

ARTS3510

5Xj UbWX; Yfa Ub'5

GYa YghYf'CbY''##'&\$%

7ci fgY Cj Yfj]Yk

GHJZZ7cbHJWh8YHJ]`g

7cbj Ybcfg

B Ua Y	9a U]`	5j U]`UV]`] m	@cWUhjcb	D\cbY
8 Y b]gY '< UbHY`	X"\UbHY`4 i bgk "YXi "Ui	hw	h/W	b#U

GWkcc~7cbHJWh~abZcfa Uhlcb

GWkcc`cZ<iaUb]hJYg'UbX'@Ub[iU[Yg

@cWUhjcb. 'GW\cc`'C ZZWYž'A cfj Yb'6fck b'6i]`X]b[ž'@Yj Y``&ž'&),

CdYb]b[< ci fg. A cbXUm!: f]XUmž-Ua !(.() da

D\cbY. Ž*%'&'-',) '%*, %

: UI . 'Ž * %'&'-' ,) ', +\$)

9a U]`. \<u>U`4 i bgk "YXi "Ui</u>

5 hyb XUb WY F Yei]fYa Ybhg

5 'ghi XYbhi]g'Yl dYWYX'hc'UhiYbX'U```WUgg'WebhUWi\ci fg'Zcf'U'ZUWY!hc!ZUWY'fl &: Ł'cf'V`YbXYX'Wei fgY'UbX Wea d'YhY'U```UWfj]hjYg'Zcf'U'V`YbXYX'cf'Z ``micb`]bY'Wei fgY''

5 'ghi XYbhik \c'Uff]j Yg'a cfY'h\Ub'%) 'a]bi hYg'`UhY'a Um'VY'dYbU`]gYX'Zcf'bcb!UhhYbXUbWY'''⊋gi W\'U'dYbU`hm]g']a dcgYXž'h\Y'ghi XYbha i gh'VY']bZcfa YX'j YfVU``m'Uh'h\Y'YbX'cZWUgg'UbX'UXj]gYX']b'k f]h]b['k]h\]b'&(\ci fg''

ZUgh XYbhYl dYf]YbWg`]``bYggža]gUXj Ybh fY`cf`ch\Yf`cVW ffYbW'`h\Uha U_Yg`UVgYbW`Zfca `U WUgg#UW]j]hmi bUj c]XUV`Yžcf`Yl dYWg`hc`VY`UVgYbhZfca `U`Zcfh\Waa]b[`WUgg#UW]j]hmžh\Ymg\ci`X`gYY_ dYfa]gg]cb`Zfca `h\Y`7 ci fgY`5i h\cf]hmž'UbX`k \YfY`Udd`]WUV`Yžh\Y]f`fYei Yghg\ci`X`VY`UVWaa dUb]YX`VmUb cf][]bU``cf`VWfhZYX`WcdmcZU`a YX]WU``WYfhZWUhY`cf`ch\Yf`Zcfa `cZUddfcdf]UhY`Yj]XYbWY"

5.7 ci fgY 5 i h\cf]hma UmYI W gY 'U'ghi XYbhZfca 'WUggYg'cf'UWjj]hJYg'Zcf'i d'hc'cbY'a cbh\"'< ck Yj Yfž'h\Ym a UmUgg][b'UXX]hJcbU``UbX#cf'U'hYfbUhJj Y'HUg_g'hc'Ybgi fY'Wca d`]UbW'''5 '7 ci fgY '5 i h\cf]hm'Wcbg]XYf]b['h\Y [fUbhJb['cZUVgYbW'a i gh'VY'gUhJgZJYX'U'ghi XYbhk]```ghJ```VY'UV'Y'hc'a YYhh\Y'Wci fgY'g'`YUfb]b['ci hWca Yg UbX#cf'j c'i a Y'cZ'YUfb]b["'5 'ghi XYbhgYY_]b['Uddfcj U`'hc'VY'UVgYbh'Zcf'a cfY'h\Ub'cbY'a cbh\'a i gh'Udd'm]b'k f]hJb['hc'h\Y'8YUb'UbX'dfcj]XY'U``cf][]bU``cf'WYfhZYX'gi ddcfhJb['XcW a YbhUhJcb"

