

ARTS3220

5g]Ub'7]hjYg.'Ghi X]Yg']b'<]ghcfmž'7i `hi fY'UbX'HfUXY

GYa YghYf'C bY''##'&\$%

7 ci fgY Cj Yfj]Yk

GHJZZ7cbHJWh8YHJ]`q

'7cbj Ybcfg'

B Ua Y	9a U]`	5j U]`UV]`] m	@cWUhjcb	D\cbY
8f"AUfb]Y:YbY`Ym	a "ZYbY`Ym4 i bgk "YXi "Ui			Ž*%'&'-',) &&,-

GW.cc`7cbhJWh =bZcfa Uhlcb

GWkcc`cZ<iaUb]hYq'UbX'@Ub[iU[Yq

@cWUhjcb. 'GW\cc`'C ZZj\\xizA cfj Yb'6fck b'6i]`X]b[z'@Yj Y``&z\&),

CdYb]b[< ci fq. A cbXUm!: f]XUmž-Ua !!(.() da

D\cbY. Ž*%'&'-',) '%*, %

: UI . Ž*%'&'-',) ', +\$)

9a U]`. \<u>U`4 i bgk "YXi "Ui</u>

5 h Yb X Ub WY F Yei] f Ya Yb h g

5 qh XYbh]q Yl dYWYX hc UhYbX U``WUqq WcbhUWi\ci fq Zcf U ZUW!hc! ZUW! fl & L'cf V YbXYX Wci fqY UbX WeadYhY'U``'UWAj]hYq'Zef'U'VYbXYX'cf'Z ``micb`]bY'WeifqY"

5 gh XYbhk\c Uff]j Yg a cfY h\Ub'%) a]bi hYg `UhY a UmVY dYbU`]gYX Zcf bcb!UthYbXUbWY"'=Zgi W\ U'dYbU`hm \ci fg"

ZU gh XYbhYl dYf]YbWg]\$ Yggža]gUXj Ybh fy cf ch\yf c\ww ffYb\w h\Uha U_Yg UVgYb\w Zfca 'U WUgg#JWNj jHJ i bUjc XUV Yžcf YI dYWng hc VY UVgYbh Zfca 'U Zcfh\Wca jb [WUgg#JWnj jHJžh\Ymg\ci X gYY_ dYfa]qq]cb 7ca 'h, Y 7 ci fqY 5i h, cf]hUžUbX k \YfY 'Udd`]WUV Yž h, Y]f fYei Yghq\ci `X 'VY 'UW\called a Ub]YX 'VU'Ub cf][|bU`cf`WfHZYX`WcdmcZU'a YX]WU`WfHZWJHY`cf`ch\Yf`Zcfa `cZUddfcdf|UHY`Yj |XYbW/"

5 '7 ci fgY '5 i h\cf]hU a UmYl W gY 'U 'gh XYbhZfca 'WUggYg 'cf'UWhj]hJYg 'Zcf'i d 'hc 'cbY 'a cbh\"' < ck Yj Yfž'h\Ym a UU'Ugg][b'UXX]h]cbU``UbX#cf'U'hYfbUh]j Y'hUg_g'hc'Ybgi fY'Wca d`]UbWY"'5'7 ci fgY'5i h\cf]hU'Wcbg]XYf]b['h\Y [fUbhb[cZUVqYbW]aighVYqUhqZYXUqhXYbhk]\$ VY'UV'Y'hc'a YYhh\Y'Wti fgY'g''YUfb]b['ci h\take Yg gh|\$ UbX#cfjciaYcZYUfb]b["5ghXYbhgYY_]b['UddfcjU'hc'VY'UVgYbhZcfacfY'h\Ub'cbY'acbh\aighUdd'm]b'k f]hb['hc'h\Y'8YUb'UbX'dfcj]XY'U```cf][]bU``cf'WYfhZYX'gi ddcfhb['XcW a YbHJhcb"

cfacfy]bzcfaUt]cbUVcihthYUthYbXUbWYdfchcVc`g]bthYY:UW`tmcZ5fhgUbX'GcWJU` GWYbWrg. \htdg.#k k k "Uffig"i bak "YXi "Ui #W ffYbhah XYbha#UWJXYa \\mathbb{W}\delta Zcfa Uhcb#dfchcWc\a![i \]XY\\delta Ya#

