

## **MMAN4953**

FYgYUfW\`H\Yg]g`7

HYfa 'C bY''##'&\$&%

## 7ci fgY'Cj Yfj ]Yk

## GHJZ:7cbHJWh8YHJ]`g

#### 7cbj Ybcfg

B Ua Y	9a U]`	5j U]`UV]`]lm	@cWJhjcb	D\cbY
HfUW]Y 6UfVYf	$\mathbf{e}$	J	>%+ '( \$%5	
		Ya U]``cf'j ]U'HYUa g		

#### GWkcc~7cbhJWh~abZcfa Uh]cb

#### @cWUhlcb

I BGK 'A YVX.Ub]WU``UbX'A Ubi ZUWi f]b[ '9b[ ]bYYf]b[

5]bgk cfh\ 'Vi ]`X]b[ '>%+ž'@Yj Y`'%

5Vcj Y 7 c ZZYY cb 7 Ua di g

#### <ci fg

-.\$\$-).\$\$da ž'A cbXUm-: f]XUm

ł7 `cgYX cb 'di V`]W\c`]XUmgž GWkcc``gWkYXi `Y%Wj Ybhg \$bXT b]j Yfg]hmG \ZMXKcdbb7 Ua di g

#### K YV

GWXcc`cZA YWXUb]WU`UbX'A Ubi ZUWi f]b[ '9b[ ]bYYf]b[

9b[]bYYf]b[]Gh XYbhGi ddcfhGYfi ]WYa

9b[]bYYf]b['=bXi ghf]U`'HfU]b]b[

LBGK Ghi Xm5VfcUX UbX 91 VX Ub[Y flcf]bVci bX ghi XYbhgŁ

I BGK : i hi fY Ghi XYbhg

#### D\cbY

fŽ\*%&Ł-',),)\$\$-BiWYigGhXYbh<iV

fŽ\*%%&L'-',) '+\*\*%'-'9b[]bYYf]b['=bXi glf]U`'HfU]b]b[

fŽ\*%%&L-',) ''%+- - I BGK Gh Xm5VfcUX UbX I BGK '91 WX Ub[Y fZcf]bVci bX gh XYbhgL

 $f\tilde{Z}^*\%.\&L^{-}',).($-+-$$  ZYY.cb.7 Ua di g

#### 9a U]`

<u>9b[]bYYf]b[ 'Gh XYbhGi ddcfhGYfj ]W</u>yg'-'W ffYbhgh XYbhYbei ]f]Yg

• Y"[""Ybfc`a Ybhž'dfc[fYgg]cbž'WUg\"fYei Yghgž'Wci fgY']ggi Yg'cf'dfc[fUa!fY`UhYX'ei Yf]Yg

<u>9b[]bYYf]b[ '±xi glf]U`'HfU]b]b[</u> '-'±xi glf]U`'lfU]b]b[ 'ei Ygl]cbg

<u>I BGK "Gh Xm5VfcUX"</u>—"gh XmUVfcUX"gh XYbhYbei ]f]Yg"fZcf"]bVci bX"gh XYbhgŁ

<u>I\_BGK\_'9| W.Ub[Y</u>'-'gh XYbhY| W.Ub[Y'Ybei]f]Yg'flcf']bVci bX'gh XYbhgŁ

I BGK : i h fY'Gh XYbhg'-'dchYbhJU'gh XYbhYbei ]f]Yg

• Y"["UXa]gg]cbgžZYYgždfc[fUagžWfYX]hlfUbgZYf

<u>GWXcc``CZZJWY</u>'--'GWXcc``[YbYfU``cZZJWY'UXa]b]ghfUh]cb'Ybei]f]Yg

• B6. h\Y fY`Yj UbhhYUa g``]ghYX UVcj Y a i ghVY WcbHUWYX -

gh XYbhYbei ]f]Yg

7 fYX]h'Dc]bhg'('	
Gi a a UfmcZh\Y'7ci fgY	
H\Y`h\Yg]g`dfcj]XYg`Ub`cddcfhib]hmZcf`mci `hc`Vf]b[`hc[Yh\Yf`Yb[]bYY	f]b[ 'df]bWjd`Yg``YUfbYX'cj Yf

7ci fgY<sup>.</sup>8YHJ]`g

 $\label{thm:condition} $$HY'WcifgY']g'HUi[\hrUg'Ub']bX]j']XiU''fYgYUfWX'dfc'YWz'hc'XYjY`cd'U''YjY''cZfYgYUfWX'g_]`g'UbXUihcbcam''$ 

