

# 7ci fgY<sup>·</sup>Cj Yfj ]Yk

# GhUZZ:7cbhUWh:8YhU]`g

# 7cbj Ybcfg

BUa Y	9a U]`	5j U]`UV]`]hm	@cWUh]cb	D\cbY		
H\Ub\`B\c`8c	hb"Xc4 i bgk "YXi "Ui		Fcca '%\$\$' ž @Yj Y`'%2'9&* 6]c`c[]WU` GW]YbWYg Gcih\			
@YWhifyfg						
	1					

# 7ci fgY 8YW] g

## I b]hg~cZ7fYX]h~\*

## Gi a a UfmcZh\Y 7ci fgY

H\]g`Wci fgY`gYfj Yg`Ug`Ub`]bfcXi Wf]cb`hc`d\mg]c`c[]\WJ``a YUgi fYa Ybhi g]b[`V]cgYbgcfg`UbX`hfUbgXi Wfg" H\]g`Wci fgY`XYU`g`df]a Uf]`mk]h\[U]b]b[`Ub`i bXYfghUbX]b[`cZh\Y`d\mg]\WJ``df]b\Wd`Yg`k\]\W.`[cj Yfb`h\Y a YUgi fYa YbhcZU`V]c`c[]\WJ``j Uf]UV`Y`cf`gmghYa žVmU`hfUbgXi WYf`k\]\W.`\wcbj Yfhg`h\Y`j Uf]UV`Y`]bhc`Ub Y`Y\\f]\WJ``g][bU`"`6mh\Y`YbX`cZh\Y`\wci fgY`mci `g\ci `X`i bXYfghUbX`j Uf]ci g`a YUgi fYa YbhXYj ]\Wg`UbX UddfcU\WYg`]\bWi X]b[`h\Y`i bXYf`m]b[`V]c`c[]\WJ``dfc\Wgg`h\Uh[YbYfUhYg`h\Y`ei Ubh]mhc`VY`a YUgi fYX`cf \wcbhfc``YX"`H\Y`VUg]\WJ]cgYbgcfg`UbX`hfUbgXi \Wfg`i gYX`hc`a YUgi fY`dfYggi fYžZck žj c`i a Y`UbX \_\_]bYa Uh]\\g`UfY`YI Ua ]bYX`U`cb[`k]h\`UgdY\\g`cZY`Y\\f]\WJ``gUZYhmUbX`a YX]\\WJ``]bghfi a YbhUh]cb"

## 7ci fgY 5]a g

H\Y'U]a g'cZh\]g'Wti fgY'UfY'hc.

### 7 ci fgY @YUfb]b[ Ci hWca Yg

- %" 8 YgWf]VY 'h\Y 'Udd`]WUh]cbg'cZj Uf]ci g'gYbgcfg'UbX'hfUbgXi WYfg'Uj U]`UV`Y 'Zcf'd\mg]c`c[]WU``UbX WY``i `Uf'a YUgi fYa Ybhg
- &" 91 d`U]b Z bXUa YbHJ`V]cgYbg]b[ 'UbX'ffUbgXi Wfjcb'df]bWjd`Yg
- ' "5dd`mY`YWf]WU`ža YWXUb]WU``UbX`WXYa ]WU``Yb[]bYYf]b[`WcbWYdhg`hc`U`fUb[Y`cZdfcV`Ya g`UbX a YX]WU``Udd`]WUhcbq
- ("7ca di hY'g]a d'Y'V]cgYbg]b[ 'UbX'lfUbgXi Whjcb'dfcV'Ya g
- ) " F Yj ]Yk 'h\Y``]hYfUhi fY`]b'h\Y`V]cgYbg]b[ 'UbX'hfUbgXi Wh]cb'Udd`]\WUh]cb'UfYU

## ; fUXi UhY WUdUV]`]h]Yg

H\YgY``YUfb]b['ci hWca Yg`fY`UhY'a cghighfcb[`mhc'h\Y'Zc``ck]b['I BGK'[fUXi UhY ci hWca Yg.