5 WUXYa W = DZcfa Uhlcb

5ggYgga Ybh

5ggYgga YbhHUg_g

5ggYgga Ybh'hUg_	K Y][\h	8i Y'8UHY	Gh XYbh@YUfb]b[Ci hWca Yg 5ggYggYX
Dcd'Ei]n'	%) ၊	&&#\$' #&\$% `%&.\$\$`DA</td><td>%</td></tr><tr><td>FYdcfh</td><td>%) ၊</td><td>&*#\$(#&\$% `%\$.\$\$`5A</td><td>%ž&ž(</td></tr><tr><td>9ggUmiD`Ub</td><td>&\$ı</td><td>\$' #\$) #&\$% '%\$.\$\$"5A</td><td>%ž&Ž</td></tr><tr><td>9ggUmi</td><td>) \$1</td><td>%+#\$) #&\$% `\$(.\$\$`DA</td><td>%ž&Ž</td></tr></tbody></table>	

5ggYgga Ybh8YHJ]`g

5ggYgga Ybh% Dcd Ei]n

GhUfhXUhY. Bch5dd`]WUV`Y

@Yb[h\.'()a]b

8YHJ]`g. `Ghi XYbhg`Wca d`YhY`U`a i `h]d`Y`W\c]WY`ei]n`cZ(\$`ei Ygh]cbg`]b`WJ"'' \$`a]bi hYg"`Ghi XYbhg`fYWY]j Y`U a Uf_`UbX`WcffYWhUbgk Yfg"

5ggYgga Ybh& F Ydcfh

GHJfhXUhY. Bch5dd`\WJV`Y

8YHJ]`g. `Ghi XYbhg`k cf_'hc[Yh\Yf`cb`U`[fci d`fYgYUfW\`dfc`YWhUbX`dfYgYbh']hcfU``mhc`h\Y`WUgg`]b`U dfYgYbh'Jhcb`cZ%) `a]bi hYg"'Ghi XYbhg`k]```VY`a Uf_YX`]bX]j]Xi U``m''Ghi XYbhg`fYW\]j Y`U`a Uf_ž`U`fi Vf]WUbX Wca a Ybhg"'

5ggYgga Ybh' . '9ggUm'D`Ub

GhUfhXUhY. Bch5dd`]WUV`Y

8 YHJ]`g. `Ghi XYbhg`k]```XYgWf]VY`h\Y]f`YggUmiUf[i a Ybhž`ghfi Whi fY`UbX`gci fWrg`]b`Ub`YggUmid`Ub`cZ)\$\$ k cfXg"`H\Ymk]``fYWY]j Y`]bX]j]Xi U``Wca a Ybhg"`

5ggYgga Ybh (. '9ggUm

GhUfhXUhY. Bch5dd`]WUV`Y

 $\label{eq:higher} \begin{tabular}{ll} High \$

Gi Va]gg]cb cZ5ggYgga YbhHUg_g

Gh XYbhg UfY Yl dYWYX hc di hh\Y]f bUa Yg UbX gh XYbhbi a VYfg cb Yj YfmdU[Y cZh\Y]f Ugg][ba Ybhg"

Hi fb]h]b Gi Va]gg]cb

#mci YbWci bhYf'U'dfcV'Ya 'k \Yb'UthYa dr]b['rc'gi Va]hmci f'Ugg][ba Ybht\fci [\'Hi fb]r]bž'd'YUgY
hY'Yd\cbY'9I hYfbU'Gi ddcfhcb'-',) '''' %cf'Ya U]''h\Ya 'cb'<u>Yl hYfbU'hY'hgi ddcfh4 i bgk "YXi "Ui"</u>"'Gi ddcfh
\ci fg'UfY', .\$\$Ua '-'%\$.\$\$da 'cb'k YY_XUmg'UbX'-.\$\$Ua '-').\$\$da 'cb'k YY_YbXg'fl *) 'XUmg'U'mYUft\"'=\maintention
UfY'i bUV'Y'hc'gi Va]hmci f'Ugg][ba YbhXi Y'hc'U'ZJi 'hk]h\'Hi fb]h]b'mci 'a Um'Udd'm\Zcf'Ub'YI hYbg]cb\ZVi hmci
a i ghfYhJ]b'mci f'h]\W_Yhbi a VYf\Zfca '9I hYfbU''Gi ddcfhfU'cb['k]h\'Ubmch\Yf'fY'Yj UbhXcW'a Ybhgt'hc
]bWi XY'Ug'Yj]XYbW' hc'gi ddcfhmci f'Yl hYbg]cb'Udd']\WJh]cb'''\=\maintention
Uh\WJ'`mfYWY']j Y'U'h]\W_Yhbi a VYf\ZVi h]Zmci 'hY'Yd\cbY'mci 'k]``bYYX'hc'gdYW]\Z\WJ'`mUg_'Zcf'cbY''
Hi fb]h]b'U'gc'dfcj]XYg'i dXUhYg'cb'h\Y]f'gmghYa 'gfUh' g'cb'Hk]hYf"