: cf'a cfY']bZcfa Uhjcb'UVci hih\Y'UhhYbXUbWY'dfchcWc`g']b'h\Y': UWV`hmcZ5fhg'UbX'GcWJU`GWJYbWYg.'\hdg.#k k k "Ufhg"i bgk "YXi "Ui #W ffYbhgh XYbhg#UWUXYa]W]bZcfa Uhjcb#dfchcWc`g![i]XY`]bYg#

5 WUXYa | W = b Zcfa Uh | cb ·

cfYggYbhJU`gh XYbh]bZcfa UhlcbfY`Uhlb[hc.fYei YghgZcfYl hYbg]cb/fYj]Yk cZa Uf_g/cWW dUhlcbU``\YUh\

UbX`gUZ/my'Yl Ua]bUh]cb`dfcWXi fYg/gdYW]U``Wtbg]XYfUh]cb`]b`h\Y`Yj YbhcZ]``bYgg`cf`a]gUXj Ybhi fY/ghi XYbhYei]lmiUbX`X]gUV]`]lmy'UbX`ch\Yf`YggYbh]U``UWJXYa]W]bZcfa Uh]cbž gYY`\hdg.#k k k "Ufhg"i bgk "YXi "Ui #W ffYbhghi XYbhg#JWJXYa]W]bZcfa Uh]cb#dfchcWt`g![i]XY`]bYg#

7ci fgY 8YHJ] g

7 fYX]hDc]bhg *

Gi a a UfmcZh\Y 7ci fgY

 $GiVYWh5fYU.9Wd_S`EfgV[We]$

#b 'fh]g 'Wci fgY 'mci 'k]```Wcbgc`]XUHY 'UbX'YI HY bX 'mci f'g_]``g']b``]ghY b]b['hcžgdYU_]b[žfYUX]b['UbX'k f]h]b['Yfa Ubžk]hh 'U'X]gh]bWiZcW g'cb'; Yfa Ub 'gcW]Y miUbX'W 'hi fY" @YUfb]b['UWh]j]h]Yg']bWi XY 'UbU'mg]b[Wca d'YI 'hYI hg'cb'WcbhYa dcfUfmhcd]Wg/\c'X]b['X]gW gg]cbg'cb'dfYdUfYX'gi V'YWhg'k]hh 'ZY ``ck 'ghi XYbhgž UbX'Wca a i b]WUh]b['cb'U'fUb[Y'cZgdYW]Z]YX'gi V'YWhg'fY`Uh]b['hc']ggi Yg'cZh\Y'Yj YfmXUmVi h'U`gc'hc VfcUXYf'gcW]U'ž'dc`]h]WU'ž'UbX'W 'hi fU''ei Ygh]cbg" 'Nci 'k]``'U`gc YI dUbX'UbX'\cbY']a dcfhUbhghi Xmg_]``g gi Wk'Ug'Wkccg]b['Uddfcdf]UhY '`YUfb]b['ghfUhY[]Ygža cb]hcf]b['UbX'UXj UbW]b['mci f'ck b'dfc[fYgg"

5 hh Y WcbWi g]cb cZh]g Wci fgY h Y gh XYbhk] ` VY UV Y hc

 $\% \ 5bU'mgY'Uf[i \ a \ Ybhg']b'hYl \ hg'XYU']b['k]h'wbhYa \ dcfUfmdfcV'Ya \ g'h'uhUfY'fY'Yj \ Ubhhc$

; Yfa Ubcd\cbY Wca a i b]h]Yg"

&" 8YVUhY cb dfYdufYX gi VYWg]b; Yfa Ub k]h U XY[fYY cZZi YbWhUbX gdcbhUbY]m"

' "DfcXi WY WYUfžXYHJ]YX k f]HYb UbX gdc_Yb X]gW gg]cbg cb U k]XY fUb[Y cZgi V (YbWggi igg]tG[

a YUbgʻcZWca a i b]WUh]cbʻUbXʻUgʻUbʻU]Xʻhcʻ`YUfb]b[ʻUgʻk Y```UgʻhcʻXYa cbghfUhYʻgca YʻUV]`]hmUgʻUb]bXYdYbXYbh`YUfbYf

5ggYgga Ybh

5ggYgga YbhHUg_g

5ggYgga Ybh'hJg_	K Y][\h	8i Y`8UhY	

HYgh'&''&(#\$)#&\$% '%\$!%%'Ua

.

