba Ybh']g'gi Va]hhYX'h\fci [\''Hi fb]hjb'UbX'ghi XYbhg'WUb'gYY'Hi fb]hjb'g]a]`Uf]hm fYdcfhg''$

Gi Va]gg]cb cZ5ggYgga YbhHUg_g

 $Gh\ XYbhg\ UfY\ YI\ dYWMYX\ hc\ di\ hih\ Y]f\ bUa\ Yg\ UbX\ gh\ XYbhbi\ a\ VYfg\ cb\ Yj\ YfmdU[\ Y\ cZh\ Y]f\ Ugg][\ ba\ Ybhg\ bug\ Ybhg\ bug\ Yhhg\ Yhhg\ bug\ Yhhg\ Yhhg\ bug\ Yhhg\ bug\ Yhhg\ bug\ Yhhg\ bug\ Yhhg\ bug\ Yhhg\ Yhhg\ bug\ Yhhg\ Yhhg\ bug\ Yhhg\ Yhhg\$

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Zmci 'YbWci bhYf'U'dfcV'Ya 'k \Yb'UhhYa dh]b['hc'gi Va]hmci f'Ugg][ba Ybhh\fci [\'Hi fb]h]bžd'YUgY hY'Yd\cbY'9| hYfbU''Gi ddcfhcb'-',)'''' %cf'Ya U]''h\Ya 'cb'<u>Yl hYfbU'hY`hgi ddcfh4 i bgk "YXi "Ui</u>"'Gi ddcfh ł `G][b]Z]\WbhmUZZY\Wimci f`dYfZcfa Ub\Wr`]b`UggYggUV`Y`k cf_ž`VY`]h'U`Zcfa U``YbX!cZgYa YghYf`Yl Ua]bUh]cbž`U`\WUgg`hYghž`U``UVcfUhcfmihYghž`U`gYa]bUf`dfYgYbhUh]cb`cf`Ubmch\Yf`Zcfa 'cZUggYgga Ybh'

5 WUXYa]W<cbYghmUbX D`U[]Uf]ga

D`U[]Uf]ga `]g`i g]b['h\Y`k cfXg`cf`]XYUg`cZch\Yfg`UbX`dfYgYbh]b['h\Ya `Ug`mci f`ck b"'\lefi\Wb'hU_Y`a Ubm Zcfa gžZfca `XY`]VYfUhY`W\YUh]b['hc`UVW]XYbhU`mWcdm]b['Zfca `U`gci f\W' k]h\ci hUW_bck `YX[Ya Ybh'

IBGK [fcidgdu[]uf]ga]bhch\YZc``ck]b[WuhY[cf]Yg.

7 cdm]b[.'i g]b['h\Y'gUa Y'cf'j Yfmg]a]`Uf'k cfXg'hc'h\Y'cf][]bU`hYl h'cf']XYU'k]h\ci h'UW_bck `YX[]b['h\Y gci fW'cf'i g]b['ei chUh]cb'a Uf_g"'H\]g'U`gc'Udd`]Yg'hc']a U[Ygž'Ufh'UbX'XYg][b'dfcYWhgž'Ug'k Y``'Ug dfYgYbhUh]cbg'k \YfY'gca YcbY'dfYgYbhg'Ubch\Yf'g']XYUg'cf'k cfXg'k]h\ci h'WfYX]h'

±DUddfcdf]UhY`dUfUd\fUg]b[.'W\Ub[]b['U'ZYk'kcfXg'UbX'd\fUgYg'k\]`Y`acghmfYhJ]b]b['h\Y`cf][]bU`ghfi WhifY`UbX`]bZcfaUh]cb`k]h\ci hUW_bck`YX[YaYbh'H\]g'U`gc'Udd`]Yg`]b'dfYgYbhUh]cbg'k\YfY`gcaYcbYdUfUd\fUgYg`Ubch\Yf'g`]XYUg`cf'kcfXg'k]h\ci hWfYX]h''±iU`gc'Udd`]Yg`hc'd]YW]b['hc[Yh\Yf'ei chYg'UbXdUfUd\fUgYg`]bhc'U'bYk'k\c`Yžk]h\ci hfYZ/fYbW]b['UbX'U'ghi XYbh'g`ck b'UbU`mg]g`hc'Vf]b['h\Y`aUhYf]U`hc[Yh\Yf''

7 c``i g]cb. 'k cf_]b['k]h\ 'ch\ Yfg'Vi h'dUgg]b['c\Z'h\ Y 'k cf_'Ug'U'dYfgcb'g']b\X]j]\Xi U``k cf_"'7 c``i g]cb'U`gc]b\Wi XYg'dfcj]\X]b['mci f'k cf_'hc'Ubch\ Yf'ghi XYbh\ VYZcfY'h\ Y 'Xi Y 'XUhYzcf'Zcf'h\ Y' di fdcgY'cZh\ Ya d`U[]\Uf]g]b['Uh\Ubmh]a Yz'dUm]b['Ubch\ Yf'dYfgcb'hc'dYfZcfa 'Ub'U\WUXYa]\Wh\Ug_z'ghYU']b['cf'U\\ello i]f]b[Ubch\ Yf'dYfgcb'g' U\WUXYa]\Wk cf_'Ub\X'\\ello dm]b[']hz'c\ZYf]b['hc'\\ello a d`YhY'Ubch\ Yf'dYfgcb'g' k cf_'cf'gYY_]b[d\una Ybh\Zcf'\\ello a d`Yh\beta d`

±bUddfcdf]UhY`W]hUh]cb.`7]h]b[ˈgci fW/gˈk \]WX`\Uj Y`bchVYYb`fYUXžk]h\ci hUW_bck`YX[]b[ˈh\Y`″gYWcbXUfm″gci fW/Zfca k \]WX`_bck`YX[Y`cZh\Ya`\Ug'VYYb`cVhU]bYX"

8 i d`]\WUh]cb`ff`gY`Zld`U[]\Uf]ga "Ł`gi Va]\h]b[`mci f`ck b`k cf_ž]b`k \c`Y`cf`]b`dUfhžk \YfY`]h`\Ug`dfYj]ci g`m VYYb`dfYdUfYX`cf`gi Va]\hYX`Zcf`Ubch\Yf`UqqYqqa Ybhcf\Wci fgY`UhI_BGK_`cf`Ubch\Yf`i b]\Yfq]\m"

7 cffYWhfYZYfYbWb[dfUWhWyg.

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K YY_'% .'&, 'A Um!'' >i bY	Hi hcf]U`	FYj]Yk

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5```k YY_`mfYUX]b[g'UfY']b'h\Y'Wti fgY'_]h'Uj U]`UV`Y'Zcf'di fW\UgY'UhI BGK '6cc_ghcfY"

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H\]g`Vcc_`]g`Uj`U)`UV`Y`Uhih\Y`I_B`GK_`6cc_ghcfY"'±i]g`U`gc`Uj`U)`UV`Y`Y`YWfcb]WU``mih\fci [\'ih\Y`i b]j Yfg]hm`]VfUfmiWUhU`c[i Y"

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7ci fgY 9j U`i Uh]cb UbX 8Yj Y`cda Ybh

: cfa U`ZYYXVUW_Zfca 'ghi XYbhg'k]``VY'Wt``YWhYX'j]U'a m9I dYf]YbWY'UbX'k]``VY'i gYX'hc']a dfcj Y'Z hi fY]hYfUh]cbg'cZh\]g'Wti fgY"'=bZcfa U`ZYYXVUW_]g'U'gc'j Yfmik Y`Wta Y"

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