## MATHEMATICS ENRICHMENT CLUB. Problem Sheet 15, September 2, 2014 <sup>1</sup>

- 1. Which is larger  $10\hat{\theta}^{00}$  or 300!?
- 2. A chess board is an 88 grid of squares coloured white or black so that no two adjacent squares are the same colour. Given tiles that are 2 grid squares it is possible to cover the chessboard completely, and it takes precisely 32 tiles. Show that it is impossible to cover a chessboard with opposite corners removed.

3.

Two functions, f and g, are said to be *orthogonal* if hf; gi = 0. Let  $p_0(x) = 1$  and  $p_1(x) = x$ ,

- (a) Show that  $p_0$  and  $p_1$  are orthogonal.
- (b) Find  $p_2(x)$