Hi fb]hjb gYhjb[. H\]g]g bchU Hi fb]hjb Ugg][ba Ybh

5ggYgga Ybh' . 'GdYU_]b['5ggYgga Ybh

GHJfhXUhY. Bch5dd`]WUV`Y

@Yb[h\. +!, a]bg

 $8YhU]^*g. ^Gh XYbhg ^WcbXi Whg \cfh X]U^*c[i Yg^*f +!, 'a]bg +!]b^*d U]^*fg^*cf^*ga U^*[fci dg'': YYXVUW_j^*]]U^*a Uf_]b[fi Vf]WUbX^*]b X]j]Xi U^*Wca a Ybhg''$

 $\label{eq:higher_high_substitution} \mbox{Hi fb]h]b "gYhh]b[."H\]g"]g"bchU"Hi fb]h]b"Ugg][\ ba\ Ybh$

Gi Va]gg]cb cZ5ggYgga YbhHUg_g

Gh XYbhg UfY Yl dYWYX hc di hh\Y]f bUa Yg UbX gh XYbhbi a VYfg cb Yj YfmdU[Y cZh\Y]f Ugg][ba Ybhg"

Hi fb]h]b Gi Va]gg]cb

Imagi YbWci bhYf'U'dfcV'Ya 'k \Yb'UthYa dr]b['rc'gi Va]hmci f'Ugg][ba Ybht\fci [\'Hi fb]r]bž'd'YUgY hY'Yd\cbY'9I hYfbU'Gi ddcfhcb'-',) "''' %cf'Ya U] hYa 'cb'<u>Yl hYfbU'hY'hgi ddcfh4 i bgk "YXi "Ui"</u> "Gi ddcfh \ci fg'UfY', .\$\$Ua '-'%\$.\$\$da 'cb'k YY_XUmg'UbX'-.\$\$Ua '-') .\$\$da 'cb'k YY_YbXg'fl *) 'XUmg'U'mYUft'" Imai UfY'i bUV'Y 'rc'gi Va]hmci f'Ugg][ba YbhXi Y'rc'U'ZJi 'hk]h\ 'Hi fb]h]b'mci 'a UmUdd'mZcf'Ub'YI hYbg]cbž'Vi hmci a i ghfYhJ]b'mci f'h]\W_Yhbi a VYf'Zfca '9I hYfbU''Gi ddcfhfU'cb['k]h\ 'Ubmch\Yf'fY'Yj UbhXcW a Ybhgt'rc]bWi XY'Ug'Yj]XYbW' 'rc'gi ddcfhmci f'Yl hYbg]cb'Udd']\WJhjcb"'\Imai 'Ya U]''9I hYfbU''Gi ddcfhmci 'k]'`Ui hca Uh]\WJ'`mfY\W']j Y'U'h]\W_Yhbi a VYfž'Vi h]Zmci 'hY'Yd\cbY'mci 'k]'`'bYYX'rc'gdY\WZ\WJ'`mUg_'Zcf'cbY" Hi fb]h]b'U'gc'dfcj]XYg'i dXUhYg'cb'h\Y]f'gmghYa 'ghUh' g'cb'Hk]hYf"