## 5ggYgga Ybh

## 5ggYgga Ybh HUg\_g

5ggYgga Ybh'tUg_	K Y][ \h	8iY'8UHY	Gh XYbh@YUfb]b[ Ci hWca Ygʻ5ggYggYX
H\Yg]g`dfcYWhUbX`fYdcfh	*\$1	: f]XUmi) da 'K YY_'%\$	%ž'&ž'' ž'( ž')
H\Yg]g`dfYgYblUh]cb`	<b>%</b> \$I	K YXbYgXUmK YY_'%%fH67Ł	

## 5ggYgga Ybh'8YhJ]`g

5ggYgga Ybh% H\Yg]g dfc YWhUbX fYdcfh

8 YW] g.

Н%

Dfc YWrfYdcfhf[i]XY UbX a Uf\_]b[ 'fi Vf]WUj U] UV Y cb h Y Wci fgY A G HYUa g g]hYŁ"

H&.

Η' .

: ]bU``dfc^YWifYdcfhif[ i ]XY`UbX`a Uf\_]b[ `fi Vf]WUj U]`UV`Y`cb`h\Y`Wci fgY`A G`HYUa g`g]hYŁ"

DfYgYbhUhjcb`f]bZcfa Uhjcb`k ]```VY`Uj U]`UV`Y`cb'h\Y`Wci fgY`A G`HYUa g`g]hYŁ"`

.

5ggYgga Ybh& H\Yg]g dfYgYbhJhjcb

8YHJ]`g.

Н%

## F Ygci fWyg

FYWca a YbXYX FYgci fWfg

BchUj U]`UV`Y

7ci fgY 9j U`i Uh]cb UbX 8Yj Y`cda Ybh

@UVcfUhcfmK cf\_g\cd \pdzcfa Uhlcb

7 C J =8!% 'B C H9. 'H\Y'GW\cc```UVcfUhcfmiZJW]']h]Yg'UfY'cdYb'hc'fYgYUfW\'h\Yg]g'gh XYbhg/\ck Yj Yfž'UWW'gg ]g``]a ]hYX"'Hc'Wca d`mk ]h\'[ cj Yfba Ybhfg'gcW]U`X]ghUbW]b[ 'fYei ]fYa YbhgžY"[ "ž'( 'gei UfY'a YhYfg'dYf dYfgcbžYUW\'fcca '\Ug'U'a Ul ]a i a 'WUdUW]hm`]a ]hž'k \]W\'k ]``'VY'a cb]hcfYX'Vmh\Y'gi dYfj ]g]b[ dfcZYgg]cbU`'ghUZ''D`YUgY'W\YW\_'k ]h\'h\Y'`UVcfUhcfmicZ]WYf]b'mci f'UfYU'VYZcfY'UWW'gg]b[ 'UbX'cVgYfj Y'h\Y `]a ]h'UbX'U``'ch\Yf'qUZYhmdfYWUi hlcbq"

•

 $\label{eq:maighgyy} $$Mci 'a i ghgyy_'[i ]XUbW' UbX' Uddfcj U``Zfca 'mci f'H\Yg]g'gi dYfj ]gcf'df]cf'hc' Ubm'`UVcfUhcfm'UWfj ]h]Yg'' $$$ 

.

 $\label{thm:condition} $$HY^*UVcfUhcf]Yg^*UfY^hY^*fYgdcbg]V]^]hmcZhY^*ghUZ]b!W.Uf[Yž^*UbX^mci a i ghcdYfUhY^k]hY]bhYY^*UWWdhYX dfUWf]WYg^*cZhY^*UVcfUhcfmWcbWfbYX''@UVcfUhcfmghUZUfY^\][\`mg_]`YX^*UbX^\Y^dZ\'AZ' \``UXj UbhU[Y cZhY]fYl dYf]YbW/\ck Yj Yfz^mci g\ci `X'bchYl dYWh`UVcfUhcfmghUZhc'hU_Y`fYgdcbg]V]`]hmZcf'mci f'hYg]g cf'WUffmci hk cf_'Zcf'mci ''$ 

.

.