- %" gWkc`Uf`mYbei ]fmWUdUV`Y`cZ`]bXYdYbXYbhUbX`Wc``UVcfUhjj Y`Ybei ]fm/
- &" i bXYfgHJbX]b[ cZh\Y]fX]gW[d`]bY]b ]hg ]bhYfX]gW[d`]bUfmWcbhYl h/
- "UV`Y`hc`Udd`mih\Y]f`\_bck`YX[Y`UbX`g\_]``g`hc`gc`j ]b[`dfcV`Ya gžUbX/
- ("Wc``UVcfUhjjY'UbX'YZZYWhjjY'hYUa kcf\_Yfg"

### HYUWX]b[ GhfUhY[]Yg

HYUWX]b[ 'ghfUhY[]Yg

H\]g`Wci fgY`Wcbg]ghg`cZ]bhY[ fUhYX``YWfi fYžhi hcf]U``UbX`dfUWf]WU``k cf\_": cf'h\Y`Z]fghZci f`k YY\_g`cZh\Y gYa YghYf'h\YfY`k]```VY`U'`h\fYY`\ci f`dYf]cXžk\]W\`k]```]bWi XY`U``YWfi fY`UbX`ga U```[ fci d Yl YfW]gYg#i hcf]U`gž[ fci d`X]gWi gg]cbg`UbX`ch\Yf`a Yh\cXg`hc`ZUWj`]hUhY`ghi XYbh`YUfb]b[ "5`hYfbUhY``YWfi fY`k YY\_g`k]```VY`Zc``ck YX`i d`k]h\`\ca Yk cf\_`Ugg][ ba Ybhgžk\]W\`ghi XYbhg`k]```HU\_Y Uk UmUbX`gc`j Y`UbX`gi Va]hih\Y`Zc``ck]b[ `k YY\_`Zcf`UggYgga Ybh''H\YgY`k]```Wcbhf]Vi hY`hck UfXg`h\Y ZbU``Wci fqY`a Uf\_"

 $\label{thm:condition} $$H\YfY'k ]^*VY'U'ei ]n'UggYgga Ybh]b'K YY_'+Wcblf]Vi h]b['hc'h\Y'Z]bU'a Uf_"'H\]g'k ]^*Ugg]ghk ]h\ gc`]X]Zm]b['h\Y'h\Ycfm'UbX'WcbhYbh'Wcj YfYX']b'h\Y'YUf`]Yf'k YY_gz'VYZcfY'h\Y'`UVcfUhcfm'gYgg]cbg'ghUfh ]b'h\Y'Zc``ck ]b['k YY_g"$ 

: fca 'K YY\_') 'hc'K YY\_'%\$ž'U'gYhcZ`UVcfUhcfmiYl dYf]a Ybhg'k ]``VY'WcbXi WhYX'hc'\Y`d'XYj Y`cd'U dfUWf]WU``UbX']bhi ]hjj Y'i bXYfgHUbX]b[ 'cZU'gY`YWf]cb'cZgYbgcfg'hmdYg" 5 'Z]bU``Yl hYbXYX'fYj ]g]cb'hi hcf]U``k ]```VY'[ ]j Yb']b'UXj UbWY'cZh\Y'Z]bU``UggYgga Ybh'

## 5XX]hjcbU`7ci fgY ±bZcfa Uhjcb

DfYgi a YX \_bck `YX[Y

5 [ccX VUW\_[fci bX']b a Uh\Ya Uh\Ya Uh\Wg'UbX'd\mg]\Wg']g'YggYbhJU'"6Ug]\W\_bck `YX[Y'cZW\Ya ]ghfm]g'Uggi a YX" Gca Y'\_bck `YX[Y'cZY'YWf]\WD'Yb[]\bYYf]b['k ci `X'U'gc'VY'YI hfYa Y'm'UXj UbhU[Yci gž'U'h\ci [\'h\Y'VUg]\Wg k]``VY'Wcj YfYX']b'h\Y'YUf'm'YWh fYg"'H\Y'A 5H@56'dfc[fUa a ]b['Ybj]fcba Ybhk]``VY'i gYX']b'h\Y `UVcfUhcf]\Yg'UbX'Ug'dUfhcZgca Y'\ca Yk cf\_'YI Yf\WgYz'gc'\ZJa]']\Uf]\mik ]h\'A 5H@56'cf'gca Y'ch\Yf dfc[fUa a ]b['`Ub[i U[Y'k]``VY'\Y'd\Z']Z'\mci 'Ybfc'']b'h\]g'\Wci fgYz'Ub'UXX]\h]cbU'`A ccX'Y'a cXi 'Y'k]``VY a UXY'Uj U]`UV'Y'hc'mci 'k\]\W.'\WcbHJ]bg'gca Y'A 5H@56'h hcf]U'`a UhYf]U'zj ]XYcg'UbX'ei ]nnYg'hc'\Y`d'Vf]b[mci 'i d'hc'gdYYX"

.