; YbYfU``mž'UggYgga YbhitUg_g'a i ghVY'gi Va]hhYX'Y`YWfcb]WU``mj]U'Y]h\Yf'Hi fb]h]b'cf'U'A ccX`Y Ugg][ba Ybh'' =b']bghUbWfg'k \YfY'h\]g']g'bchdcgg]V`Yž']hk]```VY'ghUhYX'cb'mci f'Wci fgY'g'A ccX`Y'g]hY'k]h\U`hYfbUh]j Y'gi Va]gg]cb'XYhU]`g''

@UhY 5ggYgga Ybh'DYbU`h]Yg

5b'UggYggYX'HUg_']g'XYYa YX``UHY']Z]h']g'gi Va]HHYX'UZHYf'H\Y'gdYW]Z]YX'H]a Y'UbX'XUHY'Ug'gYhci h']b'H\Y Wti fgY'@YUfb]b['A UbU[Ya YbhGmghYa 'f@A GŁ"

 $\label{thm:condition} $$HY^UHY^dYbU^m]g^hY^cgg^cZ)_L^cZ^hY^hcHU^dcgg]VY^aUf_g^Zcf^hYY^HUg_Z^cf^YUW^XUmcf^dUfhhYfYcZhY^kcf_]g^UHY^@UhYbYgg^k]^*]bW^XY^kYY_YbXg^UbX^di_V^]WYc^]XUmg^"HY]g^XcYg^bchUdd^mhc^U'HUg_'hWh]g^UqqYqqYX^Vi_hbc^aUf_]g^Uk_UfXYX"$$$

K cf_'gi Va]hhyx'zci fhyyb'fl%(EXUmg'Uzhyf'h\y'Xi Y'XUhy'k]``VY'a Uf_YX'UbX'zYYXVUW_'dfcj]XYX'Vi hbc'a Uf_ k]``VY'fYWcfXYX"'=Zh\Y'k cf_'k ci `X'\Uj Y'fYWr]j YX'U'dUgg'a Uf_'Vi hzcf'h\Y'`UhybYgg'UbX'h\Y'k cf_']g'U Wca di `gcfm'Wci fgY'Wca dcbYbhz'U'gh XYbh'k]``VY'XYYa YX'hc'\Uj Y'a Yhih\UhfYei]fYa Ybh''H\]g'XcYg'bch Udd`mhc'U'hUg_'h\Uh']g'UggYggYX'Vi hbc'a Uf_']g'Uk UfXYX"

K cf_'gi Va]hh/X'hk YbhnlcbY'f&&XUmg'UZhYf'h\Y'Xi Y'XUhY'k]```bchVY'UWWdhYX'Zcf'a Uf_]b['cf'ZYYXVUW_UbX'k]```fYWY]j Y'bc'a Uf_'cf'[fUXY"'=Zh\Y'UggYgga YbhHUg_']g'U'Wca di `gcfmWca dcbYbhcZh\Y'Wci fgY'U gh XYbhk]```Ui hca Uh]WU``mZU]`'h\Y'Wci fgY"

GdYWJU`7cbg]XYfUhJcb55dd`]WUhJcbg

 $\label{eq:linear_continuity} $$Mc_i = W_0 - W_$

G]W_bYggža]gUXj Ybhi fY'cf'ch\Yf'W]fW a ghUbWrg'VYmcbX'mci f'Wcbhfc``a Um

ł DfYj Ybhimci Zfca Wca d`Yhlb[U.Wci fqY fYei]fYa Ybhž

ł? YYd mci Zfca 'UthYbX]b['Ub 'UggYggUV`Y 'UWhj]tmž

ł Ghod moi gi Va]h]b['UggYggUV'Y'k cf_ Zcf'U'Wci fgYž

ł `G][b]Z]\WbhmUZZY\Wimci f`dYfZcfa Ub\Wf`]b`UggYggUV`Y`k cf_ž`VY`]h'U`Zcfa U``YbX!cZgYa YghYf`Yl Ua]bUh]cbž'U \WUgg`hYghz`U``UVcfUhcfmhYghz`U`gYa]bUf`dfYgYbhUh]cb`cf`Ubmch\Yf`Zcfa 'cZ`UggYgga Ybh'

5 WUXYa]W<cbYghmUbX D`U[]Uf]ga

D`U[]Uf]ga `]g`i g]b['h\Y`k cfXg`cf`]XYUg`cZch\Yfg`UbX`dfYgYbh]b['h\Ya `Ug`mci f`ck b"'\lefi\Wb'hU_Y`a Ubm Zcfa gžZfca `XY`]VYfUhY`W\YUh]b['hc`UVW]XYbhU`mWcdm]b['Zfca `U`gci f\W' k]h\ci hUW_bck `YX[Ya Ybh'

IBGK [fcidgdu[]uf]ga]bhch\YZc``ck]b[WuhY[cf]Yg.