: cf'a cfY']bZcfa Uhjcb'UVci h'UVWYgg]b['h\Y'GW\cc''g''UVcfUhcf]Ygž'd'YUgY'j ]g]hh\Y'GW\cc'\
k YVg]hY.`\hdg.#k k k "Yb[]bYYf]b["i bgk "YXi "Ui #a YV\Ub]\W'!Yb[]bYYf]b[#Ygci f\Wg#UV!U\W\gg!\ck!hc!\
Zcfa q

## K cf g\cd

.

Mci 'a i ghgYY\_'[i]XUbW''UbX'Uddfcj U`'Zfca 'mci f'H\Yg]g'gi dYfj]gcf'df]cf'hc'fYei Ygh]b['Ubmik cf\_g\cd UWn]j]h]Yg"

.

5```ghi XYbhUWhji JhjYg`fYei Jf]b[ `a Ubi ZJWhi fY`]b`h\Y`A YW\Ub]WJ``UbX`A Ubi ZJWhi f]b[ `9b[ ]bYYf]b[ `fA A 9Ł k cf\_g\cd`g\ci `X`VY`X]gW ggYX`k ]h\ 'h\Y`k cf\_g\cd`dYfgcbbY``Uhh\Y`]bWYdh]cb`cZh\Y`k cf\_"'H\Y`k cf\_g\cd dYfgcbbY``a i gh\Uj Y`h\Y`cddcfhi b]hmhc`UXj ]gY`UbX`]bZi YbWY`h\Y`XYg][ b`hc`\Y`d`a ]b]a ]gY`UggYa V`mž a Ubi ZJWhi fY`cf`Z bWh]cbU``dfcV`Ya g"

•

H\Y'k cf\_g\cd']g'i gi U``m']b'j Yfm\][\'XYa UbX"'=\mci 'fYei ]fY'h\Y'k cf\_g\cd'hc'a Ubi \( \text{Z}\)Wi fY'Yei ]da Ybh YggYbh]U`hc'mci f'h\Yg]g\( \text{z}'\)h\Yb'a U\_Y'gi fY'h\Uhimci 'X]g\( \text{gg'mci f'fYei }]fYa Ybhg'\Ug'Y\Uf'm\Ug'\dcgg]\VY'k ]h\'h\Y \( \text{cf\_g\cd}\)\\ \( \text{cf\_g\cd}\)\\ \( \text{glob}\) \( \text{glob}\) \( \text{glob}\) \( \text{glob}\)\\ \( \text{glob}\)\\\ \( \text{glob}\)\\\ \(

UggYgga YbhidYfZcfa UbWYžmci 'UfY'Y`][]V`Y`hc'Udd`m'Zcf'GdYWJU``7cbg]XYfUhJcb'df]cf'hc'gi Va]htjb['UbUggYgga Ybhicf'g]htjb['Ub'Yl Ua"

I BGK 'bck '\Ug'U': <u>|hhc'G|h#Gi Va |hfi `Y</u>ž'k \]W\ 'a YUbg't\\Uh']Zmci 'UthYa dh'Ub'Yl Ua 'cf'gi Va ]h'U'd]YW'cZ UggYgga Ybhž'mci 'UfY'XYWUf]b[ 'mci fgY`ZZ]h'Ybci [\'hc'Xc'gc'UbX'WUbbch`UhYf'Udd`mZcf'GdYW]U` 7 cbg]XYfUh]cb"

: cf`XYhJ]`g`cZUdd`m]b[ 'Zcf`GdYW]U``7cbg]XYfUh]cb`UbX`WcbX]h]cbg`Zcf`h\Y`Uk UfX`cZgi dd`Ya YbhUfm UggYgga Ybhž'd`YUgY`gYY`h\Y`]bZcfa Uh]cb`cb`I BGK 'g`<u>GdYW]U``7cbg]XYfUh]cb`dU[Y</u>"

D`YUgY'bchY'h\Uhghi XYbhg'k]``bch'VY'fYei]fYX'hc'dfcj]XY'Ubm'XcW'a YbhUfm'Yj]XYbWY'hc gi ddcfh'UVgYbWg'Zfca 'Ubm'WUggYg'a]ggYX'**VYWUi gY'cZ'7CJ=8!%** 'di V`]W\YU'h\ 'a YUgi fYg'gi W\'Ug]gc`Uh]cb"'| BGK 'k]``bch'VY']bg]gh]b[ 'cb'a YX]WU`'VW'fh]ZJWUh'Yg'Zfca 'UbmcbY'XYYa YX'hc'VY'U'dcg]h]j Y'WUgYZ cf'k\Yb'h\Ym\Uj Y'fYWcj YfYX"'Gi W\'WYfh]ZJWUh'Yg'UfY'X]ZZJW 'hhc'cVhU]b'UbX'di h'Ub'i bbYWYggUfmghfU]b'cb ghi XYbhg'UbX'a YX]WU`'ghUZZ''