 $\label{eq:continuity} $$H\]g'UggYgga\YbhUXXfYggYg'`YUfb]b[\ ci \ hMca\ Yg.\ @%2@&2@\ 2@(\ "$ 

FY`UhYX'[fUXiUhY`WUdUV]`]h]Yg.; &ž '"

H\]g^]g^bch'U^Hi fb]h]b^Ugg][ ba Ybh

5ggYgga Ybh' . <ca Yk cf\_Ei Ygh]cbg

GHJfh'XUh'Y. '%( #\$&#&\$&' '%\$.\$\$'5A 8i Y'XUh'Y. '%'k YY\_'Zfca 'h\Y'ghJfh'XUh'Y

5 'a U'cf'UgdYWficZh\]g'Wci fgY']g'dfcV'Ya 'gc'j ]b["'H\]g'YbhU]`g'Wkccg]b['h\Y'Uddfcdf]UhY'a cXY`ž ]a d'Ya Ybh]b[']hWcffYWfimUbX'Uff]j ]b['Uhih\Y'WcffYWfiUbgk Yf"'Hc'Wca d'YhY'h\Y'\ca Yk cf\_'ei Ygh]cbgž ghi XYbhg'k ]``i gY'Z bXUa YbhU``a UhYf]U``Zfca 'h\Y``YWfi fYg'UbX'hi hcf]U`g"'5gg][ ba Ybhg'g\ci `X'VY'gi Va ]hhYX cb'h]a Y"'A Uf\_g'k ]``VY'XYXi WhYX'Zcf``UhY'gi Va ]gg]cb'k ]h\ci hdf]cf'Uddfcj U`"

.

H\]g`UggYgga Ybh'UXXfYggYg``YUfb]b[ `ci hWca Yg.`@%z`@\z`@\ z`@( z'@) "

FY`UhYX'[fUXi UhY`WUdUV]`]h]Yg.'; %ž'; &ž'; 'ž'; ("

H\]g']g'bch'U'Hi fb]h]b'Ugg][ ba Ybh

### 5XX]h]cbU`XYhU]`g

.

5ggYgga Ybh(.:]bU`9l Ua

 $\begin{array}{ll} \textbf{GHUfhXUhY}. \text{ 'H} Y \text{ 'gHUfhXUhY} \text{ 'k }] \text{``VY} \text{`XYhYfa} \text{ ]bYX} \text{``UhYf} \\ \textbf{5ggYgga} \text{ Ybh} \text{`Yb} \text{ [h\.'' \circ} \text{ fg} \\ \end{array}$ 

 $\label{eq:continuity} $$HY'Z_bU'Y'U'Z_cfa 'g]_a 'Uf'hc'hY'a ]X!gYgg]cb'ei ]n'z'Wcbg]gh]b['cZU'a]I'cZX]gW'fg]jY'bU'YI'Ua'k ]$$$ 

FY`UhYX'[fUXiUhY'WUdUV]`]hJYg.;'"

### 5ggYgga Ybh). A U'cf@UVcfUhcfmF Ydcfh

GHJfhXUHY. %(#\$'#&\$&' \*\\$.\$\$ 5A 8i Y XUHY. \$) #\$) #&\$&' \*\%) - DA

#i]g'Yl dYWYX'h\Unghi XYbhg'k ]```UhtYbX`U````UVcfUhcfmiWUggYg'UbX`XcW a YbhfYgi `hg'UbX`X]gW gg]cb']b'U Zcfa U```UVcfUhcfmiVcc\_"'H\]g'Vcc\_'k ]```VY`a Uf\_YX`YUW\ k YY\_`fUhih\Y`ghUfhcZh\Y``UV`Zcf'h\Y`UbU`mg]g'UbX X]gW gg]cb'cZh\Y'dfYj ]ci g'k YY\_g'Yl dYf]a Ybhgž'UbX`Uhih\Y'YbX'cZh\Y``UV`Zcf'h\Y`fUk 'XUhU'cZh\Y`W ffYbh k YY\_g'Yl dYf]a YbhgŁ'Zcf'Wca d'YhYbYgg'UbX`Wcbg]ghYbWnk ]h\'U'gYhcZ`UVcfUhcfmbchYVcc\_'[i]XY`]bYg'h\Uh k ]```VY'gi dd`]YX'hc'h\Y'ghi XYbh'

.