7 cdm]b[.'i g]b['h\Y'gUa Y'cf'j Yfmg]a]`Uf'k cfXg'hc'h\Y'cf][]bU`hYl h'cf']XYU'k]h\ci h'UW_bck `YX[]b['h\Y gci fW'cf'i g]b['ei chUh]cb'a Uf_g"'H\]g'U`gc'Udd`]Yg'hc']a U[Ygž'Ufh'UbX'XYg][b'dfcYWhgž'Ug'k Y``'Ug dfYgYbhUh]cbg'k \YfY'gca YcbY'dfYgYbhg'Ubch\Yf'g']XYUg'cf'k cfXg'k]h\ci h'WfYX]h'

±DUddfcdf]UhY`dUfUd\fUg]b[.'W\Ub[]b['U'ZYk'kcfXg'UbX'd\fUgYg'k\]`Y`acghmfYhJ]b]b['h\Y`cf][]bU`ghfi WhifY`UbX`]bZcfaUh]cb`k]h\ci hUW_bck`YX[YaYbh'H\]g'U`gc'Udd`]Yg`]b'dfYgYbhUh]cbg'k\YfY`gcaYcbYdUfUd\fUgYg`Ubch\Yf'g`]XYUg`cf'kcfXg'k]h\ci hWfYX]h''±iU`gc'Udd`]Yg`hc'd]YW]b['hc[Yh\Yf'ei chYg'UbXdUfUd\fUgYg`]bhc'U'bYk'k\c`Yžk]h\ci hfYZ/fYbW]b['UbX'U'ghi XYbh'g`ck b'UbU`mg]g`hc'Vf]b['h\Y`aUhYf]U`hc[Yh\Yf''