 $5\,dd^{3}WUhlcbg^{3}Zcf^{3}gdYW_{U}^{3}W^{3}bg^{3}XYfUhlcb^{3}k^{3}XYfUhlcb^{3}xYfUh$ 

## 5 WUXYa ]W<cbYghmUbX D`U[ ]Uf]ga

 $\label{thm:continuous} IBGK ``Ug`Ub`cb[c]b[`Wcaa]haYbhhc`ZcghYf]b[``U`W``hifY`cZ`YUfb]b[`]bZcfaYX`VmUWUXYa]W]bHY[f]hm'`5``IBGK ``ghiXYbhg``UjY`U`fYgdcbg]V]`]hmhc`UX\YfY`hc`h\]g`df]bW]d`Y`cZUWUXYa]W]bHY[f]hm'`D`U[]Uf]gaibXYfa]bYg`UWUXYa]W]bHY[f]hmUbX`]g`bchhc`YfUhYX`UhIBGK "`B'SY[Sde_SfG@EI[eVWY] WWSege[YfZW_aXSekagdai`ž$ 

D`U[]Uf]ga `]g`U`lmdY`cZ]bhY``YWi U``lh\YZh'`\#i\WUb`HU\_Y`a UbmZcfa gžZfca `XY`]VYfUhY`\W\YUlf]b[`lc`U\W]XYbhU``m \\cdrigot f\W`k ]lh\ci hU\\\_bck `YX[Ya Ybh'`I BGK `\Ug`dfcXi \\X'X`U`k YVg]lhY`k ]lh\ci hU\\\_bck `YX[Ya Ybh'`I BGK `\Ug`dfcXi \\X'X`U`k YVg]lhY`k ]lh\`U`k YU`h\`cZ fYgci f\W`g`lc`gi ddcfhighi XYbhg`lc`i bXYfghUbX`UbX`Uj c]X`d`U[]Uf]ga žij ]g]h 'ghi XYbh'i bgk "YXi "Ui \\d'\U[]Uf]ga "\\Y`@YUfb]b[`7 YbhY`Ugg]ghg`ghi XYbhg`k ]lh\`I bXYfghUbX]b[`U\WUXYa ]\W]bhY[f]hmUbX`\ck 'bchlc'd`U[]Uf]gY" \\YmU`gc`\c`X`k cf\_g\cdg`UbX`\WUb`\Y`d`ghi XYbhg`cbY!cb!cbY"

Mci 'UfY'U'gc fYa ]bXYX'h\Uh\WUfYZ ``h]a Y`a UbU[ Ya Ybh]g Ub']a dcffUbhdUfhcZgh XmUbX'cbY'cZh\Y

## 5 WUXYa ]W = b Zcfa Uh cb

#### 7 fYX]hdc]bhg

7 ci fgY'WfYX]h']g'WU'W'`UhYX']b'I b]hg!C ½7 fYX]hfl C 7 L'''H\Y'bcfa U``k cf\_`cUX'YI dYWfUhJcb'Zcf'cbY'I C 7 ]g'UddfcI ]a UhY`m'&) '\ci fg'dYf'hYfa "'H\]g']bWi XYg'WUgg'WcbhUWh'\ci fgz'df]j UhY'ghi Xmz'ch\Yf'`YUfb]b[ UWfj] ]h]Ygz'dfYdUfUhJcb'UbX'hJa Y'gdYbh'cb'U``'UggYggUV`Y'k cf\_"

#### Cb!WUa di g WUgg UHYbXUbW

Di V`]WX]ghJbV}b[ 'WcbX]hJcbg'a i ghVY'Zc``ck YX'Zcf'U```ZJWY!hc!ZJWY'WUggYg"'Hc'Ybgi fY'h\]gž'cb`migh XYbhg