; YbYfU`mž'UggYgga YbhitUg_g'a i ghVY'gi Va]hhYX'Y`YWfcb]WU``mj]U'Y]h\Yf'Hi fb]h]b'cf'U'A ccX`Y Ugg][ba Ybh''=b']bghUbWfg'k \YfY'h\]g']g'bchdcgg]V`Yž']hk]```VY'ghUhYX'cb'mci f'Wci fgY'g'A ccX`Y'g]hY'k]h\U`hYfbUh]j Y'gi Va]gg]cb'XYhU]`g"

@UhY 5ggYgga Ybh'DYbU`h]Yg

5b'UggYggYX'HUg_']g'XYYa YX``UhY']Z]h']g'gi Va]hhYX'UZhYf'h\Y'gdYW]Z[YX'h]a Y'UbX'XUhY'Ug'gYhci h']b'h\Y Wci fqY'@YUfb]b['A UbU[Ya YbhGmqhYa 'f@A GŁ"

$$\label{thm:condition} \begin{split} &\text{H}^{\text{U}$$

K cf_'gi Va]hhyx'zci fhyyb'fl%(EXUmg'Uzhyf'h\y'Xi Y'XUhy'k]``VY'a Uf_YX'UbX'zYYXVUW_'dfcj]XYX'Vi hbc'a Uf_ k]``VY'fYWcfXYX"'=Zh\Y'k cf_'k ci `X'\Uj Y'fYWr]j YX'U'dUgg'a Uf_'Vi hzcf'h\Y'`UhybYgg'UbX'h\Y'k cf_']g'U Wca di `gcfm'Wci fgY'Wca dcbYbhz'U'gh XYbh'k]``VY'XYYa YX'hc'\Uj Y'a Yhih\UhfYei]fYa Ybh''H\]g'XcYg'bch Udd`mhc'U'hUg_'h\Uh']g'UggYggYX'Vi hbc'a Uf_']g'Uk UfXYX"

K cf_'gi Va]hh/X'hk YbhnlcbY'f&&XUmg'UZhYf'h\Y'Xi Y'XUhY'k]```bchVY'UWWdhYX'Zcf'a Uf_]b['cf'ZYYXVUW_UbX'k]```fYWY]j Y'bc'a Uf_'cf'[fUXY"'=Zh\Y'UggYgga YbhHUg_']g'U'Wca di `gcfmWca dcbYbhcZh\Y'Wci fgY'U gh XYbhk]```Ui hca Uh]WU``mZU]`'h\Y'Wci fgY"

GdYWJU`7cbg]XYfUhJcb55dd`]WUhJcbg

 $\label{eq:linear_continuity} $$Mc_i = W_0 - W_$

G]W_bYggža]gUXj Ybhi fY'cf'ch\Yf'W]fW a ghUbWrg'VYmcbX'mci f'Wcbhfc``a Um

ł DfYj Ybhimci Zfca Wca d`Yhlb[U.Wci fqY fYei]fYa Ybhž

ł? YYd mci Zfca 'UthYbX]b['Ub 'UggYggUV'Y 'UWnji]tmž

ł Ghod moi gi Va]hh]b['UggYggUV'Y k cf_ Zcf'U Wci fgYž

ł `G][b]Z]\WbhmUZZY\Wimci f`dYfZcfa Ub\Wr`]b`UggYggUV`Y`k cf_ž`VY`]h'U`Zcfa U``YbX!cZgYa YghYf`Yl Ua]bUh]cbž`U \WUgg`hYghž`U``UVcfUhcfmhYghž`U`gYa]bUf`dfYgYbhUh]cb`cf`Ubmch\Yf`Zcfa 'cZUggYgga Ybh'