H\]g`UggYgga YbhUXXfYggYg``YUfb]b[ `ci tWta Yg.`@%ž@&ž@ ž@( ž@) "

FY`UhYX`[fUXiUhY`WUdUV]`]h]Yg.; %ž; &ž; 'ž; ("

H\]g^]g^bchU^Hi fb]hb^Ugg][ ba Ybh

# 5 hmy b X Ub WY F Yei ] f Ya Yb hg

 $\hbox{Ghi XYbhg'UfY'ghfcb[`m'YbWc'i fU[YX'hc'UhhYbX'U```WUggYg'UbX'fYj]Yk'``YWhi fY'fYWcfX]b[g''' } \\$ 

7ci fgY GWX YXi `Y

				_

			&\$h\ A Uf	Htiuhcofjuliagijsowih Xijlo(din g E/5 'Zof'a]X!HYfa Yl Ua	
K YY_`+.`&+`A UfWX`!`' % A UfWX	5ggYgga Ybh	K YY_ +	<b>Solutive</b> &, th A UfVX	Hacp  W   ?;6产7?7EF7D  QG; Lz	hidingr DhiBn\60
K YY_', .'' '5df]`'! '+'5df]`	@UNACCE Ware form y	K YY_			

# FYgci fW/g

## DfYgWf]VYX F Ygci fWYg

C b`]bY`Wci fgY`a UhYf]U``WUb`VY`UWWYggYX`h\fci [\`A ccX`Yžk\]W\`]g`a UbU[YX`Vmih\Y`I BGK `HYW\bc`c[m 9bUV`YX`@YUfb]b[`UbX`HYUW\]b[`i b]h`\hdg.##a ccX`Y"hY`h'i bgk "YXi "Ui "`C bWY`mci `UfY`Ybfc``YX`]b`h\Y Wci fgYž6€A-\*)\$`k]```VY`j ]g]V`Y`hc`mci `UZhYf`h\Y`gYgg]cb`ghUfhgž`k\Yb`mci ``c[`]bhc`A ccX`Y`i g]b[`mci f nDUgg"

Hi hcf]U``hUg\_gž[fci d`X]gW gg]cbgž`YWh fY`bchYg`UbX`fYgci fWra UhYf]U`g`k]```VY`a UXY`Uj U]`UV`Y`cb`h\]g`g]hY Xi f]b[ `gYgg]cb"`5bbci bWra Ybhg`a UXY`cb`A ccX`Y`k]```VY`Zcfk UfXYX`hc`mci f`ghi XYbhYa U]`/mci `UfY fYei]fYX`hc`WXYW\_mci f`ghi XYbhYa U]``ZfYei YbhmZcfi dXUhYg"`

Gca Y'i gYZ ``fYZYfYbWY'Vcc\_q'h\Uh'UfY'\Y`X']b'h\Y'I BGK '@]VfUfm'UfY.

# Gi Va ]gg]cb cZ5ggYgga YbhHUg\_g

@UVcfUlrcfmfYdcfhg`UbX`a U'cf`Ugg][ ba Ybhg`k]``fYei]fY`U`<u>Bcb`D`U[]Uf]ga `8YWUfUh]cb`7cjYf`G\YYh</u>'

5gg][ ba Ybhgʻg\ci `X`VYʻgi Va ]hhYXʻcbʻhja Y"`5`XU]`mdYbU`hmcZ) ı `cZh\Y`a Uf\_gʻUj U]`UV`YʻZcfʻh\Uh Ugg][ ba Ybhk ]```Udd`m'Zcfʻk cf\_ fYVW]j YX`UZhYfʻh\Y`Xi Y`XUhY"`5bmUgg][ ba Ybha cfYʻh\Ubʻ) `XUmg``UhYʻk ]``bch VY`UWWdhYX"'H\Y`cb`mYl Ya dhjcbʻk ]```VYʻk \Ybʻdf]cfʻdYfa ]gg]cbʻZcf``UhYʻgi Va ]gg]cbʻ\UgʻVYYbʻ[ fUbhYX`Vm h\Y`7 ci fgY`WccfX]bUhcf"'9I hYbg]cbgʻk ]```VY`[ fUbhYX`cb`mcbʻa YX]WU``cf`Wca dUgg]cbUhYʻ[ fci bXgʻi bXYf YI hYa Y`W]fW a ghUbWfg"

# 5 WUXYa ]W<cbYghmUbX D`U[]Uf]ga

D@5; =5F =€A

6Yk UfY"5b'Ugg][ ba Ybhih Uh]bWi XYg'd'U[ ]Uf]gYX'a UhYf]U`'k ]``'fYWY]j Y'U'\$i ': U]`ž'UbX'ghi XYbhg'k \c d'U[ ]Uf]gY'k ]``'\Uj Y'h\Y]f'bUa Yg'YbhYfYX'cb'U'd'U[ ]Uf]ga fY[ ]ghYf'UbX'k ]``'\Uj Y'h\Y]f'bUa Yg'YbhYfYX'cb'U'd'U[ ]Uf]ga fY[ ]ghYf'UbX'k ]``'VY'`]UV'Y'hc'X]gW]d']bUfmUW]cbž']bWi X]b[ 'YI Wi g]cb'Zfca 'Ybfc`a Ybh'''