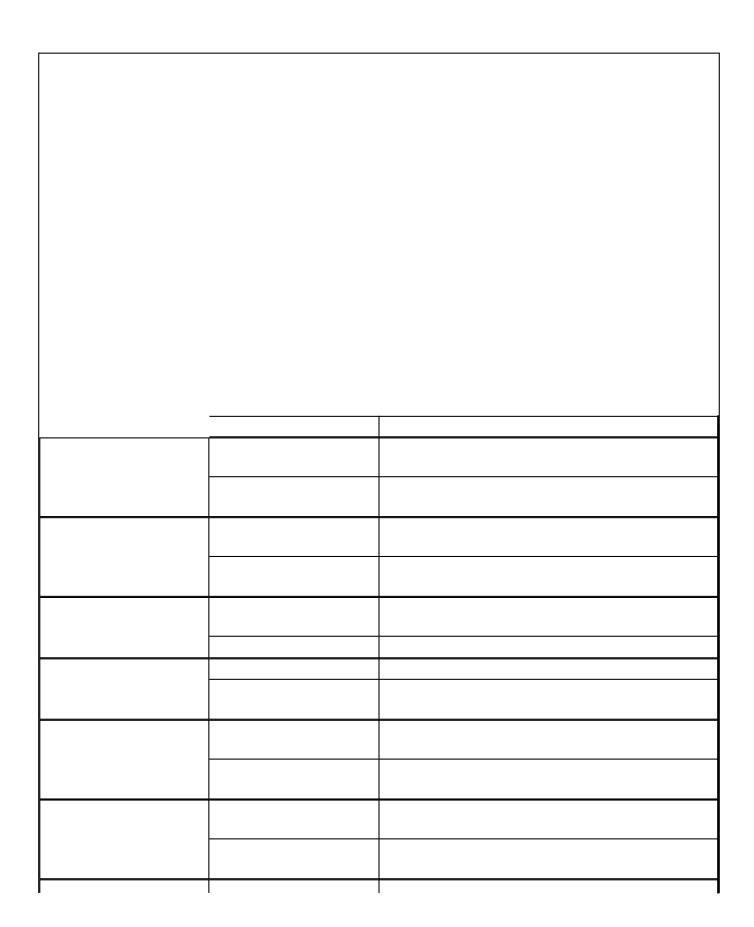
7 c``i g]cb. 'k cf_]b['k]h\ 'ch\ Yfg'Vi h'dUgg]b['c\Z'h\ Y 'k cf_'Ug'U'dYfgcb'g']b\X]j]\Xi U``k cf_"'7 c``i g]cb'U`gc]b\Wi XYg'dfcj]\X]b['mci f'k cf_'hc'Ubch\ Yf'ghi XYbh\ VYZcfY'h\ Y 'Xi Y 'XUhYzcf'Zcf'h\ Y' di fdcgY'cZh\ Ya d`U[]\Uf]g]b['Uh\Ubmh]a Yz'dUm]b['Ubch\ Yf'dYfgcb'hc'dYfZcfa 'Ub'U\WUXYa]\Wh\Ug_z'ghYU']b['cf'U\\ello i]f]b[Ubch\ Yf'dYfgcb'g' U\WUXYa]\Wk cf_'Ub\X'\\ello dm]b[']hz'c\ZYf]b['hc'\\ello a d`YhY'Ubch\ Yf'dYfgcb'g' k cf_'cf'gYY_]b[d\una Ybh\Zcf'\\ello a d`Yh\beta d`

±bUddfcdf]UhY`W]hUh]cb.`7]h]b[ˈgci fW/gˈk \]WX`\Uj Y`bchVYYb`fYUXžk]h\ci hUW_bck`YX[]b[ˈh\Y`″gYWcbXUfm″gci fW/Zfca k \]WX`_bck`YX[Y`cZh\Ya`\Ug'VYYb`cVhU]bYX"

8 i d`]\WUh]cb`ff`gY`Zld`U[]\Uf]ga "Ł`gi Va]\h]b[`mci f`ck b`k cf_ž]b`k \c`Y`cf`]b`dUfhžk \YfY`]h`\Ug`dfYj]ci g`m VYYb`dfYdUfYX`cf`gi Va]\hYX`Zcf`Ubch\Yf`UqqYqqa Ybhcf\Wci fgY`UhI_BGK_`cf`Ubch\Yf`i b]\Yfq]\m"

7 cffYWhfYZYfYbWb[dfUWhWyg.

• VYHYfa UbU[Ymcifh]a Y



K_YY_"%&."&%"A_Um"!"&+	Hi hcf]U`	FYj]g]cb%HYghdfYdUfUh]cb	
A Um	@YWhifY	HYgh&:#GdYU_]b[:HYghdfYdUfUh]cb	
K YY_'% . '&, 'A Um'! ''	Hi hcf]U`	GdYU_]b['5ggYgga Ybh	
>i bY			

FYgci fWfg

DfYgWf]VYX F Ygci fWYg

HYI hVcc_

 $5gdY_hY'bYi''6\&'''@Y\f!'ibX'5fVY]hgViWX'a]h5iX]c!78'''HY]'''%' = 68'-+, !'!\&!**) $\&+!\&'fUjU]'UV'Y'UhhXYIb]iYfg]hm6cc_ghcfYL$

FYWca a YbXYX FYgci fWYg

GYY'A ccX`Y'Wci fgY'k YVg]hY

7 ci fgY '9j U'i Uh]cb 'UbX '8 Yj Y`cda Ybh

a U[Y'7fYX]h

GmbYf[]Yg^]b^GcibX^&\$%*

7F=7CG

7F =7 C G 'Dfcj]XYf'7cXY. '\$\$\$-,;