5 WUXYa]W<cbYghmUbX D`U[]Uf]ga

D`U[]Uf]ga `]g`i g]b['h\Y`k cfXg`cf`]XYUg`cZch\Yfg`UbX`dfYgYbh]b['h\Ya `Ug`mci f`ck b"'\lefi\Wb'hU_Y`a Ubm Zcfa gžZfca `XY`]VYfUhY`W\YUh]b['hc`UVW]XYbhU`mWcdm]b['Zfca `U`gci f\W' k]h\ci hUW_bck `YX[Ya Ybh'

IBGK [fcidgdu[]uf]ga]bhch\YZc``ck]b[WuhY[cf]Yg.

7 cdm]b[.'i g]b['h\Y'gUa Y'cf'j Yfmg]a]`Uf'k cfXg'hc'h\Y'cf][]bU`hYl h'cf']XYU'k]h\ci h'UW_bck `YX[]b['h\Y gci fW'cf'i g]b['ei chUh]cb'a Uf_g"'H\]g'U`gc'Udd`]Yg'hc']a U[Ygž'Ufh'UbX'XYg][b'dfcYWhgž'Ug'k Y``'Ug dfYgYbhUh]cbg'k \YfY'gca YcbY'dfYgYbhg'Ubch\Yf'g']XYUg'cf'k cfXg'k]h\ci h'WfYX]h'

±DUddfcdf]UhY`dUfUd\fUg]b[.'W\Ub[]b['U'ZYk'kcfXg'UbX'd\fUgYg'k\]`Y`acghmfYhJ]b]b['h\Y`cf][]bU`ghfi WhifY`UbX`]bZcfaUh]cb`k]h\ci hUW_bck`YX[YaYbh'H\]g'U`gc'Udd`]Yg`]b'dfYgYbhUh]cbg'k\YfY`gcaYcbYdUfUd\fUgYg`Ubch\Yf'g`]XYUg`cf'kcfXg'k]h\ci hWfYX]h''±iU`gc'Udd`]Yg`hc'd]YW]b['hc[Yh\Yf'ei chYg'UbXdUfUd\fUgYg`]bhc'U'bYk'k\c`Yžk]h\ci hfYZ/fYbW]b['UbX'U'ghi XYbh'g`ck b'UbU`mg]g`hc'Vf]b['h\Y`aUhYf]U`hc[Yh\Yf''

7 c``i g]cb. 'k cf_]b['k]h\ 'ch\ Yfg'Vi h'dUgg]b['c\Z'h\ Y 'k cf_'Ug'U'dYfgcb'g']b\X]j]\Xi U``k cf_"'7 c``i g]cb'U`gc]b\Wi XYg'dfcj]\X]b['mci f'k cf_'hc'Ubch\ Yf'ghi XYbh\ VYZcfY'h\ Y 'Xi Y 'XUhYzcf'Zcf'h\ Y' di fdcgY'cZh\ Ya d`U[]\Uf]g]b['Uh\Ubmh]a Yz'dUm]b['Ubch\ Yf'dYfgcb'hc'dYfZcfa 'Ub'U\WUXYa]\Wh\Ug_z'ghYU']b['cf'U\\ello i]f]b[Ubch\ Yf'dYfgcb'g' U\WUXYa]\Wk cf_'Ub\X'\\ello dm]b[']hz'c\ZYf]b['hc'\\ello a d`YhY'Ubch\ Yf'dYfgcb'g' k cf_'cf'gYY_]b[d\una Ybh\Zcf'\\ello a d`Yh\beta d`

±bUddfcdf]UhY`W]hUh]cb.`7]h]b[ˈgci fW/gˈk \]WX`\Uj Y`bchVYYb`fYUXžk]h\ci hUW_bck`YX[]b[ˈh\Y`″gYWcbXUfm″gci fW/Zfca k \]WX`_bck`YX[Y`cZh\Ya`\Ug'VYYb`cVhU]bYX"

8 i d`]\WUh]cb`ff`gY`Zld`U[]\Uf]ga "Ł`gi Va]\h]b[`mci f`ck b`k cf_ž]b`k \c`Y`cf`]b`dUfhžk \YfY`]h`\Ug`dfYj]ci g`m VYYb`dfYdUfYX`cf`gi Va]\hYX`Zcf`Ubch\Yf`UqqYqqa Ybhcf\Wci fgY`UhI_BGK_`cf`Ubch\Yf`i b]\Yfq]\m"

7 cffYWhfYZYfYbWb[dfUWhWyg.