♣i]g'YI dYWYX'h\Uh'U``'ghi XYbhg'a i ghUh'U``'h]a Yg'gi Va ]hh\Y]f'ck b'k cf\_'Zcf'UggYgga Ybh''Gi Va ]hh\b (h\Y k cf\_'cf']XYUg'cZgca YcbY'Y`gY'k ]h\ci h\WYUf'mUW\_bck `YX[ ]b[ 'h\Y'gci fW'cZVcffck YX'a UhYf]U``cf']XYUg']g d`U[ ]Uf]ga "

## 5 WUXYa ]W = DZcfa Uhjcb

#### 7CI FG9'9J5@I 5H€B'5B8'89J9@CDA 9BH

Ghi XYbhZYXVUW\_`\Ug`\Y`dYX'hc`g\UdY`UbX`XYj Y`cd`h\]g`Wci fgYž`]bWi X]b[ `ZYYXVUW\_`cVhJ]bYX`Zfca `cb! `]bY`Yj U`i Uh]cbg`Ug`dUfhcZl BGK 'g`Ug`dUfhcZl BGK 'g`a m9l dYf]YbWi`dfcWigg"`Mci `UfY`\][ \`m YbWci fU[ YX`hc`Wca d`YhY`gi W\`Ub`cb!`]bY`Yj U`i Uh]cb`hck UfX`h\Y`YbX`cZHYfa "`: YYXVUW\_`UbX`gi [ [ Ygh]cbg dfcj ]XYX`k ]```VY`]a dcfhUbh`]b`]a dfcj ]b[ `h\Y`Wci fgY`Zcf`Z hi fY`ghi XYbhg"

.

#### 85H9G'HC'BCH9

FYZYfihciA ml BGK iZcfi=a dcfhUbh8UhYgžiUjU]iUViYiUh \hhdg.##a mii bgk "YXi "Ui #gh XYbh#Ygci fWYg# Ym8UhYg"\hai

.

### 57589A = 758J = 79

: cf ]bZcfa Uh]cb UVci h

- "Bchyg'cb'Uggygga Ybhg'UbX'd'U[]Uf]ga ž
- · · · · GdYWJU` · 7 cbg]XYfUh]cbgž
- "GWXcc"Gh XYbh9h\]Wa'CZZWYfž'UbX
- .... 69GG

.

#### Gi dd Ya YbhUfm 91 Ua ]bUh cbg.

GiddYa YblUfm91Ua ]bUl]cbg'Zcf'HYfa '%&\$&' k ]``VY'\Y`X'cb'fH67Eg\ci`X'mci VY'fYei ]fYX'lc'g]hcbY"

H\]g`Wci fgY`ci h]bY`gYhg`ci hXYgWf]dh]cb`cZWUggYg`Uhih\Y`XUhY`h\Y`7 ci fgY`Ci h]bY`]g`di V`]g\YX"`H\Y bUhi fY`cZWUggYg`a UmW\Ub[Y`Xi f]b[`h\Y`HYfa `UZhYf`h\Y`7 ci fgY`Ci h]bY`]g`di V`]g\YX"``A ccX`Y`g\ci `X`VY Wcbgi `h\X`Zcf`h\Y`i d`hc`XUhY`WUgg`XYgWf]dh]cbg"``=Zh\YfY`]g`Ubm]bWcbg]ghYbWn]b`h\Y`XYgWf]dh]cb`cZ UWhj ]h|Yg`VYhk YYb`h\Y`I b]j Yfg]lmiha YhUV`Y`UbX`h\Y`7 ci fgY`Ci h]bY`fUg`i dXUhYX`]b`A ccX`Y\Z`h\Y XYgWf]dh]cb`]b`h\Y`7 ci fgY`Ci h]bY#A ccX`Y`Udd`]Yg"

### = a U[Y'7fYX]h

GmbYf[]Yg']b'GcibX'&\$%\*

### 7F = 7CG

7F = 7CG Dfcj ]XYf 7cXY. \$\$\$-,;

### 5W\_bck `YX[ Ya YbhcZ7ci bhfm

 $K Y : UW\underline{b} ck `YX[Y : h, Y : 6YXY[U : dY cd `Y : k \ c : UfY : h, Y : hfUX]h\underline{b} cb : `W : ghcX]Ubg : cZh, Y ``UbXg : cb : k \ ]WX : I BGK ? Ybg]b[hcb : WUa di g : ]g ``cWUhYX"$