## a dcfhUbh'@]b\_g

- A ccX`Y
- <u>@UV:5\W\/aa</u>
- < YU`h\ 'UbX'GUZY m
- <u>7 ca di h|b[ : UW|^]h|Yq</u>
- Gh XYbhF Ygci fWg
- 7 ci fgY 'Ci h]bYg
- 9b[]bYYf]b['Gh XYbhGi ddcfhGYfj]\Wg:7YblfY
- A U YfadUW
- I BGK 'H]a YHUV'Y
- I BGK '< UbXVcc
- LBGK 'A YWXUb]WU`'UbX'A Ubi ZUWi f]b[ '9b[ ]bYYf]b[
- <u>9ei ]hUV`Y`@YUfb]b[`GYfj ]WYg</u>

## a U[Y'7fYX]h

GmbYf[]Yg^]b^GcibX^&\$%\*

#### 7F = 7CG

7F = 7CG Dfcj ]XYf 7cXY. \$\$\$-,;

#### 5W\_bck `YX[ Ya YbhcZ7ci blfm

 $K Y : UW\underline{b} ck `YX[Y : h, Y : 6YXY[U : dY cd `Y : k \ c : UfY : h, Y : hfUX]h\underline{b} cb U : W ghcX]Ubg : cZh, Y ``UbXg : cb : k \ ]WX : I B G K ? Ybg]b[hcb : WUa di g : ]g ``cWUhYX''$ 

# 5ddYbX]I. '9b[]bYYfg'5i ghfU`]U'f95Ł'DfcZYgg]cbU`'9b[]bYYf'7ca dYhYbWmGHJbXUfX

Dfc[fUa '±bhYbXYX'@YUfb]b['CihWca Yg	
?bck `YX[Y'UbX'g_]```VUgY	
D9%%7ca dfY\Ybg]j Yž'h\YcfmVUgYX'i bXYfgHJbX]b[ 'cZh\Y'i bXYfd]bb]b[ 'bUhi fU`'UbX d\mg]WJ`'gWJYbWYg'UbX'h\Y'Yb[ ]bYYf]b[ 'Z bXUa YbHJ`g'Udd`]WJV`Y'hc'h\Y'Yb[ ]bYYf]b[ 'X]gWJd`]bY	
D9%%.7cbWrdhi U`i bXYfghUbX]b[ cZh\Ya Uh\Ya Uh\Ya Uh]Wgžbi a Yf]WU`UbU`mg]gžghUh]gh]WgžUbX Wca di hYf'UbX`]bZcfa Uh]cb'gW]YbWrg'k\]W\i bXYfd]b'h\Y'Yb[]bYYf]b[ 'X]gW]d`]bY	
D9%" '±0!XYdh\'i bXYfgh\bX]b[ 'cZgdYW]U`]ghVcX]Yg'cZ_bck `YX[ Y`k ]h\]b'h\Y'Yb[ ]bYYf]b[ X]gW]d`]bY	
D9%"( '8]gWYfba YbhcZ_bck 'YX[ Y'XYj Y`cda YbhUbX'fYgYUfW\'X]fYWIjcbg'k ]h\]b'h\Y Yb[ ]bYYf]b[ 'X]gWJd`]bY	
D9%") "? bck "YX[Y"cZYb[]bYYf]b[ "XYg][b"dfUWf]VY" "UbX" WcbhYl hi U" "ZJWcfg"]a dUWf]b[ "h\YYb[]bYYf]b[ "X]gW]d"]bY	
D9%"* I bXYfgHJbX]b[ 'cZh\Y'gWcdYž'df]bWjd`Ygž'bcfa gž'UWVci bHJV]`]hjYg'UbX'Vci bXg'cZ gi gHJ]bUV`Y'Yb[ ]bYYf]b[ 'dfUWjWY']b'h\Y'gdYWjZJWX]gWjd`]bY	
9b[]bYYf]b['Udd`]WUh]cb'UV]`]hm	
D9&"%5dd`]WUhjcb`cZYghUV`]g\YX`Yb[]bYYf]b[`a Yh\cXg`hc`Wca d`Yl `Yb[]bYYf]b[`dfcV`Ya gc`j ]b[	
D9&"&": `i Ybh'Udd`]WUh]cb'cZYb[]bYYf]b['hYVXb]ei Ygž'hcc`g'UbX'fYgci fWfg	
D9&"' '5dd`]\WInjcb'cZgmghYa Unj\WYb[]bYYf]b['gmbh\Yg]g'UbX'XYg][b'dfc\WggYg	