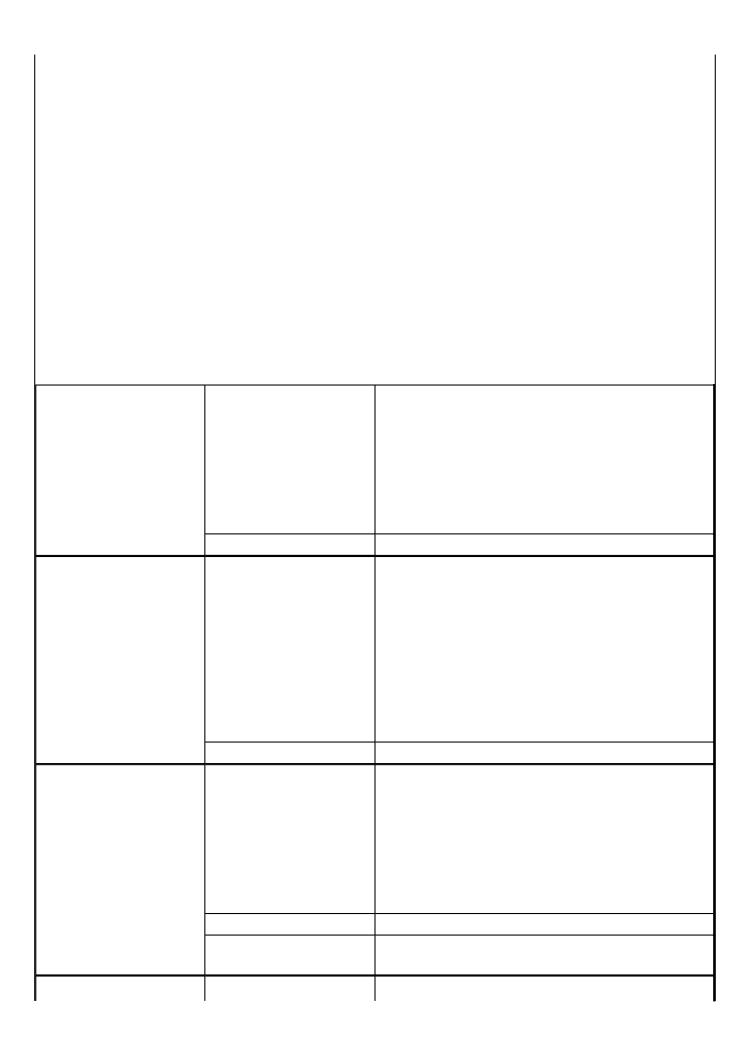
• VYHYfa UbU[Ymcifh]a Y

7ci fgY GWX YXi `Y

J]Yk 'WUgg'ha YhUV'Y

H]a YtUV`Y

8 UHY	Hmd Y	7 cbhYbh
K YY_'%'&*': YVfi Ufm!'(A UfWX	@YWn fY	±blfcXiWf]cb"!"H\]g"YWfifY"k]```dfcj]XY"Ub"cjYfj]Yk cZh\Y"WcifgY"UbX"`cc_"Uh'h\Y"Zc"`ck]b["eiYgh]cbg."
		K \UhXc'kY'a YUb'Vm5g]U'UbX'GYUg]U3
		K \Uh]g:h\Y:VYbYZ hcZi bXYfgHJbX]b['5g]Ub:\]ghcfm8
		<pre><ck 'wub'ufwxuyc`c[myb\ubwy'\]ghcf]wu`="" bxyfghubx]b[3<="" i="" pre=""></ck></pre>
		<pre>< ck 'WUb'bYk 'hYWXbc`c[mi\Y`d'i g'i bXYfghUbX'UbX dfYgYfj Y'h\Y'dUgh8</pre>
K YY_'&.') 'A UfWX'!'%% A UfWX	l@YWhifY K │	Aidtbh_gʻlddf}(`jbogʻfUNXXJbhg``!`H\Y`AUf]h]aY`G]`_`FcihY`
		H\Y'lfUbga]gg]cb'cZfY`][]cbžW`li fY'UbX'lfUXY"
		H\]g``YWnfYk]``YId`U]b`h\Y`UbWJYbhaUf]rjaY`gd]WYfcihY`UbX`]rg`]adUWrcb`h\Y`Wjj]`]nUrjcbg`cZ5g]U" K\UhXcYg`UfW\Yc`c[mihY```ig`UVcihih\Y`cf][]bg`UbX XYgrjbUrjcbg`cZh\Y`gd]WYg`UbX`[ccX



		H\]g``YWifYk]```X]gW gg`fYWbhifYgYUfW k\]W\`]bX]WUHYg`U``cb[``\]ghcfmcZcWW dUh]cb`cb`h\Y]g`UbX`cZG]b[UdcfY`VYZcfY`h\Y`9b[`]g\`WU]a\YX`]h'``
	Hi hcf]U`	
	5ggYgga Ybh	9ggUmD`Ub'!'dYYf'fYj]Yk 'Xi f]b['h\Y'h hcf]U`"'H\Y Z]bU`'UggYgga Ybhk]``'VY'[]j Yb'Vm`YWh fYf''&\$i `cUX]b[
K YY_'%\$.'+'A Um'!'% A Um	@YWh fY	Gf]'@Ub_U'!``UbX'cZgYfYbX]d]rm
		H\]g``YWiffY``cc_g`UhGf]`@Ub_U'g`]a dcffUbhdcg]h]cbcb'h\Y`A Uf]h]a Y`G]`_`F ci hY`UbX`\ck `]hVYWUa Y`Ub]a dcffUbh'hfUXY`dcgh'UbX`6i XX\]ghWfbhY`cZ hYUW.]b["``
	Hi hcf]U`	
K YY_'%%'%('A Um'!'&\$ A Um	@YWhi fY	J]YhbUa '!''h\Y'\]XXYb'ghcfm
		91 d`cfY`h\Y`amghYf]cig`W]h]Yg`cZì b[`8 b[`UbX A]`Gcb"
		H\Y`A]'Gcb'hYad'Y`[fcid'UfY'cbY'cZJ]YhbUa'g aU'cf'hcif]ghUhhfUWhJcbg"'Gc'k\c'kYfY'h\Y'dYcd'Y'cZ 7\UadU'k\c'Vi]'hh\Ya'UbX'k\Uh']g``YZhcZh\Y]f W`hifY3
	Hi hcf]U`	
	5 ggYgga Ybh	:]bU``UggYgga Ybh'`9ggUm' \$\$\$`k cfXg"`Hc`VY \UbXYX`]b`Vm(da `cb`h\Y`%+h\`A Um') \$i ``cUX]b[`
K YY_'%&.'&%'A Um'!'&+ A Um	@YWhi fY	8][]hu``5fVXUYc`c[m
		H\]g``YWnfYk]```YId`cfY'h\Y``UhYghUXjUbWYg]b`X][]HU``aYX]U`Zcf'h\Y`Yb\UbWYaYbhUbX'X]gd`UmcZUfW\UYc`c[mUbX'Udd`]YX'UbX'\]ghcf]WU``fYgYUfW\"'
		Ghi XYbhgʻk]``Yl dYf]YbWYʻUʻ' 8 J FʻUi [a YbhYX fYU`]hmiX]gd`Um
	Hi hcf]U`	
K YY_'% . &, 'A Um!'' >i bY	Hi hcf]U`	

Fygci fWyg

DfYgWf]VYX F Ygci fWYg

D`YUgY 'gYY 'cb 'a ccX`Y

FYWca a YbXYX FYgci fWYg

D`YUgY`gYY`cb`a ccX`Y

7 ci fgY '9j U'i Uh]cb 'UbX '8Yj Y`cda Ybh

 $: cfa\ U``ZYYXVUW\underline{\ '}\overline{Z}ca\ 'ghi\ XYbhg`k\]```VY`Wc```YWhYX`j\]U`a\ m9I\ dYf]YbWY`Uhih\Y`YbX`cZh\Y`Wci\ fgY''`$

a U[Y⁻7fYX]h